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DEDUCTIVE LOGIC

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Clarendon Press Series

THE ELEMENTS

OF

DEDUCTIVE LOGIC

DESIGNED MAINLY
FOR THE USE OF JUNIOR STUDENTS
IN THE UNIVERSITIES

BY

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NINTH EDITION

CORRECTED AND REVISED

@xford

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PREFACE.

THE precise object of the following pages is (without pre-supposing any technical acquaintance with logical terminology) to enable a student of average intelligence to acquire for himself an elementary knowledge of the main problems, principles, and rules of Deductive Logic. They are not designed to save him the trouble of afterwards consulting more advanced text-books, either in his own or other languages. The English student who wishes to gain an exact and detailed knowledge of the relations of Deduction to Induction, and consequently of the true place and value of the former process in any special science, must still have recourse to the works of Mr. Mill; or, if he wish to trace the history of logical terms and doctrines (one of the most important chapters in the history of both ancient and modern literature), he must still consult Sir W. Hamilton's Lectures, and the Appendices and Notes of Dr. Mansel to Aldrich's Logic.

To these works, as well as to Archbishop Whately's luminous Chapter on Fallacies, and to the original and suggestive work of Mr. James Mill on the Analysis of the Phenomena of the Human Mind, the Author must, once for all, express his obligations. He has, however, endeavoured, on all disputed points, to reason out his

own conclusions, feeling assured that no manual, however elementary, can be of real service to the student, unless it express what may be called the 'reasoned opinions' of its author.

The great difficulty to be encountered by any writer of an English Manual of Logic is the unsettled state of our logical terminology. Many words have various significations, or are used in different senses by different writers, and often there are no recognised terms to express some distinction which it is still incumbent on the logician to notice. A fixed and sufficient terminology can, however, only be created by the habit of teaching Logic, and of carrying on our discussions on the science, in our own language. But though, in some respects, the Latin terminology may be superior to our own, there can be no question that the language in which men habitually think must be the fittest medium for analysing their thoughts.

The Notes appended to the Chapters (as distinguished from the foot-notes) are designed to inform the student of any divergences from the ordinary mode of treatment, or to suggest to him further reading on topics which, if noticed at all, are only alluded to in the text. They may be omitted on the first reading.

Besides the Notes appended to the various Chapters, it is perhaps desirable that the student, if he is entirely unacquainted with logical and psychological discussions, should omit, on the first reading, the Chapters on the Relation of Logic to Psychology, on the various Kinds

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of Terms, on the Denotation and Connotation of Terms, on the Relation of the Predicate to the Subject of a Proposition, on Verbal and Real Propositions, on Definitions, and on Divisions and Classifications. Unfortunately, the most difficult problems which the logician has to solve occur at the outset of his task.

It is hoped that, independently of its bearing on University studies, a Short English Manual of Logic may be used with advantage in the Upper Forms of Schools, and that it may not be without interest to the general reader.

The Manuals of Sanderson, Wallis, Aldrich, &c., owing to the peculiar circumstances of the period in which they were written (a period, which, being transitional, retained not only much of the scholastic terminology, but also much of the Realistic doctrine), have ceased to be adapted to modern instruction. The Author, with some misgivings, and a keen sense of the difficulties of the task, trusts that the present work may be found usefully to occupy their place. Its propositions cannot, however, be presented in the same curt and dogmatic shape, for we have learnt to regard many portions of Logic, like many portions of the sciences whose method it claims to analyse, as fairly open to differences of opinion.

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^{*,*} In the Table of Contents it will be observed that the words Definitions, Divisions, Classifications, Inferences, Oppositions, Conversions, Permutations, occur in

place of the more ordinary forms Definition, Division, Classification, &c. The object of this change is to suggest to the student the importance of distinguishing the results from the processes by which they are gained. Many words employed in Logic and Psychology admit of both these meanings, and it is only by prefixing the indefinite article or using the plural number, as when we speak of 'a definition' or 'definitions,' that we can make it plain that we mean the result and not the process. It would be very difficult in all cases to mark the distinction, but I have endeavoured to do so wherever it seemed to be of any importance?

A similar confusion in many of the terms employed in Physics has been noticed by Mr. [now Sir W. R.] Grove (Correlation of Forces, fifth ed., p. 251). 'Another confusion of terms has arisen, and has, indeed, much embarrassed me in enunciating the propositions put forth in these pages on account of the imperfection of scientific language; an imperfection in great measure unavoidable, it is true, but not the less embarrassing. Thus, the words light, heat, electricity, and magnetism, are constantly used in two senses—viz. that of the force producing, or the subjective idea of force or power, and of the effect produced, or the objective phenomenon. The word motion, indeed, is only applied to the effect, and not to the force, and not to the effect; but the other four terms are, for want of a distinct terminology, applied indiscriminately to both.'

PREFACE TO SUBSEQUENT EDITIONS.

IN subsequent Editions several minor alterations and additions have been introduced into the Text of some of the Chapters. A few Notes, as well as an Index and a Collection of Examples, have also been added. In making these alterations and additions, the Author has gladly availed himself of suggestions kindly offered, from time to time, by various correspondents and friends, amongst whom he ought specially to mention Professor Park, of Belfast. He has, however, endeavoured to prevent the work from materially exceeding the limits of its original size.

Several friends have suggested to the Author the introduction of two new chapters, one on the Categories, the other on the Formation of Terms. Influenced partly by a desire not to increase the bulk of the volume, and partly by still more important reasons, he has, after some hesitation, decided against the introduction of these chapters. The doctrine of Categories is important in the history of Logic¹, but it is not properly a branch of Logic, as that word is now generally understood and as it has been understood throughout this work. The Formation of Terms is a subject which properly belongs to Psychology and not to Logic, and moreover could not be adequately treated in a small compass. It is true that some questions properly belonging to Psychology or the History of

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¹ On the categories of Aristotle the reader is referred to Hamilton's Lectures on Logic, Lect. xi., and the Appendix to Mansel's Aldrich, Note B. Both Sir W. Hamilton and Dr. Mansel, especially the former, insist on their 'wholly extra-logical' character.

Logic have been noticed in various parts of the book, but they have only been casually alluded to, not treated in distinct chapters. Logic has always been over-weighted with extraneous matter, and, wherever it is possible, it is desirable to relieve it of its superfluities, though much discretion may be needed in the process, and though the requirements of examinations have a constant tendency to lead writers on Logic to consider not how little, but how much they can introduce into their works.

In the Fifth and subsequent Editions, the Author has added an Appendix on the Heads of Predicables. is no branch of elementary Logic so difficult to state in a form at once satisfactory to the teacher and intelligible to the learner. The attempt at a scientific treatment which he has made in Pt. II. ch. v. is, he believes, usually found too complicated for a beginner. As, however, he cannot state his own view of the doctrine in a simpler form, he has thought it the best course to add an Appendix, which, without any attempt at an exhaustive treatment, simply offers an explanation of the five words, Genus, Species, Differentia, Property, Accident. This Appendix, on the first reading of the book, may be substituted by the student for Pt. II. ch. v., but should be combined with the formal definitions given on p. 45, of which, in fact, it furnishes an explanation.

The principal changes in the eighth Edition are the addition of notes to Pt. III. chs. i. and vii., and some alterations in the text of the latter part of ch. vii.; and, in the present Edition, certain additions to the latter part of ch. vii. and to the foot-note on p. 73.

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ELEMENTS

OF

DEDUCTIVE LOGIC

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INTRODUCTION.

CHAPTER I.

On the Relation of Logic to Psychology.

PSYCHOLOGY, or Mental Philosophy, may be defined as the science which classifies and analyses the phenomena of the human mind. It notes mental phenomena, considers them in their mutual relations, and investigates the mode of their generation. Of these mental phenomena some are called emotional, others intellectual. The intellectual phenomena may be regarded as the result, partly of Perception, partly of Imagination, partly of Comparison, Reflexion, or Thought. Perception is the act or operation of apprehending some present phenomenon. Imagination is the act or operation of representing to the mind some absent phenomenon. Comparison, Reflexion, or Thought, is the act or operation of comparing phenomena, whether present or absent, as well as of comparing, either with these or with one another, the results themselves which we derive from such comparisons. Thus I perceive this particular rose before me, its colour, its smell, and the pleasure I derive

from seeing and smelling it. All these perceptions I can recall to-morrow, even though the rose be absent, by the act or operation of imagination. Lastly, I may compare this particular rose with another which lies on the table, or with one which I saw yesterday, and I may express their similarity by calling them both moss-roses, or their difference by calling one a moss-rose and the other a Tudor rose. Again, moss-rose and Tudor rose, which names are both results of the act or operation of comparison, may themselves be compared, and their points of similarity expressed by the word 'rose.' So rose and dahlia may be compared, and their points of similarity expressed by the word 'flower.' Or I may compare the feeling with which I contemplate the rose with similar feelings which I have previously experienced, and call it 'pleasure'; or I may compare it with the feeling which I experience when I prick my finger with a thorn, and call one 'pleasure,' the other 'pain'; or I may compare pleasure and pain themselves, and call them both 'feelings.' The act of making comparisons, and of apprehending similarities and differences, is usually called Thought or Thinking, and the results at which it arrives Thought or Thoughts. The act or operation itself, as distinguished from other mental acts or operations, and the results which ensue from its correct or incorrect exercise, are alike legitimate subjects of investigation for the psychologist or mental philosopher. But the more detailed consideration of the latter, i.e. Thoughts or the results of Thinking, becomes the subject

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of a science with a distinct name, Logic, which is thus a subordinate branch of the wider science, Psychology.

Note 1.—The term Perception is here used in its ordinary sense. The distinctions between External and Internal Perception, Perception Proper and Sensation Proper, are foreign to the present subject. They are discussed at great length in the works of Sir William Hamilton and Dr. Mansel, as well as in those of the Scottish school of metaphysicians generally, but, as involving some of the most abstruse and disputed questions in Psychology, it is not necessary or desirable that the student should acquaint himself with them till he commences the special study of that science.

Note 2.—Imagination, as here defined, is what may be called Simple, or Reproductive, as distinguished from what may be called Complex, or Productive Imagination. The former simply represents to the mind absent objects of perception as they have already been perceived, the latter combines phenomena or portions of phenomena, whether absent or present, into a new whole. Thus the notions of a particular man or a particular horse, if the man and horse be absent, are products of simple or reproductive imagination; the notion of a centaur would be a product of complex or productive imagination. For further and more precise information on this distinction, which is here necessarily stated somewhat roughly,

RELATION OF LOGIC TO PSYCHOLOGY.

see Sir W. Hamilton's Lectures on Metaphysics, Lect. xxxiii. The creations of poetry and art are results of complex imagination, or, in other words, of repeated processes of simple imagination and comparison. Inasmuch as complex imagination may be analysed into simple imagination and comparison, and is thus not one of the ultimate acts or operations to which our mental phenomena are traceable, it would have been beside my purpose to have noticed it in the text.

Note 3.—I have employed the expression 'act or operation,' avoiding the expression 'power or faculty,' as the latter implies a theory of mental phenomena which would be rejected by many psychologists. It has been necessary to speak of 'act or operation,' as the word 'act,' like many other terms of logic or psychology, may mean either the operation or the result. This is an instance at the very outset of the ambiguity noticed in the paragraph at the end of the preface.



CHAPTER IL

Definition of Logic.

IT is the province of Logic to distinguish correct from incorrect thoughts, i.e. to analyse those thoughts which are accepted by mankind as indubitably correct, and to point out wherein they differ from those which are regarded as doubtful or incorrect; and, as a consequence of this function, it is also its province to lay down rules for the attainment of correct thoughts and for the avoidance of incorrect thoughts. Thus Logic is both a Science and an Art. It is a Science, inasmuch as it furnishes us with a knowledge of what is, inasmuch as it is an analysis, and determines the conditions on which valid thoughts depend. It is an Art, inasmuch as it lays down rules for practice, and thus enables us to detect incorrect thoughts in the reasonings of others, and to avoid them in our own.

Logic may therefore be defined as the science of the conditions on which correct thoughts depend, and the art of attaining to correct and avoiding incorrect thoughts.

Note.—This definition is in substance that given by Mr. Mill in his Examination of Sir W. Hamilton's

Philosophy, p. 391 (third ed., p. 448). 'Logic,' he says, 'is the art of thinking, which means of correct thinking, and the science of the conditions of correct thinking.' The word 'thoughts' is substituted for 'thinking,' in order to bring more prominently before the student, what Mr. Mill himself acknowledges, the fact that Logic is concerned with the products or results rather than with the process of thought, i.e. with thoughts rather than with thinking, though, in estimating the conditions on which · correct thoughts depend, it is necessary, to some extent, to take account of the processes by which they are formed. It seems also desirable to introduce into the definition of Logic some reference to 'incorrect thoughts,' as bringing out more distinctly the character of Logic as an art, and asserting for it the right of investigating fallacies.



CHAPTER III.

On the Relation of Thought to Language.

WHETHER it is possible to think without the aid of language, is a question which has been a constant source of dispute amongst logicians and psychologists. It is not necessary, however, here to enter on this discussion. As all logicians are agreed that we cannot communicate our thoughts without the aid of language, or of equivalent signs, and that practically we do always think by means of language, by a sort of internal converse, it will be safer to adopt the terminology of those authors who regard our thoughts as expressed in language rather than that of those who consider or attempt to consider them in themselves as apart from their expression in words. I shall therefore speak of Terms and Propositions, not of Concepts and Judgments.

Note.—Sir W. Hamilton and his followers, regarding Logic as primarily and essentially concerned with thought, and only secondarily and accidentally with language, attempt to mark the products of thought by words which do not imply their expression in language. Thus, instead

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of Terms and Propositions, they use respectively the words Concepts and Judgments. The word Syllogism, owing to the ambiguity of the Greek word λόγος, stands either for the internal thought or the external expression of it. (See Hamilton's Lectures on Logic, Lecture i.)



CHAPTER IV.

Division of the Products of Thought.

IT has been stated that thought is the act or operation Its simplest result is that which is exof comparison. pressed by the Term. Terms may be combined into Propositions, and Propositions, either singly or in conjunction with one or more other propositions, may lead I shall treat in order of the Term, to Inferences. of the Proposition, of Inferences. Before proceeding further, it may perhaps be useful to the student to give by anticipation instances of these products or results of thought. Man, good, manliness, goodness, the goodness of man, the virtue of manliness, are all instances of terms. 'This man is good,' 'All citizens of a state are under an obligation to obey its laws,' are instances of Propositions, and, according to logical phraseology, 'good' is said to be predicated of 'this man,' and 'under an obligation to obey its laws' is said to be predicated of 'all citizens of a state.' The term predicated is called the Predicate, and the term of which it is predicated is called the Subject, the word 'is' or 'are' (or, in the case of negative propositions, 'is not' or 'are not'), which connects the two, being called the Copula. Lastly, we may take as instances of Inferences the following:-

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10 DIVISION OF THE PRODUCTS OF THOUGHT.

No rectilineal figure is contained by less than three lines;

Therefore, no figure contained by less than three lines is a rectilineal figure.

All Englishmen are of mixed descent,

This is an Englishman;

Therefore, he is of mixed descent.

The last proposition (which is called the *conclusion*) is said to be *inferred* from the proposition or propositions which precede it (called the *premiss* or *premisses*).



PART I .- THE TERM.

CHAPTER I.

On the Various Kinds of Terms.

A TERM (so called from terminus, a boundary, because the terms are the two extremes or boundaries of the proposition) is a word or combination of words which may stand by itself as the subject or predicate of a Proposition; it expresses either an individual, a group of individuals, an attribute, or a group of attributes. This definition obviously excludes all articles, adverbs, interjections, conjunctions, prepositions, and oblique cases of It also excludes verbs; for though a verb expresses attributes, and often serves at once for the copula and the predicate (or part of the predicate), as in the propositions 'John walks,' 'William fears Thomas,' it must, in a logical proposition stated according to strict form, always be analysed into the copula and participle: thus the above propositions, when stated logically, become 'John is walking,' 'William is fearing Thomas 1.' A

A proposition of which the verb is not analysed into the copula and a participle is called by the older logicians 'secundi adjacentis,' in contradistinction to the form of proposition as ordinarily stated in Logic, which is called 'tertii adjacentis.' Thus vir currit is a proposition secundi adjacentis, vir est currens is a proposition tertii adjacentis.

pronoun is only significant as standing in the place of a substantive, and therefore we may limit ourselves to the consideration of substantives, adjectives, and participles.

By the older logicians a term was defined as a Cate-gorematic word (from κατηγόρημα 'something which can be predicated'), i.e. a word or combination of words which can stand by itself as the predicate of a proposition. All words or combinations of words which require to be joined with some other word or words in order to serve this purpose were called Syncategorematic words.

It has been said that a term expresses an individual, a group of individuals, an attribute, or a group of attributes. If it expresses an individual, as Socrates, the present Queen of England, the sea, hic, ille, hoc, illud, &c., it is called a (1) Singular Term. If it expresses a group of individuals, it may either be applicable to each individual of the group severally as well as to the group collectively, or to the group collectively but not to each individual severally. Thus the terms, man, horse, flower, are not only applicable to each individual of the groups which they express, but also to the groups collectively; I can say, 'John is a man,' 'Thomas is a man,' 'this is a horse,' 'that is a horse,' 'the rose is a flower,' 'the dahlia is a flower,' &c. But I cannot say 'Caius is the fourteenth legion,' 'Pompey is the Roman senate,' though I can predicate 'fourteenth legion' or 'the Roman senate' of the groups, taken collectively, which these terms express. In the former case the term is called a (2) Common Term, in the latter a (3) Collective

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Term. A collective term may by a slight change of phraseology be expressed as a common term; thus, 'Roman senate' may become 'Roman Senators,' or 'fourteenth legion' 'soldiers of the fourteenth legion.' But, as it stands, a collective term is, in predication, as will be noticed hereafter, equivalent to a singular term.

A common term is equally applicable to each individual severally of the group which it expresses, and it is so in virtue of certain points of similarity which all the individuals possess in common. It is in fact because we have observed that they all possess certain attributes in common, that we are able to call them by a common name. Thus a common term, like man, horse, &c., at once suggests to me a certain group of individuals and a certain group of attributes which is predicable of each of these individuals severally. But there are other terms, called (4) Attributives, and (5) Abstract Terms, which express attributes or groups of attributes only. Attributives may be distinguished from Abstract Terms by the fact that they may form the predicate, but cannot, unless joined with a singular, collective, common, or abstract term, form the subject of a proposition. Grammatically, they are represented by adjectives and participles, when not used substantively. Of this class are the terms, human, red, heavy, brave, willing, thinking, running, &c., when not used substantively. Thus I may say, 'Socrates is human,' but, when I wish to employ the term 'human' in the subject of a proposition, I must append to it some such word as 'being,' and say 'this human being is

Socrates.' Such terms have, in fact, no signification, unless used substantively, or in conjunction with a substantive, either as qualifying it or as predicated of it.

Abstract Terms, on the other hand, not only express mere attributes or groups of attributes, but may be thought of without any reference to the individuals of which these attributes are predicable. Of this class are such terms as humanity, colour, figure, fortitude, &c. To it may be referred sentences employing the indicative mood and introduced by the word 'that,' infinitive moods, some instances of adjectives and participles used substantively, and generally every term, being neither singular, collective, nor common, which may be employed both as the subject and as the predicate of a proposition.

All the terms discussed above may be employed as predicates of propositions. Attributives alone cannot be employed as subjects.

We have thus divided terms into singular, collective, and common terms, attributives, and abstract terms. It must however be borne in mind that many of those attributives and abstract terms which are most frequently in use, or which have been for a long time in use, have come to be employed as common terms. Thus we sometimes speak of red, good, virtue, figure, number, pleasure,

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It is perhaps hardly necessary to remark that in such phrases as 'Great is Diana of the Ephesians,' 'Great is my rejoicing,' the places of the subject and predicate are reversed, for the sake of laying greater emphasis on the predicate. In a logical analysis of such propositions, the subject and predicate must be restored to their normal positions.

colour, &c. (both in the singular and plural number), exactly as if they were common terms, though they still retain in other connexions their use as abstract terms or attributives. This remark will be found of great importance in some of the subsequent sections.

Note 1 .- Nothing has been said above of the common distinction between abstract and concrete terms. An abstract term would be defined as a term expressive of an attribute or group of attributes considered apart from the individuals of which it is predicable; a concrete term as a term expressive of an attribute or group of attributes considered in reference to the individuals of which it is predicable, as well as of an individual or group of individuals itself. The terms John, the tenth legion, man, human, would all be called concrete; humanity would be called an abstract term *. It will be noticed that I have availed myself of the expression 'abstract term,' but avoided, as too wide to be of practical service, the contrasted expression 'concrete term.' Concrete terms include what I have called attributives, as well as singular, collective, and common terms.

^a Mr. Mill (Logic, bk. i. ch. ii. § 4) states that Locke and several later writers have applied the expression 'abstract name' to all general names, that is, attributives and common terms as well as what I have called abstract terms. This statement, however, is not uniformly true of Locke. See, for instance, Essay, bk. iii. ch. viii. Mr. Mill himself, following the practice of the Schoolmen, takes the expression in the same limited sense as in the text. By the older logicians singular and collective terms were not regarded as concrete, no account being taken of them in this distinction.

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Note 2.—The term 'attributive' (which has already been employed by Harris and James Mill) is used in preference to the term 'adjective,' both because it includes participles, and because it seems undesirable in a work on Logic to employ a technical term of Grammar. Harris (Hermes, bk. i. ch. vi.) includes amongst 'attributives' verbs; but a verb, as has already been stated, is, in Logic, always represented by the copula and a participle.

I have placed attributives before abstract terms, because they are more nearly allied to singular, collective, and common terms, being, for the most part, either predicated of these terms or employed to qualify them. They seem also as a rule to precede abstract terms in their formation. Thus human, red, brave, good, willing, must have been employed before the corresponding terms humanity, redness, bravery, goodness, willingness.

Note 3.—For the sake of completeness, I have spoken of a term as expressing an attribute or a group of attributes. There is however no distinct name for a term expressing a single attribute incapable of analysis, and the only peculiarity of such terms is, as will be seen below, that they are incapable of definition. Locke called attributes which were incapable of analysis 'simple ideas,' but the expression 'simple term' would not be applicable in a corresponding sense.

Note 4.—That common terms, attributives, and abstract terms are formed from a comparison of individual objects or groups of objects, and that consequently they are results of thought, is obvious. But it may not be so

easy to perceive that this is the case with singular and collective terms. These terms however are appropriated to individual objects or groups of objects in order to distinguish them from others, and the necessity for such distinction can only arise after a comparison of this or that individual or group with others, and a perception of certain points of resemblance and difference between them. Unless I had observed some difference between John and Thomas, this table and that, the thirteenth legion and the fourteenth, it would never have occurred to me to distinguish them by separate names; but this very observation of a difference involves an act of comparison, and consequently an act of thought.

Note 5.—It is important to notice that in a series of terms, like man, human, humanity, all expressing the same attributes, the later and more abstract terms can hardly fail to suggest the earlier and more concrete, and it is so because the earlier terms of the series have been longer formed and are therefore, as a rule, more familiar to us. Thus 'humanity' can hardly fail to suggest to us the word 'human,' from which it is formed, and 'human' will suggest the word 'man,' from the Latin equivalent of which it is also formed, and whose attributes it expresses. Nor can we use the word 'man' without thinking of this or that individual man with whom we are familiar. A common term, in fact, expresses simply an individual object divested of all its peculiar attributes, and regarded as possessing only those attributes which it has in common with all the other objects which are desig-

nated by the same name. But it is indifferent on which object of the group the mind concentrates its attention, and we are all along conscious that the particular object selected is simply representative of the group. And hence it is that a common name simultaneously suggests to the mind a group of individual objects and a bundle of attributes characteristic of that group. For a further discussion of this subject, see Hamilton's Lectures on Metaphysics, Lect. xxxv. and xxxvi.; Mansel's Prolegomena Logica, ch. i.; and Mill's Examination of Hamilton, ch. xvii.

Note 6.-Mr. Mill maintains that attributives, when employed as predicates, are really common terms. Thus the propositions 'All triangles are three-sided,' 'All wise men are just,' are regarded by him as only abbreviated modes of saying 'All triangles are three-sided figures,' 'All wise men are just men.' I should allow that the attributive in the predicate, when taken in conjunction with the subject, always suggests a common term which may be substituted for it, as in the syllogism 'All wise men are virtuous, All virtuous men are happy; ... All wise men are happy.' But, though the attributive may always admit of being expressed as a common term, while it continues to be expressed as an attributive there seem to be present to the mind only attributes, whereas, when it becomes a common term, there seems also to be present a group of individuals possessing those attributes.

CHAPTER II.

On the Denotation and Connotation of Terms.

A TERM may be said to *denote* or designate individuals or groups of individuals, to *connote* or mean attributes or groups of attributes ¹.

¹ It ought, perhaps, to have been stated in the earlier editions of this work that the term *connotation* is here employed in a somewhat different sense from that which is attached to it either in the scholastic logic or in the system of Mr. Mill.

In the scholastic logic, a *connotative* term is 'one which primarily signifies an attribute, secondarily a subject,' as 'white,' the contrasted term being called an 'absolute term,' as 'man' or 'whiteness.' See Mansel's Aldrich, cap. 1, § 3, note g.

According to Mr. Mill's nomenclature, a connotative term is one which 'denotes a subject and implies an attribute.'

By Mr. Mill, not only singular and collective, but also abstract terms are regarded as non-connotative. In the scholastic logic, what I have called attributives are alone recognised as connotative terms. See Mill's Logic, Bk. I. ch. ii. § 5.

As the term is already employed with so much uncertainty, it appears to me not mexcusable to claim still further licence, and to appropriate the expressions 'denotation' and 'connotation' of 'terms' in a sense parallel to that which is expressed by the distinction between the 'extension' and the 'intension' of a 'notion' or 'concept,' applying 'denotation' simply to the objects, and 'connotation' simply to the attributes which are signified by a term. This is a broad and exceedingly convenient distinction, and, notwithstanding the apparent paradox involved in it, namely, that 'abstract terms are not denotative,' I believe that the general employment of the expressions in this sense would considerably simplify the statement and explanation of many logical difficulties.

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In the first place, a term may serve to denote or point out an individual object or group of individuals. Thus 'Socrates' denotes or points out and distinguishes from all others the individual man Socrates. The expression 'tenth legion' denotes or points out, and distinguishes from all other collections of men, the particular group known as the tenth legion. Similarly, the word 'man' denotes or points out, and distinguishes from all other groups, a certain group of individuals to each member of which and to each member of which only the word 'man' may legitimately be applied. All terms of this kind, therefore, viz. singular, collective, and common terms, are denotative; but terms like human, white, humanity, whiteness, i.e. attributes and abstract terms, are not denotative, except mediately, that is, so far as they suggest the common terms 'human beings,' 'white things.'

In the second place, a term may serve to connote attributes or groups of attributes. Thus terms like humanity, human, man, viz. abstract, attributive, and common terms, are all connotative, that is, they at once suggest or imply attributes. But singular and collective terms like 'Socrates,' 'the tenth legion,' are not connotative, except so far as they suggest common terms. This remark requires some explanation. A collective term like 'the tenth legion,' 'the House of Commons,' at once suggests the corresponding common term, 'soldiers of the tenth legion,' or 'members of the House of Commons'; and this common term may

connote any number of attributes, but, as the attributes are suggested mediately through the common term and not directly by the collective term, the collective term is, strictly speaking, non-connotative. The same is the case with a singular term. A term like 'William' may suggest to me 'man,' 'male,' 'Englishman,' 'one of my friends,' &c., and so may become connotative, but it is in itself rightly regarded as non-connotative, inasmuch as it suggests to me these attributes only through the medium of the common terms to which it is referred.

It appears therefore that common terms are both denotative and connotative; that singular and collective terms are denotative, but not connotative; that abstract terms and attributives are connotative, but not denotative; and finally, that mediately, as suggesting common terms, any non-connotative term may become connotative and any non-denotative term denotative.

Note.—The distinction between the denotation and connotation of a term is often otherwise expressed, as that between the extension and intension (or comprehension), or the extensive and intensive (or comprehensive) capacity, or the breadth and depth, of a notion. Having adopted the phraseology which designates the simplest product of thought as a term, instead of a notion, I shall speak of the extensive and intensive (or comprehensive) capacity of a term. The extensive capacity of a term is measured by the number of individuals which it

designates (denotes), the intensive or comprehensive capacity of a term by the number of attributes which it includes, suggests or implies (connotes). It is plain that in a series of common terms, standing to one another in a relation of subordination, the denotation and connotation, or the extensive and intensive capacities, of the term are so related, that as the one increases the other decreases, and vice versâ. Thus, if we arrange in order any series of common terms, as flower, rose, moss-rose, we see that 'flower,' which implies the smallest number of attributes, is applicable to the largest number of individuals; 'moss-rose,' which is applicable to the smallest number of individuals, implies the largest number of attributes: and generally in any series of common terms arranged in subordination, the larger the denotation or extensive capacity, the smaller is the connotation or intensive capacity, and vice versa. In conformity with this principle, the singular term which stands for the individual, and is smallest in denotation, is, when we refer it to the various common terms which may be predicated of it, and so assign to it mediately an intensive capacity, the largest in connotation. Thus the term Socrates, when I regard it as expressing one who was a philosopher, a teacher, a martyr, a soldier, an Athenian citizen, &c., &c., suggests to me far more attributes than any one of these common terms singly.

PART II.—THE PROPOSITION.

CHAPTER 1.

On the Subject and Predicate.

A PROPOSITION asserts or denies, as the result of comparison, some word or combination of words of some other word or combination of words, as e.g. 'James is the man I saw yesterday'; 'No rectilineal figure is contained by less than three lines'; 'Some stars are not planets.' As before stated, the words or combinations of words thus employed are called terms, the term affirmed or denied is called the predicate, the term of which it is affirmed or denied the subject, the connecting verb, whether qualified or not by the negative particle, the copula, and the predicate is said to be predicated of the subject. In the above examples, 'the man I saw yesterday,' 'contained by less than three straight lines,' and 'planets' are predicates and are predicated respectively of 'James,' 'all rectilineal figures,' and · 'some stars,' as subjects. In the first case the predicate is predicated affirmatively, a fact which is expressed by the copula 'is'; in the two last negatively, a fact which is

expressed by the copula 'is not.' These remarks may appear inconsistent with the form of the second example, but 'no rectilineal figure is, &c.' is really an abbreviated and unambiguous mode of stating the longer and ambiguous proposition 'All rectilineal figures are not, &c.'

The word 'predicated,' as equivalent to 'asserted or denied,' is here used in a wider than its ordinary signification. In common language, we say such and such an attribute cannot be predicated of such and such a term, using 'predicated' as equivalent to 'asserted' and as opposed to 'denied.' All ambiguity may be avoided by speaking of the predicate as predicated affirmatively or predicated negatively of the subject.

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CHAPTER II.

On the Copula.

THE Logical Copula, it being its office simply to serve as a sign of predication, is limited to the present tense of the verb 'to be,' with or without the addition of the negative particle, according as the proposition is negative or affirmative. This limitation follows from the fact that it is simply the office of the proposition to express my present judgment as to the compatibility or incompatibility of two Hence all reference to time, past or future, and even to time present, as respects the terms themselves, and not my judgment as to their compatibility, must be expressed in the predicate and not in the copula. I may, for brevity's sake, say 'fire burns,' 'Alexander was the son of Philip,' 'The guns will be fired to-morrow,' and, in conversation or discussion, it would undoubtedly be pedantic to express the propositions otherwise; but formally, for the purpose of being estimated logically, I must resolve them into their logical elements, and say 'Fire is burning,' 'Alexander is a person who was son of Philip,' 'The firing of the guns is an event which will take place to-morrow."

Not only does the logical copula convey no notion of time with reference to the terms themselves (or, to speak more accurately, the things signified by them), but it is also divested of the notion of existence. In other words, it is employed simply as a connecting particle, not as a substantive verb. Where the substantive verb is used in a logical proposition, it must be expressed in the predicate. Thus 'I am,' 'The king is not,' become 'I am existent,' 'The king is non-existent.' That the copula implies no notion of existence is evident from the fact that we can use such propositions as these: 'The labours of Hercules are a myth,' 'He is a nonentity.'

Can we modify the copula so as to express certainty, probability, possibility, or other modes of connexion between the subject and the predicate? This is the celebrated question of Modality, a question which has been the source of much difference of opinion amongst logicians. Even though it were granted that the proposition simply expresses our present judgment on the compatibility or incompatibility of two terms, it might be maintained that it should express the nature of our judgment and the degree of our assent or dissent, whether it be certain, approximating to certainty, or faltering. Thus it might be maintained that the following should be accepted as instances of the ultimate analysis of a logical proposition: 'This is certainly the man I saw yesterday,' 'This is probably the man I saw yesterday," 'This is possibly the man I saw yesterday.' That we use these forms in conversation and discussion is unquestionable, but it is one main object of Logic to analyse our abbreviated inferences and statements into their full logical equivalents. Instead therefore of admitting various descriptions of copulæ (other than the affirmative and negative), in order to adapt

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Logic to ordinary language, it seems simpler, as well as more scientific, to insist on the uniform character of the copula, and to represent propositions like the foregoing as predicating our degree of assent to or dissent from the sentence in question. Thus, after asking myself the question 'Is this the man I saw yesterday?' I may either answer simply 'This is the man I saw yesterday,' or I may describe the degree of my assent by stating 'That this is the man I saw yesterday is certain, probable, possible,' &c. In fact, such propositions seem to be the result of an act of reflexion on the degree of our own conviction.

I shall therefore regard the form A is or is not B as the ultimate and uniform logical analysis of all propositions, though I shall occasionally, for the sake of brevity, avail myself of the forms sanctioned by popular language.

Note.—As regards the expression of time in the copula, the student will find the opposite opinion to that taken in the text adopted by Mr. Mill, Logic, vol. i. ch. iv. § 2. In support of my view, he may refer to Dr. Mansel's Prolegomena Logica, pp. 63, 64. On the question of expressing in the copula the degrees of assurance with which a proposition is entertained ('certainly,' 'probably,' &c.), see Sir W. Hamilton's Discussions, pp. 145-7, and, for a more qualified view than that taken either by Sir W. Hamilton or myself, Dr. Mansel's Prolegomena Logica, note G.

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CHAPTER III.

Division of Propositions according to their Quantity and Quality.

WE have already seen that propositions are either affirmative or negative, according as the copula used is of the form 'is' or 'is not.' This is called a division of propositions according to their Quality.

They are further divided, according to their Quantity, into Universal and Particular. For, in affirming or denying a predicate of a subject, it is obvious that I may either affirm or deny the predicate of all the individuals denoted by the subject, or of part only. Thus in affirming mortality of man, I may say 'All men are mortal,' or 'Some men are mortal'; in denying wisdom of man, I may deny it of all men or only of some men, i.e. I may say 'No men are wise,' or 'Some men are not wise.' When the predicate is affirmed or denied of all the individuals denoted by the subject, the proposition is called an Universal Proposition; when of part only, a Particular Proposition. A Singular Proposition, i.e. a proposition of which the subject is a singular term, ranks as an Universal, because the predicate is affirmed or denied of everything (i.e. in this

case, the one thing) denoted by the subject. The same remark holds good of a proposition in which the subject is a collective term. An attributive, as we have already seen, cannot, by itself, be used as the subject of a proposition. Abstract terms which have come to be used as common terms, and admit of plurals, as figure, triangle, virtue, pleasure, &c., have a denotative power, and may, like common terms, form the subjects of either universal or particular propositions. But those abstract terms, like humanity, wisdom, &c., which retain their original characteristic of being connotative only, and admit of no plurals, simply express an attribute or group of attributes with which, as a whole, it is asserted or denied that the predicate is compatible; consequently, a proposition, of which such a term is the subject, ranks as an universal.

Thus such propositions as 'Ambition is aggressive,' 'Wisdom is a virtue,' 'The fourteenth legion is disbanded,' 'Socrates is an Athenian citizen,' are, on the very face of them, universals. But propositions in which the subject is a common term or an abstract term used as a common term, must be quantified; that is, we must attach to the subject either an universal or a particular designation. It is not sufficient to say, 'triangles are figures,' 'horses are black'; we must state whether we mean that 'all triangles' or 'some triangles' are 'figures,' whether we mean that 'all horses' or 'some horses' are black. 'Indefinite' or 'indesignate' propositions, as they are called, i.e. propositions in which the subject, being

a common term, is not quantified, are inadmissible in Logic.

By combining the division of propositions into universal and particular with that into affirmative and negative we obtain four forms, viz.—

Universal Affirmative. All X is Y. (A)

Universal Negative. No X is Y. (E)

Particular Affirmative. Some X is Y. (I)

Particular Negative. Some X is not Y. (O)

I shall in future designate these forms of proposition respectively as A, E, I, O'.

Note.—Sir W. Hamilton², followed by several other logicians, maintains that in thought the predicate is always quantified as well as the subject. He proposes to reform the logical theory of the proposition accord-

It sometimes requires a little ingenuity to state a given proposition in one of the above forms. Thus the propositions 'None but the brave deserve the fair,' 'The wise alone are good,' 'Not every historian is worthy of credit,' 'All his acts are not defensible,' when stated in strictly logical form, become respectively, No not-brave (or None who are not brave) are deserving of the fair, No not-wise (or None who are not wise) are good, Some historians are not worthy of credit, Some of his acts are not defensible. The simplest equivalents of the two former propositions are, All who deserve the fair are brave, All good men are wise; but these are arrived at by permutation and conversion, two forms of inference which have not yet been explained.

² Sir William Hamllton's theory was anticipated in a work now little read, but full of original suggestions on logical questions, Mr. George Bentham's Outline of a New System of Logic, published in 1827.

ingly, and in lieu of the four ordinary forms of proposition substitutes the following:---

All X is all Y.
All X is some Y.
All X is not any Y.'
All X is not some Y.'
Some X is all Y.
Some X is some Y.
Some X is not any Y.
Some X is not any Y.

This scheme, if adopted, would, as Sir W. Hamilton shews, reduce all conversion to simple conversion, render nugatory any discussion as to the distribution of terms, and considerably simplify the forms of syllogism: see the Appendices to Sir W. Hamilton's Discussions, and to his Lectures on Logic. Amongst other criticisms may be seen Mr. Mill's in his Examination of Hamilton's Philosophy, ch. xxii. It would of course be undesirable to enter here into any discussion as to the merits of Sir W. Hamilton's theory, but, as reasons for not adopting the quantification of the predicate in the present work, it may be sufficient to state (1) that, as to utility, the trouble entailed by quantifying the predicate in every proposition would probably far exceed that saved by simplifying the forms of Conversion and Syllogism; (2) that the forms of expression given above are not merely unusual, but are such as we never do use; whereas, though the analysis of our thoughts frequently leads to

forms of expression which are unusual, this would, if admitted, be the only case in which it led to forms which are never used at all; (3) that some of the above propositions really contain in a compressed form two ordinary propositions, as e.g. 'All A is all B,' contains the two ordinary propositions 'All A is B' and 'All B is A,' the proposition 'Some A is all B' contains the two ordinary propositions 'Some A is B' and 'All B is A,' whereas it is the object of Logic not to state our thoughts in a condensed form but to analyse them into their simplest elements.



CHAPTER IV.

Distribution of Terms.

A TERM is said to be distributed, when it is employed in its entire extent, i.e. when it applies to all the individuals denoted by the name. Thus, when we say, 'all men,' 'no men,' 'man' is distributed; when we say 'some men,' it is undistributed. This phraseology of course applies directly only to common terms; but singular and collective terms, as has already been explained, are always taken in an universal acceptation, or, in other words, are always distributed. The same is true of those abstract terms which have not come to be used as common terms, because they, as it were, personify the attribute or group of attributes which they express; so far as regards distribution, they are, in fact, virtually singular terms. In such propositions as, 'This is wisdom,' 'Wisdom is justified of her children,' 'Warmth is essential to growth,' 'Knowledge is power,' it is obvious that the abstract terms are distributed precisely as if they were singular terms, and that, for all logical purposes, these propositions rank as universal. Attributives, i.e. adjectives and participles, have no meaning except in connexion with a substantive. They must either be prefixed to a substantive or predicated of it: we cannot say 'human' alone; we must either speak of 'human being,' 'human nature,' &c., or say, 'So and so is human.' Consequently the distribution or non-distribution of an attributive, as 'human,' 'red,' &c., follows that of the corresponding common term, 'human being,' 'red thing,' &c.

Hence we perceive that a singular, collective, or abstract term is distributed wherever it may occur in a proposition. We have therefore only to enquire as to the distribution of common terms and attributives. With regard to these, the two following rules may be laid down.

- r. All universal propositions distribute their subject, whereas particular propositions do not. This rule is obvious. The very word 'all' or 'no' shews that the subject is distributed, whereas the word 'some' shews that it is undistributed.
- 2. All negative propositions distribute their predicate, whereas affirmative propositions do not. For in every negative proposition we necessarily exclude from the subject every individual denoted by the predicate, but in an affirmative proposition we do not necessarily include in the subject every individual denoted by the predicate. Thus, if I say, 'No crows are yellow,' 'Some cherries are not red,' I exclude from the group 'crows' every individual object denoted by the term 'yellow things,' and from the group 'some cherries' every individual object denoted by the term 'red things'.' But if I say, 'All

¹ Here it will be noticed that the terms 'yellow' and 'red,' though not in themselves denotative, suggest the corresponding common terms, 'yellow things' and 'red things,' and thus, through the medium of the common terms, become denotative.

men are animals,' or 'Some Englishmen are poets,' I do not include in the group 'men' all animals, nor in the group 'Englishmen' all poets. It may of course happen that the predicate in an A or I proposition is co-extensive with the subject, as in the propositions 'All men are rational animals,' 'Some men are poets,' but this fact is accidental, and is not implied in the form of the proposition.

From these two rules we infer that, in the case of common terms and attributives, an A proposition distributes its subject only, E both its subject and predicate, I neither, O its predicate only. If a term be singular, collective, or abstract, it is invariably distributed.



CHAPTER V.

Relation of the Predicate to the Subject of a Proposition (Heads of Predicables.)

N.B. For this Chapter, in the case of beginners, may be substituted Appendix, p. 160. See Preface, p. x.

FROM what has already been said, it is plain that a singular, collective, or abstract term, inasmuch as it is always distributed, cannot form the subject of an I or O proposition: on a little reflexion it will also be plain that the predicate of a proposition cannot be singular, collective, or abstract, unless the subject be the same. I have already noticed that an attributive can never form the subject of any proposition. These considerations will be found to simplify the problem before us.

This problem may be stated thus: How may the predicates of propositions be classified in relation to their subjects? or What are the heads of predicables (prædicabilia, things or words that may be predicated)? I shall discuss the four forms of proposition in order.

To commence with A, and with the special case where both subject and predicate are common terms, or abstract

terms which are used as common terms 1. 2 Here the predicate may either be (1) equivalent in extent to the subject, or (2) greater; it cannot be less. We can say, for instance, 'All men are animals,' or 'All men are rational animals,' but we cannot say 'All animals are men.' Now, if the predicate be (1) equivalent in extent to the subject, it is either (a) a Synonym, as 'A wold is a down'; or (\$) a Definition, as 'A plane triangle is a three-sided rectilineal figure'; or (y) a combination of a genus (a term which will be explained immediately) with some attribute which is peculiar to the term in question (called by Aristotle an 7000 or 'peculiarity'), as 'A plane triangle is a rectilineal figure the sum of whose angles is equal to two right angles.' A synonym, it need hardly be stated, is an equivalent word, and a definition is an exposition of the connotation of a term. Now it will be observed that the definition of a plane triangle consists of two parts, one in which it is designated as a 'rectilineal figure'a wider group, which includes not only triangles but other rectilineal figures-and the other part an attribu-

It may perhaps assist the student in following what, to be exhaustive, must necessarily be a tedious disquisition, if I afford him some the to the order in which the cases will be discussed:—

In the A proposition, (I) if the predicate be a common term, the subject may be (a) a common, (β) a singular or collective term; (2) if the predicate be a singular or collective term, the subject must be the same; (3) if the predicate be an abstract term, the subject must be the same; and (4) if the predicate be an attributive, the subject may be (a) a common, (β) a singular or collective, (γ) an abstract term. The discussion of the cases in I, E, and O is much less elaborate.

tive, 'three-sided,' which distinguishes triangles from all other groups contained in the wider group to which triangle has been referred. The former part of the definition is called the genus, and with reference to it 'plane triangles,' the group of figures defined, are called a species; the latter part of the definition, 'three-sided,' which distinguishes triangles from squares, pentagons, and other rectilineal figures which are designated by the wider term, is called the differentia or 'differencing' attribute. It is obvious that there might be more than one of these, and then they would be called the differentia. With reference to the third case, 'A plane triangle is a rectilineal figure the sum of whose angles is equal to two right angles,' 'rectilineal figure' is, as before, to be regarded as a genus, but the attributive 'having the sum of its angles equal to two right angles' cannot be regarded as a differentia, for it is not connoted by the term 'plane triangle,' but requires to be proved of it; at the same time it is an attribute peculiar to the plane triangle, and hence, retaining the Aristotelian term, we may call it an idoor. Lastly, there remains (2) the case in which the predicate is of greater extent than the subject, both being common terms, as in the propositions 'All men are animals,' 'All triangles are figures.' Here the subject denotes a smaller group of individuals included under the wider group designated by the predicate; that is, according to the nomenclature already explained, the predicate is related to the subject as genus to species. This relation is often spoken of as that of the containing to the contained.

When the predicate is a common term, and the subject a singular or collective term, as in the instances 'Socrates is a philosopher,' 'Socrates is an Athenian citizen,' 'The House of Commons is a branch of the legislature,' the predicate is related to the subject as a group of individuals to an individual, i. e. as a species to an individual, for the word 'genus' is only applicable to a group containing other groups. The same account must be given of those propositions in which the predicate is an abstract term employed as a common term, and the subject is an abstract term employed strictly as such, as e. g. 'Temperance is a virtue,' 'Heat is a mode of motion.'

When the predicate is a singular or collective term, the subject must, as we have already seen, be a similar term. Moreover the predicate in these propositions is always distributed as well as the subject, and consequently the two terms are co-extensive. But, inasmuch as singular and collective terms have, at least directly, no connotation, the predicate cannot stand to the subject in the relation of a definition, or of an Thor 2 (i.e. an attribute peculiar to the subject) combined with a genus. It can only be (1) a synonym, or (2) a singular or collective term designating the individual or the collective group. As instances of these propositions we may take the following: 'Cephas is Peter,' 'Socrates is the son of Sophroniscus,' This is the man whom I saw yesterday, and whom I told

² The English word 'characteristic' might perhaps be employed as the equivalent of the Greek Thor.

to come to me,' 'The fourteenth legion is the legion quartered in Britain.' When the predicate is not a synonym, it may perhaps be called a Designation.

When the predicate is an abstract term, the subject must be abstract as well, and, as in the case of singular and collective terms, the subject and predicate are both distributed, and consequently are of equal extent. We may take as instances of the various forms which propositions of this kind assume, 'Charity is love,' 'Honesty is the best policy,' 'Definition is the exposition of the connotation of a term.' Now in the first example 'love' is intended as a synonym of 'charity,' in the second 'the best policy' is predicated of 'honesty' as distinguishing it from all other courses of conduct; the third example is an ordinary case of a definition. The case of two abstract terms may therefore be regarded as identical, so far as concerns the relation of the predicate to the subject, with that of two common terms which are co-extensive.

Lastly, there remains the case in which the predicate is an attributive. Supposing the subject to be a common term, the predicate may, as we have seen, be (1) a differentia, as in the proposition 'All triangles are three-sided,' or (2) an the proposition 'All plane triangles have the sum of their angles equal to two right angles.' Or, though neither a differentia nor an theorem, it may be (3) what, along with the theorem, modern logicians would call a Property, viz. an attribute which, though not connected by the subject, nor even peculiar to it, follows from something connoted by the subject, either (a) as effect from cause or (b) as

conclusion from premiss*. An instance of (a) a property which follows from the connotation of the subject by demonstration would be given in the proposition 'A parallelogram has its opposite sides equal,' or in the proposition 'A circle is a figure the ratio of whose circumference to its diameter is approximately 3.14159: 1.' As instances of propositions in which the predicate expresses (3) a property following from the connotation of the subject by causation, we may take 'Men are capable of combining for purposes of joint action,' 'Water communicates pressure equally in all directions.' The first property follows from rationality, or that combined with the power of articulate speech, which seems to be connoted by the very word 'man'; the second property follows from the fluidity of water. The last example of a property following by way of demonstration and the first of a property following by way of causation are that in the sense of Aristotle, as well as propria in the sense of the later logicians. There is (4) one other case, that in which the attributive, though neither connoted by the subject nor following from anything connoted by the subject, is predicable of everything denoted by it. Such an attributive is called an Inseparable Accident, and the common instance given by logicians is the proposition 'All crows are black.' If the blackness of crows could be connected by way of causation with any

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The student must bear in mind that every there is a Property, though every Property is not an theor. The definition given above applies only to those properties which are not the. The formal definition of Property will be found on p. 45.

attribute connoted by the name, it would be regarded as a property; if, on the other hand, a crow could be found which was not black, blackness would be degraded to the rank of a Separable Accident, a term which will be explained below.

We have thus far considered attributives as predicates in the special case where the subject is a common term. Where the subject is a singular or collective term, and consequently has no direct connotation, the attributive forming the predicate can only be an inseparable accident *. I may indeed say 'Socrates is rational,' but I predicate rationality of him as man, not as Socrates. Where the subject is an abstract term, the attributive which forms the predicate may be a differentia or a property, but cannot be an inseparable accident, for an abstract term denotes no individuals.

In the I proposition we are not concerned with singular, collective, or abstract terms. If the predicate be (1) a common term, it may be related to the common term in the

* Sometimes a distinction is drawn between the separable and inseparable accidents of an individual. An inseparable accident of an individual is regarded as one which is predicable of it at all times, a separable accident as predicable only at certain times. Thus in the propositions, 'John is tall,' 'John is sitting down,' 'tall' is regarded as an inseparable, 'sitting down' as a separable accident. But the expressions separable and inseparable accident are here employed in an entirely different sense from that in which they have been employed above, and it seems preferable to regard all attributes which are predicated of individuals, in their individual character, as inseparable accidents—inseparable, that is to say, from the individual under the circumstances in which it is at present placed.

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subject either (a) as species to genus, or (β) as species to species, as e.g. 'Some men are poets,' or 'Some poets are philosophers.' The latter relation is that of two groups, which have some members in common—overlapping species, as they have been called. The relation may also be (γ) that of genus to species, as 'Some men are animals,' 'Some poets are men,' but this form of proposition is practically useless, as it stops at a particular assertion when an universal assertion is legitimate. If the predicate be (2) an attributive, it must, unless the proposition state less than the truth, be a Separable Accident, i.e. an attribute which is true only of some of the individuals denoted by the subject, as e.g. 'Some men are black,' 'Some triangles are equilateral.'

With regard to negative propositions, it is not necessary to speak at any length. The negation of an attributive in an E proposition implies that it is neither a differentia, property, nor accident; in an O proposition that it is neither a differentia, property, nor inseparable accident, though it may be a separable accident. All that has been said of the relations of singular, collective, and abstract terms, as subjects, either to similar terms or to common terms and attributives, as predicates, in the case of an A proposition, holds good also, mutatis mutandis, of similar relations in E. It may perhaps be as well to give a few instances of such propositions: 'Socrates is not a poet,' 'Socrates is not the man I saw yesterday,' 'The fourteenth legion is not engaged in the battle,' 'Charity is not obtru-

sive,' 'Ambition is not a virtue.' Where a common term is denied of a singular or collective term, it stands to the subject in the relation of species to individual. Where a common term is denied of a common term, there is nothing to prevent the terms being extremely remote from each other and hardly admitting of comparison; but here the most appropriate relation is-in an E proposition, that of co-ordinate though exclusive species, i.e. of species which having many characteristics in common, and both falling immediately under the same genus, still denote no individuals in common,-in an O proposition, that of overlapping species. Thus we should be far more likely to derive information from such propositions as these, 'No sandstone is limestone,' 'Some astronomers are not mathematicians,' than from such propositions as these, 'No men are trees,' 'Some stones are not vipers.'

From what has been said we have derived the following names for the predicate in its relation to the subject:

(1) synonym, (2) definition, (3) designation, (4) genus, (5) species, (6) differentia, (7) theor, (8) property (not being an theor), (9) inseparable accident, (10) separable accident. Of these, logicians have neglected synonym and designation, the former probably on account of its slight importance, the latter perhaps because it applies only to singular and collective terms. Definition is analysed into genus and differentia; no distinction is drawn by later logicians between the and those properties which are not peculiar to the subject, both being alike designated by the word 'property';

and the word 'accident' serves alike for separable and inseparable accident. Genus, difference, species, property, and accident, are known as the five heads of predicables.

These may be briefly defined as follows:--

- A Genus is a common term expressive of a wider group of individuals including narrower groups.
- A Species, in reference to a genus, is a common term expressive of a narrower group included in the genus; in reference to an individual, of a group including it.
- A Differentia is an attributive which expresses part of the connotation of some common term, and which distinguishes that term from all other species which fall under the same genus.
- A Property is an attributive which does not express any part of the connotation of the common term, but which follows from some part of the connotation of the term, either as an effect from a cause, or as a conclusion from premisses.
- An Accident is an attributive which may be predicated of the whole or part of the individuals denoted by a common term, or which may be predicated of an individual, but which is neither connoted by the common term nor to be inferred from anything which is connoted thereby 5.
- In the above definitions, wherever the expression 'common term' occurs, it must be understood as including those abstract terms which have come to be employed as common terms.

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Note 1.—Contrary to the practice of most logicians, I have discussed the heads of predicables under the second part of Logic. In taking this course, I have attempted to restore to them their original significance in the works of Aristotle, as a classification of the predicates in their relation to the subjects of propositions. It is perhaps needless to add, that I have not followed implicitly the Aristotelian account, or in all cases adopted the Aristotelian phraseology. By Porphyry, the schoolmen, and their successors of the seventeenth and eighteenth centuries, the heads of predicables were regarded as a classification of universals in their relations to one another, rather than with reference to their place in a proposition, and consequently, from the time that Logic was divided into parts, were discussed under the first part. Definition and division, as dependent on a knowledge of genus, species, and differentia, are also here treated under the second part of Logic, though they are ordinarily discussed under the first.

Note 2.—On the vexed and subtle question of the Import of Propositions, or, as it is sometimes called, the Theory of Predication, the student may be referred to Hobbes' Computation or Logic, ch. iii., Mr. Mill's Logic, Bk. I. ch. v., Dr. Mansel's Prolegomena Logica, ch. ii., Sir W. Hamilton's Lectures on Logic, Lects. viii. and xiii., and Mr. Mill's Examination of Sir W. Hamilton's Philosophy, ch. xviii. The view I should adopt may be briefly stated as follows: wherever the predicate is a singular or collective term, or, though a common or

abstract term, a synonym of the subject, the theory of Hobbes, that the predicate is a name of the same things of which the subject is a name, furnishes a sufficient account; in all other cases, Hobbes' theory is true, though insufficient, for, where the predicate is an attributive or an abstract term (not being a synonym), the predicate also asserts or denies certain attributes of the subject, and where it is a common term (not being a synonym), not only are certain attributes asserted or denied of the subject, but the latter is referred to or excluded from the group of individuals denoted by the predicate. Thus, in the proposition 'Socrates is the son of Sophroniscus,' the predicate may be regarded as simply another name for the subject; but when we say 'Socrates is human,' we imply more than this, namely, that certain attributes connoted by the word 'human' may be affirmed of Socrates. Further, when we say 'Socrates is a man,' we not only assign another name to the subject, and predicate of it certain attributes, but we also include it in a certain group. This peculiarity follows from the double signification of common terms, by which they both denote a group of individuals and connote a group of attributes, or, in other words, simultaneously suggest to the mind a group of individual objects and a bundle of attributes characteristic of that group. From what has been said it will be seen that I do not agree with Mr. Mill in regarding all predication, other than that of a singular or collective term, as a predication merely of attributes.

CHAPTER VI.

On Verbal and Real Propositions.

AFFIRMATIVE propositions in which the subject is a common or abstract term may be divided into Verbal and Real. A verbal proposition expresses merely the connotation or part of the connotation of the term, a real proposition expresses either solely, or in conjunction with part of the connotation of the term, properties, accidents, or both. Thus a verbal proposition simply states what might be gathered from a due consideration of the name, as 'All men are rational,' 'All triangles are three-sided'; whereas a real proposition imparts knowledge which could not be gathered from the name alone, as 'All triangles have the sum of their angles equal to two right angles,' 'Some men are black.' It is plain that all particular affirmative propositions are real.

Note.—The distinction between verbal and real propositions is otherwise expressed by that between Analytical and Synthetical judgments (Kant), Explicative and Ampliative judgments (Sir W. Hamilton and Abp. Thomson), Essential and Accidental propositions (the schoolmen). Tautologous propositions (All A is A), and propositions in which the predicate is a synonym of the subject (as e.g. 'Charity is love'), should be referred to the head of verbal propositions.

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CHAPTER VII.

On Definitions.

A DEFINITION is an exposition of the connotation of a term. It may always be represented in the form of a proposition, of which the term defined forms the subject and the exposition the predicate.

As a definition expounds or enumerates the attributes which a term implies, it is plain that singular and collective terms, inasmuch as they do not in themselves connote any attributes, are incapable of definition. They may, however, be described by means of the various common terms which are predicable of them, as well as by designations which are peculiar to themselves. Thus I may say 'John is a tall man of fair complexion, is by profession a London solicitor, and occupies such and such a house in Bedford-row.' This may be called a Description of a Singular or Collective Term, in order to distinguish it from the Description of a common term, which is noticed below, and which I shall call simply Description. Besides singular and collective terms, a term expressing a single attribute, which is incapable of analysis into other attributes, is incapable of definition. Thus it has been maintained that it is useless to attempt to define such terms as pleasure, pain, colour, thing, attribute, &c.

¹ It is indifferent whether we speak of the entire proposition as the definition, or merely the exposition which forms the predicate; similarly in the case of a description.

In defining a term, it would of course be impossible, in every case, to state the definition in terms' expressive of attributes which are themselves incapable of analysis, even if we were agreed as to what are terms of this character. The terms employed in the definition may therefore express groups of attributes, provided that, when taken together, they exhaust the connotation of the term defined. Thus each of the terms 'under one supreme head' and 'political government' expresses a large group of attributes, but if, when taken together, they exhaust the connotation of the word 'monarchy,' the definition may be accepted as legitimate.

In seeking to define a term, I invariably contrast it with some other term; often, when I imagine it to be difficult to exhaust the connotation, with a variety of other terms, from which I seek to distinguish it. Thus in seeking to define 'monarchy,' I contrast it with other forms of government; in seeking to define 'plane triangle,' I contrast it not only with other rectilineal figures but with spherical triangles; in seeking to define 'light,' I contrast it with heat, sound, electricity, and other impalpable powers of nature. Now that portion of the definition which is common to the term defined and to the other terms with which it has been compared is called the genus, the term defined standing to it in the relation of a species, as has already been explained; that portion which distinguishes the term defined from the terms with which it has been compared is called the differentia, or sometimes, when there is more than one distinguishing

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attribute, the differentiæ³. Thus, if we were distinguishing rectilineal triangle from spherical triangle, 'three-sided figure' would be the genus; if from other rectilineal figures, the genus would be 'rectilineal figure'; if from both spherical triangles and other rectilineal figures, the genus would be simply 'figure.' It will be observed that the genus is always expressed in the form of a common term, or of an abstract term which is used as a common term, and that it may be qualified by an attributive. This is the case even in defining abstract terms, as e.g. in the definitions, 'Justice is a virtue which respects our relations to other men in society,' 'Temperance is a virtue which respects the control of our own desires,' the genus³ is 'a virtue,' an abstract term which has come to be used as a common term.

A Definition being an exposition of the meaning of a term, it is obvious that all definitions must be limited by the state of our knowledge at the time when we frame them. But some terms have been expressly framed or have been appropriated to express a small number of attributes. Such terms are monarchy, anarchy,

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^{*} Some logicians simply use the word 'differentia' for the purpose of expressing the distinguishing attributes, whether one or many; others, as Aristotle, would in the latter case speak of the 'differentiae.'

Whenever abstract terms are defined or divided, or occur as portions of definitions or divisions, they seem invariably to be treated as if they were common terms, and hence in the definitions of abstract terms, as in other definitions, the term defined may be regarded as a species; for the same reason, when an abstract term is divided, its relation to the dividing members may be described as that of genus to species.

triangle, square, school, monastery, &c. Our accepted definitions of these terms we may be quite sure we shall not be compelled to alter with advancing knowledge, provided at least that they continue to denote the same objects. But however full and adequate to our present state of knowledge our definitions of man, animal, vegetable, light, heat, &c., might be at the present time, they might, two hundred years hence, become most inadequate and incomplete, if not incorrect, even although the terms continued to denote the same objects or sensations. We might, for instance, discover the mode of transmission of light, or that the animal world was not separated from the vegetable by the same characteristics by which we now conceive it to be, and henceforth these discoveries would become part of the connotation of the words, or would materially alter the connotation. In the greater number of cases, therefore, we must be content to regard our definitions as provisional 4.

But not only must we in most cases be content with provisional definitions; we must often be content with definitions which, measured even by our present state of knowledge, are incomplete. It would often be most inconvenient, when it is required simply to distinguish between two terms, to give the full connotation of each.

It would be a service to logicians if there were recognised names by which to distinguish between these two different classes of definitions, viz. the definitions of terms whose connotation is limited, and whose definitions are therefore final, and the definitions of terms whose connotation is unlimited, and whose definitions are therefore provisional.

In such cases, therefore, it is regarded as practically sufficient, if we refer the terms contrasted to their common genus, and specify a sufficient number of attributes to distinguish each from the other. Thus in the oftenquoted example of definition, 'Man is a rational animal,' it would be absurd to suppose that 'rational' and 'animal' exhaust the connotation of 'man,' but the word 'rational' is sufficient, for popular purposes, roughly to distinguish the human race from the lower animals with which it is generally contrasted. When these incomplete definitions, as they are called (i.e. definitions which do not give the complete connotation of a term), are once admitted, it is obvious that our definitions of the same term may vary indefinitely according to the particular point of view from' which we make them, or the science which we happen to be pursuing at the time.

An exposition of a term which gives no part of its connotation, but in lieu of it an enumeration of properties and accidents, is called a *Description*. Thus 'Man is a featherless biped' would be regarded as a description, not as a definition of man. But the term 'description' is also extended to those cases in which properties and accidents are combined with a portion of the connotation, the latter being usually stated as the genus. Thus we might describe horse as an animal

⁶ Here the attributive 'biped,' being used as a quasi-genus (i.e. a property or accident which, for a special purpose, is employed as a genus), is stated in the form of a substantive. This particular example of a description is, of course, absurd, and simply serves the purpose of roughly distinguishing men from birds.

which is domesticated, which has a mane and a tail, which has a high value attached to it, which is to be found in Arabia and Europe, &c., &c.; or we may take as an instance of a description Cuvier's definition of man, as a mammiferous animal having two hands. The latter instance is sufficient to shew that a description may often serve the purpose of distinguishing the term described from all other terms, and may therefore be quite adequate to fulfil the purposes of a definition for any special object.

. From what has been said it will be seen that definitions and descriptions may be classified as follows:—

- (1) A definition complete and final.
- (2) Complete (so far as we know), but provisional.
- (3) Incomplete, but sufficient to distinguish the term defined from all other terms.
- (4) Incomplete, but sufficient to distinguish the term defined for the special purpose in hand.
- (5) A description only, but sufficient to distinguish the term described from all other terms.
- (6) A description only, but sufficient to distinguish the term described for the special purpose in hand.

Any pretended definition or description which does not fulfil one of these conditions must be rejected as having no value whatever. In testing a definition or description, we should at once reject it if it were applicable to any other term, unless we were expressly told that it was used only for the purposes of a particular science, and we found on investigation that it was distinguishable

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from all other terms employed in that science. Thus, in a discussion on politics, it would be sufficient to define monarchy as the supreme government of one man, but, if speaking generally, I must add 'in a state,' for one man may be supreme governor in his family, in a school, in a religious association, &c.

The rules for a legitimate definition must depend on the kind of definition which we purpose or are compelled to employ. The following rules are common to the three first kinds of definition enumerated above:—

- The definition must be convertible with the term defined, i.e. it must apply to every object denoted by the term defined, and to no other objects.
- 2. The definition must consist of one common term or abstract term employed as a common term (the genus), and of one or more attributives (the differentia or differentiæ).
- 3. Each of these terms, constituting the definition, must connote less than the term defined; otherwise, they afford no explication of it.
- 4. Each of these terms must have a connotation distinct from that of the others; otherwise, the definition will be redundant.

Note 1.—It may have occurred to the student to ask 'How are we to distinguish those attributes which form part of the connotation of a term, from the attributes which are inferred from them?' This is a question

which in many individual cases it would be extremely difficult to answer, and there might be great differences of opinion as to what attributes were to be regarded as differentiæ, and what as properties. It is in fact the same question as 'What are primary, and what are derived qualities?' The only general answer that can be given is that, wherever one attribute or quality can be inferred from another, it is to be regarded as a derived quality or a logical property, and that all those attributes that cannot be so derived are to be regarded provisionally as an assemblage of primary qualities or, in logical language, the connotation of the term. As our knowledge advances, it is of course possible that many of these primary qualities may be resolved into secondary, i.e. many of the supposed differentize may be resolved into properties.

Note 2.—The scholastic logicians distinguished between real and nominal definitions, meaning by a real definition the explication of the nature of a thing, by a nominal definition the explication of the meaning of a term. The first would give an answer to such a question as 'What is man?' the second to such a question as 'What do we mean by the term man?' As the meaning we attach to a term ought exactly to correspond with our knowledge of the primary or underived attributes of the thing, this distinction is now usually regarded as nugatory. Mr. Mill has however revived the expressions 'real' and 'nominal' definition to mark a distinction between those definitions which assume or imply the existence of the object defined

and those which carry with them no such assumption or implication. 'All definitions,' he says, 'are of names and of names only; but, in some definitions, it is clearly apparent that nothing is intended except to explain the meaning of the word; while in others, besides explaining the meaning of the word, it is intended to be implied that there exists a thing corresponding to the word.' Thus the definition of a 'horse' or a 'triangle' would be called a real definition, that of a 'centaur' a nominal definition. See Mill's Logic, Bk. I. ch. viii. s. 6.

Note 3.—Sometimes we may explain a term by a synonym, an etymology, or a translation, which may accidentally be better known to the hearer or reader than the term so explained. These explanations cannot be accepted as definitions in our sense of the word, inasmuch as they do not analyse the connotation of the term; but they would have been regarded as instances of nominal definitions by the older logicians.



CHAPTER VIII.

On Divisions and Classifications.

A DIVISION is an exposition of the denotation of a term. It may always be represented in the form of a proposition, of which the term divided forms the subject and the exposition the predicate.

In divisions the denotation of a term is expounded by enumerating, not the individuals (which would in most cases be impossible), but the smaller groups which the term denotes. The terms denoting these smaller groups are called the *dividing members* (membra dividentia) in contradistinction to the divided term (called by the older logicians the 'divided whole,' totum divisum).

It is plain that common terms, or abstract terms which are employed as common terms, are alone capable of being divided. Abstract terms and attributives have, in themselves, no denotation, while singular and collective terms are incapable of being divided into smaller groups. A collective term may however easily be transformed into a common term, and so rendered capable of being divided; thus 'the fourteenth regiment' may become 'soldiers of the fourteenth regiment,' and in this form may be divided into officers and privates, or other groups. The same remark holds good of abstract terms and attributives.

It may be laid down as a test of a logical division that the term divided must be predicable of each dividing member. Thus 'figure' is predicable alike of triangle, square, &c., 'man,' of white man and black man. In this manner it is distinguished from partition of a physical whole into its parts, as of 'man' into head, arms, legs, &c., or of the 'world' into Europe, Asia, Africa, and America. But this test, though sufficient to distinguish a division from a partition, is not sufficient to distinguish it from two other forms of propositions, which nevertheless we must beware of confounding with it. These are an enumeration of individuals, and a distinction of an equivocal term according to its various meanings, as e.g. of 'humanity,' according as it means human nature, the human race collectively, the virtue of being humane, or the study of polite letters. In a distinction the same definition is not predicable of each of the terms distinguished, but in a division the same definition is predicable of each dividing member.

In dividing a term into terms expressive of smaller groups (or, as they are frequently called, subject classes), I invariably try to think of some attribute which is predicable of certain members of the group, but not of others. This attribute suggests what is called the fundamentum divisionis or principle of division (i. e. some character of the group, which is a source of differences amongst its members). Thus, if asked to divide 'triangles,' it may first occur to me that some triangles have equal sides and others not; in this case the

property of a triangle that the lengths of its sides may be variously related, or, in other words, the relation of the sides, becomes the fundamentum divisionis, and I divide triangles into equilateral, isosceles, and scalene. Or it may first occur to me that some triangles are rightangled, and others not; in this case the measure of the angles becomes the fundamentum divisionis, and I divide triangles into right-angled, obtuse-angled, and acuteangled. Or, to take one more instance, if asked to divide 'governments,' I may reflect that in some governments the sovereignty is divided, in others it is placed entirely in the hands of one person or order, and I may divide 'governments' accordingly into pure and mixed, proceeding to divide pure governments, according to the number of persons in whose hands the sovereignty is placed, into monarchies, oligarchies, and democracies. Any division in which two or more fundamenta divisionis are confounded 1, or cut across one another, is called a crossdivision and is logically inadmissible. Thus a division of triangles into isosceles, scalene, and right-angled, or of governments into monarchies, free governments, and mixed governments, or of men into Frenchmen, Asiatics, the unproductive classes, and barbarians, would be a cross-division. In the last example there is a confusion of no less than four fundamenta divisionis.

It is maintained by many logicians, and with justice,

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¹ But, as in Natural Classifications (see p. 62 below), we may employ any number of fundamenta divisionis, provided that their results coincide.

that in every legitimate division (or, at least, in every division which we have sufficient reason for knowing to be legitimate), the process by which the division is arrived at, if strictly analysed, may be described as follows. Taking, for instance, 'triangles,' we reflect, say, that some are equilateral; we then divide triangles into equilateral and those which are not equilateral, and again, still thinking of equality of sides, those which are not equilateral into those which have two sides equal (isosceles), and those which have none (scalene). Similarly, taking 'men,' and thinking of race as our fundamentum divisionis, we divide mankind into Aryans and those who are not Aryans, the latter into Semites and those who are not, the latter into Turanians and those who are not, and so on, till our division is complete. This process, when formally drawn out, is called Division by Dichotomy, and the rule by which it proceeds is in each division to take two terms which admit no medium between them. Thus such pairs of terms as productive and unproductive, fallible and infallible, white and not white, would answer the purpose.

The divided term stands of course to the dividing members as a genus to species. We can also gather the differentia from the fundamentum divisionis. Thus, in dividing a term, we virtually define the subject terms. A pure government, for instance, may be defined as a government in which the sovereignty is undivided, and a mixed government as a government in which the sovereignty is divided. In defining also we virtually

divide. Thus the definition of man as a rational animal implies a division of animals into men and brutes, and the definition of a plane triangle as a three-sided rectilineal figure implies a division of rectilineal figures into three-sided and not three-sided (i. c. quadrilaterals and polygons).

The rules for a legitimate division may, in accordance with what has already been said, be stated as follows:—

- Each dividing member must be a common term, or an abstract term which is used as a common term.
- 2. The divided term must be predicable of each dividing member.
- 3. The division must be exhaustive, i.e. the dividing members, when taken together, must be equal in extent to the term divided.
- 4. The dividing members must be mutually exclusive, i. e. no subordinate species must be included under more than one of them; otherwise we have a cross-division.

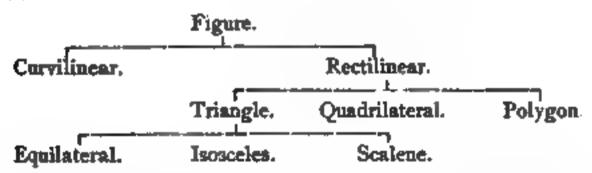
The surest mode of satisfying the last condition is to employ only one fundamentum divisionis, and in artificial classifications this method is adopted, but it is the distinctive characteristic of natural classifications, which alone are adequate to many of the purposes of science, to employ simultaneously a number of principles of division. (See *Inductive Logic*, ch. ii. § 2 (1), 4th ed. pp. 50-74.) In the latter case, therefore, the observation of this rule becomes a most important check on unskilful classification.

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² In order to adapt the Rules of Division, as here given, to the

The student may easily frame for himself examples of illegitimate divisions. If we were absurdly to divide Europeans into Celts, Teutons, Sclaves, Frenchmen, Spaniards, the Emperor of Russia, and the President of the United States of America, we should have an example of all the faults incident to a division.

In speaking of division by dichotomy I have already introduced the notion of sub-division. For scientific accuracy, and often even for practical purposes, it may be necessary to sub-divide the dividing members, again to sub-divide the results of this division, and so on. The relation of these various divisions and sub-divisions, one to another, has given rise to several logical terms, and is of sufficient importance in itself to require a brief treatment. It is best to commence with an example, and I select a mathematical one, as being of the simplest kind:—



In a series of divisions and sub-divisions like the foregoing, the term at the head of the series (in this case Figure) is called the *Summum Genus*. The terms at the bottom of the series (equilateral triangles, circles, &c.)

Natural Classifications of Science as well as to the Artificial Classifications of ordinary life, an important change has been made in the statement of Rule 4 in the later editions of this work.

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are called Infime Species. - The intermediate terms are called Subaltern Genera, or Subaltern Species, viz. subaltern genera with reference to the terms immediately below them, and subaltern species with reference to the terms immediately above them. Thus triangle would be a subaltern genus with reference to equilateral triangle, a subaltern species with reference to rectilinear figure. Species which fall immediately under the same genus, as e.g. triangle, quadrilateral, and polygon, are sometimes called Cognate Species, but might, perhaps, with greater propriety be called Co-ordinate Species. A Cognate Genus is any one of the ascending genera under which the species falls. Thus triangle, rectilinear figure, figure, are all genera cognate to equilateral triangle. A differentia which constitutes, as is said, the species of which we happen to be speaking, that is, which distinguishes it from its co-ordinate species, is called a Specific Difference, one which constitutes any of its cognate genera is called a Generic Difference. Thus 'equilateral' is a specific difference, 'three-sided' a generic difference of an equilateral triangle. Or, 'three-sided' would be regarded as a specific difference, and 'rectilinear' a generic difference of a triangle. Lastly, a property derived from an attribute or attributes connoted by the species of which we happen to be speaking is called a Specific Property; a property which is derived from any of its cognate genera is called a Generic Property. It is, for instance, a property of all rectilineal figures that the sum of their angles is equal to twice as many right angles as the figure has

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sides, minus four right angles. Thus the angles of a plane triangle are together equal to two right angles, those of a quadrilateral to four, those of a pentagon to six, and so on. It is also a property of a triangle that it may be generated by the section of a cone, but this is not a property common to other rectilinear figures. Hence the latter would be called a specific, the former a generic property.

The instance I have given is one of the simplest that could be selected. If I had taken instead of it, say, the division of animals into vertebrate and invertebrate, of vertebrate animals into fishes, amphibia, reptiles, birds, and mammals, of mammals into the various species of men, horses, oxen, &c., it would have required a long scientific discussion to distinguish the various species and genera, to state the specific and generic differences, and to give instances of specific and generic properties. And yet it is exactly in such a case as this that divisions and sub-divisions (or, in one word, Classifications) are most important. In fact, the sciences of Botany and Zoology (in the vulgar acceptation of these words) consist entirely of classifications. To give rules for so important and complicated a process as scientific classification, or even to attempt any precise definition of the word, would be to go beyond the scope of an elementary work like this 3. It may be sufficient to suggest that where, as in the case of plants and animals, species are

³ The reader will find a special section on Classification in the Author's 'Elements of Inductive Logic.'

separated from one another by an indefinite number of attributes, and may be separated by many attributes of which we are still ignorant, our classifications, like our definitions, should always be regarded as provisional. To this I may add two plain rules, which meet with universal acceptance: first, that our classifications should proceed as gradually as possible; and second, that we should select as our main principles of division attributes the most fruitful in their consequences, i. e. attributes from which the largest number of important properties can be derived. Thus the natural system of Botany, founded, in its main division, on differences in the seed-vessels of plants, is far more instructive than the Linnæan system, founded on differences in the numbers of the pistils and stamens.

Note.—I have employed the expressions 'summum genus' and 'infima species,' as if they were entirely relative to any particular classification. But in the Isagoge of Porphyry, and by the Scholastic logicians who, for the most part, adopted his account, both summa genera and infimæ species, as well as all the subaltern genera and species, were regarded as unalterably fixed by nature. Thus the ten Categories of Aristotle (Substance, Quantity, Quality, Relation, &c.) were regarded as the summa genera, and terms like man, horse, &c. were regarded as

⁴ Such attributes are called by the French physiologists caractères dominateurs. See Milne Edwards, Cours Élémentaire de Zoologie, édition septième, § 367.

expressing infimæ species. Classes like 'black men,' 'Arabian horses,' &c. would not have been admitted to be species at all. We, on the contrary, conceive that there is no limit to our power of making classes; however specialised a group may be, we can almost always think of some attribute, the addition of which will make it more special still. '

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PART III.—OF INFERENCES.

CHAPTER I.

On the Various Kinds of Inferences.

THE third and most important part of Logic treats of Inferences ¹. Wherever we assert a proposition in consequence of one or more other propositions, or, in other words, wherever we regard one or more propositions as justifying us in asserting a proposition distinct from any that has preceded, the combination of propositions may be regarded as an inference. Thus defined, inferences may be divided into inductive and deductive, and deductive inferences may be sub-divided into mediate and immediate. I shall attempt to make these distinctions clear by examples.

The word 'inference' is employed in no less than three different senses. It is sometimes used to express the conclusion in conjunction with the premiss or premisses from which it is derived, as when we speak of a syllogism or an induction as an inference; sometimes it is used to express the conclusion alone; sometimes the process by which the conclusion is derived from the premisses, as when we speak of Induction or Deduction as inferences or inferential processes. Except where the meaning is obvious from the context, I shall endeavour to confine the word to the first-named signification. The terms Induction and Deduction will be appropriated to express processes which result, the former in inductions or inductive inferences, the latter in deductions or deductive inferences, these last being sub-divided into syllogisms and immediate inferences.

I mix tartaric acid and carbonate of soda in certain proportions in water, and I observe that the mixture is followed by an effervescence; from this I infer that, whenever tartaric acid and carbonate of soda are mixed in water in these proportions, effervescence will follow. I put a poker into the fire, and I observe that after a time it becomes red-hot; from this I infer that incandescence can always be produced in iron by a certain degree of heat. I observe five points in the orbit of a planet, and, from my knowledge of mathematics, perceive that they are situated in an ellipse: from this I infer that the entire orbit of the planet is elliptical, and that, in all future revolutions of the planet, a similar orbit will be described. Now what in these cases do I mean by the word 'infer?' That the mixture is followed by effervescence is a matter of observation; but it is only an inferential process which justifies me in asserting that, inasmuch as it could have been produced by nothing else, the effervescence was produced by the mixture, and that, whenever in future I see a similar mixture, I may expect to see it followed by similar results. Two assumptions, it will be seen, underlie this inference: 1st, that every event has a cause, which leads me to assume that the effervescence must have been produced by some cause or other; 2nd, the belief in the uniformity of nature, which leads me to expect that, whenever similar circumstances are repeated, they will be followed by similar results. The reasoning therefore in these cases may be represented as follows:---

The mixture of the tartaric acid with the carbonate

of soda is *followed* by effervescence. (Original Proposition.)

- ... (Owing to the special circumstances of the case and in accordance with the principle that every event must have a cause), the effervescence was produced by the mixture.
- ... (In accordance with the principle of the uniformity of nature), a similar mixture will always be followed by an effervescence.

We may represent the reasoning in the third example in the same manner:—

- We may assert (by virtue of our knowledge of mathematics) that five points which we have observed in the orbit of the planet Mars are situated in the arc of an ellipse. (Original Proposition.)
- ... As there are, comparatively speaking, no causes determining the position of the planet at any given moment, except the attraction of the sun and the continued effects of the initial velocity, we may infer that the fact of the five points observed being situated in the arc of an ellipse is due to the combination of these two causes.
- ... (In accordance with the principle of the uniformity of nature), it may be inferred that all other points in the orbit of the planet are situated in an ellipse, and that, in all future revolutions, a similar orbit will be described; i. e. the orbit of the planet Mars may be regarded as elliptical.

Now inferences of this kind are called *Inductive*. The instances I have selected are remarkably simple, but they are sufficient to shew that an induction may be defined as an inference in which we argue from particulars to adjacent particulars, or (if we speak of the adjacent particulars collectively) from particulars to universals, in accordance with the laws of universal causation and of the uniformity of nature. As to the circumstances which justify us in asserting that one phenomenon or set of phenomena is the cause or the effect of, or is invariably conjoined with, another (for this is the problem of Induction), the student is referred to works specially treating of Inductive Inference. It is sufficient here to distinguish inductive from the deductive inferences which it is our more special business to explain.

2 An Analogy is a form of imperfect induction, and, though justifying a conclusion more or less probable, never leads to certainty. If two objects resemble each other in several important respects, and we argue that any particular attribute which we know to be predicable of the one, and do not know to be either predicable or not predicable of the other, is, on account of the general resemblance of the two objects, also predicable of the other, the argument is called an argument from analogy; and, in the same way, if two objects are dissimilar, we may argue that an attribute which is predicable of the one, is, on account of their dissimilarity, not predicable of the other Thus, from the similarity between the earth and the moon, we might argue that the latter is inhabited, or, from their dissimilarity, that it is not inhabited. The value of the inference always depends on the ratio of the ascertained resemblances to the ascertained differences (it being understood that the resemblances which we take into account are none of them derived, as properties, from each other, and so with the differences), providing that our knowledge of the objects is sufficiently large to justify us in drawing any inference at aller For a more

Beginning where induction ended, we may state such a proposition as this: 'All iron when heated to a certain degree becomes red-hot.' This, if combined with another proposition 'This is a piece of iron,' leads to the conclusion 'This piece of iron, if heated to a certain degree, will become red-hot.' Now it is plain that the con-

detailed analysis of this mode of reasoning, and an estimate of the value to be attached to its conclusions, the student is referred to the author's *Elements of Inductive Logic*, ch. iv., and to Mr. Mill's *Logic*, Bk. III. ch. xx., one of the most instructive and important chapters in his work.

It should be noticed that an analogy, as here described, is not identical with the Analogy of Aristotle, the Aristotelian Analogy being an equality of relations (lσύτης λόγων). Thus the expression,

The intellect: the soul with sight: the body, is an drahoyia. From this analogy it is argued that anything which may be predicated of the one pair of terms may be predicated also of the other. Or, to take a non-Aristotelian instance, which will be more intelligible to beginners:

A colony: the mother-country = a child: a parent. From this analogy it is argued that the reciprocal rights and duties of a colony and the mother-state are the same as those of a child and a parent. In this form of argument, if the relations between the two sets of terms were precisely the same in all respects, the conclusion would be invariably valid; as it is usually found in practice, however, the relations are the same in some respects, but not in others, and, consequently, the conclusion is valid, when based on those points in which the relations are the same, and invalid, when based on those points in which the relations are not the same. Thus, it might be maintained that, in many respects, the relation of the child to the parent is not the same as that of a colony to the mother-country, and, hence, that many of the rights and duties which exist in the one case do not exist in the other. A Metaphor is an analogy of this kind compressed into a single word or phrase.

The fallacy of False Analogy will be noticed below.

clusion we have just drawn was arrived at in a different manner from those noticed above. Instead of being the conclusion of a process by which we argue from particulars to adjacent particulars or from particulars to universals (i. e. from cases which are within the range of our observation to others which are without), it is simply a combination of two propositions into one, being an obvious inference from what has been previously stated in the premisses. Induction has been not inaptly compared to the establishing of a formula, Deduction (for that is the appropriate name of the process which I am now discussing) to the reading it off. Induction leads to truths entirely new, Deduction combines, methodizes, and developes those which we have already gained.

A Syllogism may be called a Mediate Inference, because the two terms of the conclusion are compared in the premisses by means of a third. It is thus opposed to an Immediate Inference, which consists of two propositions only, and in which the inferred proposition is derived from a single proposition without the aid of any other term or proposition, expressed or implied. Both mediate and immediate inferences may be styled deductive as opposed to inductive.

This division may easily be shewn to be exhaustive. In any inference, we argue either to something already implied in the premisses or not; if the latter, the

If we state explicitly all the assumptions made in the inductive process, the conclusion is contained in the premisses, and the form of the reasoning becomes deductive; but it is seldom that we do state

inference is inductive, if the former, deductive. If the deductive inference contain only a single premiss, it is immediate; if it contain two premisses and the conclusion be drawn from these jointly, it is mediate and is called a syllogism. All deductive inferences which apparently contain more premisses than two admit of being analysed into a series of syllogisms.

Note 1.—I am here departing from the ordinary scheme of division adopted by logicians. Inferences are generally divided into mediate and immediate, and mediate inferences are subdivided into inductive and deductive. As however I regard inductions as more strongly contrasted with both syllogisms and immediate inferences than either of these classes is with the other, it seems preferable to make inductions one of the main members, rather than

our assumptions thus explicitly. The most essential distinction, however, between inductive and deductive reasoning consists not in the form of the inferences, but in the nature of the assumptions on which they rest. Deductive reasoning rests on certain assumptions with regard to language and co-existence (namely, the so-called Law of Identity, or some modification of that law, the Law of Contradiction, the Law of Excluded Middle, and the Canons of Syllogism), while inductive reasoning assumes over and besides these laws the truth of the Laws of Universal Causation of the Uniformity of Nature and, in certain cases, of the Conservation of Energy; or, if it be of the unscientific description which is known as Inductio per Enumerationem Simplicem, it merely assumes, instead of them, the vague and wide principle that the unknown resembles, or will resemble, the known. It hardly needs to be added that all reasoning alike assumes the trustworthiness of present consciousness and of memory,

one of the subordinate members of the division. Nor is there any reason why an immediate inference should not be regarded as deductive.

It should also be noticed that Sir W. Hamilton would deny the title of inferences to inductions (as they have been here explained), whereas Mr. Mill would deny that either a syllogism or an immediate inference can properly be called an inference. Mr. Mill maintains that all Inference is 'from the known to the unknown'; Sir W. Hamilton defines Inference as the 'carrying out into the last proposition what was virtually contained in the antecedent judgments.'

Note 2.—The Aristotelian induction, in which the conclusion affirms or denies of a group what was in the premisses affirmed or denied of each member of the group severally, is, according to the above method of treatment, obviously regarded as a deductive inference. If I predicate some quality of each member of a group, and thence infer that all members of the group possess this quality, the conclusion is plainly contained in the premisses, and the inference is a syllogism. It may be represented in the form.

. . . A is B.

The minor premiss, when stated in so peculiar a form, of course admits of simple conversion, and thus assumes the form given in the text.

⁴ By Aristotle himself the inductive inference is analysed thus : x, y, z are B, x, y, z are (i.e. constitute) A;

x, y, z are B,

The individuals (or subordinate species) constituting the group A are x, y, z;

... The individuals (or subordinate species) constituting the group A are B.

Such an inference is altogether different from what we now understand by an induction. On this subject the student may with advantage read Mr. Mill's chapter on 'Inductions improperly so called.' See Mill's Logic, Bk. III. ch. ii. An account of the Aristotelian induction will be found in Appendix G to Dr. Mansel's edition of Aldrich; in Sir W. Hamilton's Essay on Logic, and in his Lectures on Logic, Lect. xvii. and Appendix vii. These authors, as already noticed in the case of Sir W. Hamilton, regard inductions, in the modern sense of the word, as extra-logical. The advanced student may also consult with advantage Mr. De Morgan's chapter on 'Induction,' Formal Logic, ch. xi.



CHAPTER II.

On Immediate Inferences.

§ 1. AN Immediate Inference may be formally defined as a combination of two propositions of which one is inferred from the other, the proposition inferred being virtually included in the proposition from which it is inferred. Of Immediate Inferences the most important forms are Oppositions, Conversions, Permutations 1.

§ 2. On Oppositions.

Two propositions are said to be opposed when they have the same subject and predicate, but differ in quantity or quality or both. An Opposition may be defined as an immediate inference in which from the truth or falsity of one proposition we infer either the truth or falsity of another, this proposition having the same subject and predicate as the former, but differing in quantity or quality or both. Thus from the proposition 'That all X is Y is true' we may infer the proposition 'That no X is Y is false,' or 'That some X is Y is false,' or 'That some X is Y is false,'

It is the more common practice to speak of Opposition, Conversion, and Permutation, but I have adopted the plural number in order to draw attention to the fact that Logic is concerned with the results rather than with the processes by which they are arrived at.

The opposition between

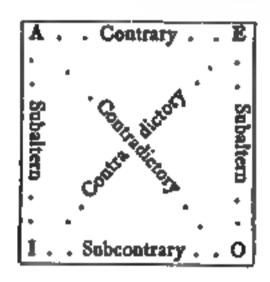
A and E is called a Contrary Opposition.

I and O, a Subcontrary Opposition.

A and I, or E and O, a Subaltern Opposition.

A and O, or E and I, a Contradictory Opposition.

These forms of Opposition are exhibited in the annexed scheme:—



If A be true; E is false, I true, O false.

If A be false; E is unknown, I unknown, O true.

If E be true; A is false, I false, O true.

If E be false; A is unknown, I true, O unknown.

If I be true; A is unknown, E false, O unknown.

If I be false; A is false, E true, O true.

If O be true; A is false, E unknown, I unknown.

If O be false; A is true, E false, I true.

It will be observed that it is only in a Contradictory Opposition (where the opposed terms differ both in quantity and quality) that from the truth or falsity of one proposition we can invariably infer the truth or falsity of another, the conclusion which we draw in this case being from the truth or falsity of the one propo-

sition to the falsity or truth respectively of the other. Hence logicians have called contradictory the most perfect form of opposition. It is a rule of practical Logic that a contradictory should always in disputations be used in preference to a contrary opposition; for it serves equally well the purpose of contradicting an opponent, and the particular proposition which it asserts affords less ground for attack than an universal. Thus, if my opponent asserts A (as e.g. All philosophers are unimaginative), I may meet his assertion by the contradictory O (Some philosophers, as e.g. Plato, Goethe, &c., are not unimaginative), and from this position I cannot well be dislodged. But suppose I assert in opposition to him an E proposition (No philosophers are unimaginative), he will probably be able to adduce instances of some philosophers who, according to the ordinary meaning of the word 'imaginative,' would be called unimaginative, and so, by meeting my E with an I proposition, gain an apparent victory. As a fact, we should each have made assertions too wide, but he would have succeeded in dislodging me from my position, whereas (owing to my neglect of the laws of contradiction) I should not have succeeded in dislodging him from his.

Note.—It is plain that, according to the ordinary meaning of the word 'opposition,' it is somewhat of an abuse of language to speak of A and I, or E and O propositions as being opposed. It would be better

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if this form of inference were called Subalternation or Subordination.

Nor, strictly speaking, can the relation between I and O be called one of opposition, for they may both be true together. Accordingly, Aristotle says that in reality (κατ' ἀλήθειαν) there are three forms of opposition (those between A and E, A and O, E and I), though in language (κατὰ τὴν λέξων) there are four (adding that between I and O). What is called Subaltern Opposition he does not recognise.

§ 3. On Conversions.

A proposition is said to be converted when its terms are transposed, so that the subject becomes the predicate, and the predicate the subject. A Conversion may be defined as an immediate inference in which from one proposition we infer another having the same terms as the original proposition, but their order reversed. This inference in some cases necessitates a change of quantity in passing from one proposition to the other, and then it is called a Conversion per accidens; when it necessitates no such change, it is called a Simple Conversion.

I and E may both be converted simply. Thus, from 'Some X is Y,' or 'Some poets are philosophers,' I may infer 'Some Y is X,' or 'Some philosophers are poets.' From 'No X is Y,' or 'No savages are trustworthy,' I may infer 'No Y is X,' or 'No trustworthy persons are savages.'

^{*} It is proposed by Sir W. Hamilton to call the original proposition the 'Convertend,' the inferred proposition the 'Converse.'

A can only be converted per accidens. For though it may sometimes happen that the subject and predicate of an A proposition are co-extensive, and therefore convertible, this circumstance is not implied in the form of the proposition, and it is with what is implied in the form of the proposition that we are alone concerned. Thus, if I assert the proposition 'All plane triangles are three-sided rectilineal figures,' it happens in this particular case that I am justified, without any change of quantity, in stating the converse, 'All three-sided rectilineal figures are plane triangles.' But if I state that 'All plane triangles are rectilineal figures,' I am only justified in inferring that 'Some rectilineal figures are plane triangles.' As, therefore, the general form of an A proposition does not imply the simple convertibility of the subject and predicate, I am only justified in inferring from 'All X is Y,' that 'Some Y is X.'

In those cases, however, in which the form of the proposition implies that the subject and predicate are coextensive, the proposition, though an A proposition, may be converted simply. Thus, from the propositions 'The second legion is the only legion quartered in Britain,' 'Virtue is the condition of Happiness,' 'All plane triangles may be defined as three-sided rectilineal figures,' it may be inferred by simple conversion that 'The only legion quartered in Britain is the second legion,' 'The condition of Happiness is Virtue,' 'All three-sided rectilineal figures may be called plane triangles.'

An O proposition cannot be converted at all. From

'Some X is not Y,' it does not follow that 'Some Y is not X,' for Y may stand to X in the relation of a species to a genus. Thus from the proposition 'Some Europeans are not Frenchmen,' I cannot infer that 'Some Frenchmen are not Europeans.'

§ 4. On Permutations3,

A Permutation may be defined as an immediate Inference in which from one proposition we infer another differing in quality, and having, therefore, instead of the original predicate its contradictory. Thus:—

From All X is Y, we may infer that No X is not-Y.

From No X is Y, All X is not-Y.

From Some X is Y, Some X is not not-Y.

From Some X is not Y, . . . Some X is not-Y.

The legitimacy of these inferences is apparent from the fact that contradictory terms (A and not-A) admit of no medium, so that, if I predicate the one affirmatively, I may always predicate the other negatively, and vice versa.

The O proposition, when permuted from 'Some X is not Y,' into 'Some X is not-Y,' may of course be converted into 'Some not-Y is X.' This combination of permutation and conversion is improperly described by Whately and many previous logicians as a single inference, and styled 'Conversion by Contra-Position or Negation.'

² The term Permutation is borrowed from Mr. Karslake's Aids to Logic. The same inference is sometimes called Infinitation, from the Nomen Infinitum, or, more properly, Nomen Indefinitum (not-Y, as the contradictory of Y), which is employed as the predicate.

It may assist the student if I add some further instances of permutations:—

All men are fallible, ... No men are infallible.

No men are infallible, ... All men are fallible.

Some poets are reflective, ... Some poets are not unreflective.

Some poets are not unreflective, ... Some poets are reflective.

All poets are men of genius, ... (by permutation) No poets are not-men-of-genius; ... (by conversion) No not-men-of-genius (= None but men of genius) are poets.

Note.—I have here employed an expression 'Contradictory Terms,' which in most works on Logic is explained in the first part, as included under the doctrine of Opposition of Terms. It seemed, however, desirable to introduce there only those distinctions of terms which were likely to be frequently required in the sequel of the work. I may here state that 'Contradictory Terms,' such as white and not-white, lawful and un-lawful, are terms which admit of no medium, i.e. terms which are not both predicable of the same thing, while one or other of them must be predicable of it. 'Contrary Terms,' like good and bad, black and white, are terms which are the most opposed under the same genus; they cannot both be predicated of the same thing, but it is not necessary that one or other of them should be predicable of it.

CHAPTER III.

On Mediate Inference or Syllogism.

§ 1. The Structure of the Syllogism.

A SYLLOGISM may be defined as a combination of two propositions, necessitating a third in virtue of their mutual connexion; or as an inference in which one proposition is inferred from two others conjointly, the inferred proposition being virtually contained in the propositions from which it is inferred. This is obviously a definition of a legitimate syllogism. There may (as will appear below) be apparent syllogisms, which do not fulfil the conditions of this definition. We may take as instances of syllogisms:—

- (I) All B is A, All C is B;
 - ... All C is A.
- (2) All sovereign powers are invested with supreme authority over their subjects,

All republics are sovereign powers;

- ... All republics are invested with supreme authority over their subjects.
- (3) No rectilinear figure is bounded by one line, A circle is bounded by one line;
 - ... A circle is not a rectilinear figure.

The proposition inferred is called the Conclusion, the propositions from which it is inferred the Premisses, either of them singly being called a Premiss.

As the conclusion is virtually contained in the premisses conjointly, it is plain that the two terms of the conclusion must occur in the premisses, one in either. If both terms occurred in the same premiss, the other premiss would be entirely alien to the conclusion. The remaining term of each premiss must be the same; else there would be nothing in common between the two premisses, and the conclusion could not be said to be inferred from the two conjointly. This third term, with which the two terms of the conclusion may be regarded as compared, is called the middle term. The predicate of the conclusion is called the major term, and the subject the minor term; the premiss, in which the major and middle terms are compared, is called the major Premiss, and should always be stated first; that in which the minor and middle terms are compared is called the minor premiss. Thus in a syllogism, formally stated, there are always three propositions including three terms, the premisses occurring first and the conclusion last. But practically, in reasoning, we frequently state the conclusion first, introducing one or both premisses with such a word as 'for' or 'because,' as stating our reason for the assertion. Thus I may say 'I will not go out to-day, for it is raining,' or, 'I will not go out to-day, for it is raining, and the rain may give me a cold.' When stated in this form, the conclusion is called by the older logicians the Problema

or Quæstio, being regarded as a question to which the reason or reasons assigned furnish the answer. It will also have occurred to the student that, as a fact, we usually state only one premiss, leaving the other (which may be either the major or minor) to be understood. Thus, instead of stating Syllogism (2) formally, as above, I should in an actual discussion say, 'A republic is invested with supreme authority over its subjects, for every sovereign power is invested with such authority,' or, 'A republic is, &c., for it is a sovereign power,' or briefly, 'A republic (being a sovereign power) is invested,' &c.; or, the premiss coming first, 'Inasmuch as every sovereign power is invested, &c., I maintain a republic to be invested with that authority,' or, 'Inasmuch as a republic is a sovereign power, it is invested with, &c. Instead of suppressing one of the premisses, I may, for brevity's sake, suppress the conclusion. Thus I may say 'Every sovereign power is invested with supreme authority over its subjects, and a republic is a sovereign power,' leaving it to the hearer or reader to draw the conclusion for himself. The syllogism does not pretend to be the form, or even a form, in which our reasonings are usually stated, but simply one of the ultimate analyses of them.

As every term in the syllogism occurs twice, it should be noticed that, on both occasions, it should be used in the same sense, or, to adopt technical language, every

¹ A syllogism with a suppressed premiss is by Aldrich wrongly identified with the Enthymeme of Aristotle. Such a syllogism was called by the Stoics a συλλογισμός μονολήμματος.

use a term equivocally, i.e. in two entirely different senses, or even analogously, i.e. in two different senses having some relation to each other, it is plain that, logically speaking, we are using two different terms, and consequently the syllogism will include four terms instead of three. This caution includes the rule usually given by logicians against an ambiguous middle. The neglect of it, palpable as it might be supposed to be, is often, especially in a long course of reasoning, very difficult of detection, and is a fertile source of fallacy. I may adduce as very simple instances:—

Humanity is a moral virtue,

The study of polite letters is humanity;

... The study of polite letters is a moral virtue.

The church is the aggregate of all Christian people,

This particular congregation (or particular building) is the church (meaning at some particular place);

... This particular congregation (or particular building) is the aggregate of all Christian people.

In the former case, the term 'humanity' has come to be used in such widely different senses, that it may be regarded as used equivocally; in the latter case, the senses of the word 'church' are perhaps sufficiently nearly allied to be regarded as analogous. All cases of what are termed 'Verbal Fallacies' may be referred to this head.

Note.—The words 'major,' 'minor,' and 'middle,' as applied to the terms in a syllogism, have been inherited

by all subsequent logicians from the nomenclature of Aristotle. He regarded what we shall presently call the First Figure (B is or is not A, C is B, ... C is or is not A) as the perfect type of syllogism, and, amongst other modes, stated it in the form C is in B (rd I corio do δλφ τφ B), B is or is not in A, ... C is or is not in A. Thus stated, C appears to be the smallest, B the intermediate, and A the largest term in extent. See Prior Analytics, Bk. I. ch. iv. In negative propositions, however, we have no means of determining the relative extent of the subject and predicate, and consequently Aristotle's nomenclature does not properly apply to negative syllogisms. To affirmative syllogisms in the first figure, whether universal or particular, it applies only in a modified shape, for the propositions All X is Y, Some X is Y, though they imply that Y cannot be less in logical extent than All X in the one case or than Some X in the other, do not exclude the possibility of the subject and predicate being co-extensive. Hence, however convenient it may be, Aristotle's nomenclature applies only, and that not with strict accuracy, to two forms of syllogism (Barbara and Darii) in the first figure.

§ 2. On Moods and Figures.

I now proceed to consider the possible, not the legitimate, forms of syllogism. Here there are two circumstances to be taken into consideration: 1st, that syllogisms may vary according to the quantity and quality

of the propositions (A, E, I, O) of which they are composed; 2nd, that they may vary according to the position of the terms in the premisses. The first consideration gives us the number of possible moods, the second the number of possible figures. It is by combining these two sources of variation that we shall obtain the number of possible syllogisms.

There are, if we take into consideration the conclusion, sixty-four possible arrangements of the propositions A, E, I, O, i. e. in technical language, sixty-four possible moods, viz. AAA, AAE, AAI, AAO, &c. But if we consider the premisses only, the number of possible moods is limited to sixteen, viz. AA, AE, AI, AO, EA, EE, EI, EO, IA, IE, II, IO, OA, OE, OI, OO. In determining what possible moods are legitimate, we may either ask 'Is this conclusion justified by these premisses?' or 'To what conclusion do these premisses lead?' If we ask the former question, we must examine the sixty-four possible moods in which the conclusion appears as well as the premisses; if the latter, an examination of the sixteen possible arrangements of premisses is sufficient.

With respect to the possible arrangements of the terms in the premisses (i. e. the figures, as they are technically called) there are also two methods of proceeding. Taking no account of the conclusion (and therefore not knowing which is the major term and which the minor), and asking simply 'In how many ways can the middle term be combined with the other terms in the premisses?' there are three possible figures; viz. 1st, that in which the

middle term is subject in one premiss and predicate in the other; 2nd, that in which it is predicate in both premisses; 3rd, that in which it is subject in both. But if we take account of the conclusion, we are able to distinguish the major and minor terms, and consequently the major and minor premisses. In this case, there are four possible figures, viz. 1st, that in which the middle term is subject in the major premiss and predicate in the minor; 2nd, that in which it is predicate in both premisses; 3rd, that in which it is subject in both; 4th, that in which it is predicate in the major premiss and subject in the minor. These four figures may be exhibited thus:—

| Fig. 1. | Fig. 2. | Fig. 3. | Fig. 4. |
|---------|---------|---------|---------|
| BA | AB | BA | AB |
| CB | CB | BC | BC |
| CA | CA | CA | .·. CA. |

If we take no account of the conclusion, either extreme in the premisses may become the major term, and the three figures may be represented thus:—

| Fig. 1. | Fig. 2. | Fig. 3. |
|----------|----------|-----------|
| BA | AB | BA |
| CB | CB | BC |
| CA or AC | CA or AC | CA or AC. |

§ 3. Determination of the Legitimate Moods of Syllogism.

Note.—Few difficulties in elementary Logic are more likely to embarrass the beginner than the variety of methods of constituting the Legitimate Moods of Syllogism. Sir W. Hamilton, as a consequence of quantifying

the predicate, is able to represent all syllogisms as equations, and thus to exhibit every affirmative syllogism as a direct application of what is called the Law of Identity (Every A is A), and every Negative Syllogism as a direct application of the Law of Contradiction (No A is not-A)². Besides Sir W. Hamilton, other logicians who do not, like him, quantify the predicate, have also attempted to enunciate general principles equally applicable to all syllogisms. See e.g. Port Royal Logic, Part III. ch. x. Others (as Abp. Thomson, Laws of Thought, § 96, and Lambert, as quoted by Dr. Mansel in his Notes on Aldrich, ch. iii. § 6) enunciate a distinct principle for each figure. Others (and pre-eminently Aristotle) enunciate a canon for the first figure², and test

These two Laws (or Principles) together with the Law or Principle of Excluded Middle (A either is or is not B) and the Law or Principle of Sufficient Reason (Infer nothing without a ground or reason), are often called the Fundamental Laws of Thought. See Thomson's Laws of Thought, § 114, and Hamilton's Lectures on Logic, Lects. vi. and vii.

^{*} Λέγομεν δὲ τὸ κατὰ ταντὸι κατηγορείσθαι, ὅταν μηδὲν ἢ λαβείν τῶν τοῦ ὑποκειμένου, καθ' οῦ θάτερον οὺ λεχθήσεται καὶ τὸ κατὰ μηδενὸς ὡσαύτως, Απ. Pr. I. I; ὅσα κατὰ τοῦ κατηγορουμένου λέγεται νάντα καὶ κατὰ τοῦ ὑποκειμένου ἡηθήσεται, Cat. 3. This principle oc canon in its Latin form was called by the Schoolmen the Dictum de Omni et Nullo. It is thus stated by Sanderson: 'Dictum de Omni est hujusmodi: Quidquid affirmatur Universaliter de aliquo Subjecto, affirmari necesse est de tis quæ sub eo continentur. Dictum de Nullo hujusmodi: Quidquid negatur Universaliter de aliquo Subjecto, negari necesse est de iis quæ sub eo continentur.' By Aldrich it is stated in a more compressed form, as follows: 'Quod prædicatur Universaliter de alio (i.e. de termino distributo), sive affirmative, sive negative, prædicatur similiter de omnibus, sub eo contentis.'

them to the first. Lastly, a favourite method amongst logicians is to enumerate the faults which are incident to a syllogism, and then reject those moods in which they are found. This method is often combined with one or more of the others. Aldrich, for instance, enunciates general canons of syllogism, then uses the method I have last explained, and finally reduces syllogisms in the other figures to their corresponding forms in the first.

In accordance with the ordinary practice of elementary treatises, and as being perhaps at first more intelligible to the learner, I shall take into consideration the conclusion, and consequently regard the number of figures as four, and that of possible moods as sixty-four, reserving for a note the shorter and more scientific procedure. The problem therefore now before us is to determine which of the sixty-four moods are admissible in each of the four figures.

In the first figure our task is easy. There we are able to establish a canon which will determine directly the legitimate moods.

With a little attention the student will be able to perceive the truth of the following propositions:—

- (a) If one term be affirmed of another (provided the latter be taken in its entire extent), and this term of a third, the first may be affirmed of the third.
- (B) If one term be denied of another (provided the

latter be taken in its entire extent), and this term affirmed of a third, the first may be denied of the third.

- (γ) If one term be affirmed of another (even though the latter be taken in its entire extent), and this term denied of a third, we are not justified in drawing any conclusion as to the relation of the first to the third. For, if one term be denied of another, it does not follow that whatever may be predicated of this first term may also be denied of the other: thus I may deny 'red' of 'blue,' but it does not follow that 'colour,' which I predicate of 'red,' may also be denied of 'blue.'
- (8) If one term be denied of another (even though the latter be taken in its entire extent), and this term denied of a third, no conclusion can be drawn as to the relation of the first to the third. For, because I deny one term of another, it does not follow that whatever I can deny of the first can also be denied of the other, nor does it follow that it can be affirmed of it: thus, because I can deny 'white' of crows, and 'black' of 'white' (or rather of the corresponding common term 'white things'), it does not follow that I can deny 'black' of crows; nor, because I can deny 'white' of crows as well as 'yellow' of 'white' (or 'white things'), does it follow that I can affirm 'yellow' of crows.

Putting together these results, we obtain the following

canon of reasoning in the first figure: If one term can be affirmed or denied of another (provided that the latter be taken in its entire extent), and this term affirmed of a third, the first can be affirmed or denied (respectively) of the third; and, if these conditions are not fulfilled, no conclusion can be drawn. The only moods which fulfil the conditions of the canon are AAA, EAE, AII, and EIO. The conclusions of two other moods, namely, AAI and EAO, might be inferred, by Subaltern Opposition, from those of AAA and EAE, and hence these are called Subaltern Moods.

We have obtained, it will be observed, forms of syllogism capable of proving any one of the four propositions, A, E, I, or O, and into one or other of the types accepted as legitimate moods of the first figure all our mediate reasonings may be thrown. Here, then, our enquiry might terminate, if it were simply our object to obtain a sufficient number of legitimate types of reasoning, but the problem before us is to state exhaustively all possible forms which can be accepted as legitimate.

There being no canon which distinguishes with equal precision the legitimate and illegitimate moods of the other figures, we must, in discussing them, have recourse to some other method. I shall first enumerate and explain certain syllogistic rules (derived from the definition

It will be plain from the statement of the Canon that the major premiss of a syllogism in the first figure must be universal. At the suggestion of Mr. St. G. Stock of Pembroke College, this fact has been made plainer in the statement of the Canon itself than was the case in the earlier editions.

of a syllogism) which will exclude illegitimate moods, and then, before accepting the remainder, I shall test them by reducing them to the first figure.

Syllogistic Rules.

I. The middle term must be distributed at least once. For, if in both premisses it were used in only a partial signification, it might denote entirely different objects in the one premiss from those which it denoted in the other, and so there might be no connexion between the two premisses. Thus, in the premisses 'All men are animals,' 'All horses are animals,' the part of the group 'animals' which is coincident with 'men' may be, and here is, entirely distinct from that portion of the group which is coincident with 'horses,' and consequently we can draw no conclusion as to the relation between men and horses. This fallacy is called *Undistributed Middle*.

II. If a term be distributed in the conclusion, it must have been previously distributed in the premisses. The reason is obvious. If we use a term in a partial signification in the premisses, we cannot legitimately use it in its entire signification in the conclusion. To do so would be to argue from part to whole, or, in other words, to employ a term in a wider signification in the conclusion than that in which it is employed in the premisses.

This fallacy is called *illicit process* of the major or minor, according as the term illegitimately distributed in the conclusion is the major or minor term. In the syllogism.

Some A is not B,
All B is C,
∴ Some C is not A,

we have illicit process of the major; in the syllogism,

All B is A, Some C is B, ∴ All C is A,

illicit process of the minor.

- III. Two negative premisses prove nothing. For they simply assert that there is no connexion between the middle term and the extremes; consequently we can draw no conclusion with respect to the relation of the extremes.
- IV. If either of the premisses be negative, the conclusion must be negative. For the other premiss is affirmative, and, if in one premiss we affirm a connexion between the middle term and one of the extremes, and in the other premiss deny any connexion between the middle term and the other extreme, there can be no connexion between the two extremes.
- V. If the conclusion be negative, one of the premisses must be negative. For we cannot deny that there is any connexion between the extremes, except we have previously denied that there is any connexion between one of the extremes and the middle term.
- VI. Two particular premisses prove nothing. For they cannot be both negative (O, O). Nor can they be both affirmative (I, I), for then the middle term would be undis-

tributed. The only remaining case is that of one affirmative and one negative premiss (I, O). But this combination of premisses would leave no term to be distributed in the conclusion. Hence the conclusion would be an I proposition, an affirmative conclusion inferred from a negative premiss, which (according to Rule IV) is illegitimate.

VII. If one premiss be particular, the conclusion must be particular.

The premisses must be either both affirmative, or one affirmative and one negative (see Rule III).

Now, if they are both affirmative, they will (by Rule VI) be A and I. This combination of premisses, as it contains only one distributed term, and the middle term must be distributed at least once (Rule I), leaves no term to be distributed in the conclusion: consequently the conclusion must be I.

If the premisses are one affirmative and one negative, they must (by Rule VI) be either O and A or I and E. In either case the premisses distribute only two terms, and, as one of them must be the middle term (by Rule I), there remains only one term to be distributed in the conclusion. But the conclusion must be negative (by Rule IV). Therefore, it must be O.5.

The converse of this Rule, viz. that a particular conclusion necessitates a particular premiss, is not true. The only cases however in which we find a particular

⁵ This proof is substituted for the somewhat more elaborate proof given in the earlier editions.

conclusion without a particular premiss are those in which the premisses assume more than is required in order to prove the conclusion. This fact will be apparent to the student from an examination of the individual cases, and it might be laid down as a rule that, wherever there is a particular conclusion without a particular premiss, something superfluous is invariably assumed in the premisses ⁶.

Of the above Rules, it is plain that Rules III, IV, V, VI, VII are applicable to the moods before they are referred to the several figures, Rules I and II are applicable only when the moods are referred to some particular figure.

By the application of the first set of Rules, the sixtyfour possible moods are reduced to twelve, viz.

AAA, AAI, AEE, AEO, AII, AOO, EAE, EAO, EIO, IAI, IEO⁷, OAO.

Thus EEE is rejected because it has two negative premisses, EAA because it has a negative premiss without a negative conclusion, AAE because it has a negative

• The syllogistic rules are comprised in the mnemonic lines:— Distribuas medium; nec quartus terminus adsit. Utraque nec præmissa negans, nec particularis. Sectetur partem conclusio deteriorem. Et non distribuat, nisi cum præmissa, negetve.

¹ It has been suggested to me by Professor Park that IEO might be rejected by the application of Rule II, even before it is referred to any particular figure. For the conclusion, O, distributes its predicate, that is the major term of the syllogism. But the major premiss, being I, evidently does not distribute this term. Consequently, there is invariably Illicit Process of the Major.

< 10 P

conclusion without a negative premiss, III because it has two particular premisses, IAA because it has a particular premiss without a particular conclusion.

By the application of Rules I and II to these twelve moods, when referred to the several figures, there remain :—

in fig. 2, EAE, AEE, EIO, AOO, EAO, AEO; in fig. 3, AAI, EAO, IAI, OAO, AII, EIO; in fig. 4, AAI, AEE, IAI, EAO, EIO, AEO.

I append a few examples of the method of testing the moods, when referred to the figures.

Take AEE in figure 2.

A All A is B,

No C is B;

... No C is A. No fault.

Take IEO in figure 3.

Some B is A, Ī

E No B is C;

O . . . Some C is not A.

Illicit process of major.

Take AII in figure 4.

All A is B, A

Some B is C; Ι

. . . Some C is A. Undistributed middle.

It will be seen that of the sixty-four moods, when referred to the four figures, there are only six in each which have not been rejected. It now remains further to test

these moods in the second, third, and fourth figures by reducing them to moods in the first.

Reduction.

As we have adopted no canon for the second, third, and fourth figures, we have as yet no positive proof that the six moods remaining in each of those figures are valid; we merely know that they do not offend against any of the syllogistic rules. But, if we can reduce them, i.e. bring them back to the first figure, by shewing that they are only different statements of its moods, or, in other words, that precisely the same conclusions can be obtained from equivalent premisses in the first figure, their validity will be proved beyond question. There are two methods of performing this operation: 1st, that called Ostensive Reduction, which consists in employing one or more of the processes of conversion, permutation, and transposition of premisses; and, that called Reductio per impossibile, which consists in shewing, by means of the first figure and the laws of opposition, that the contradictory of the conclusion is false, and therefore the conclusion itself true. Either of these methods is applicable to all the eighteen moods, and the result is that all are proved to be valid. I shall give instances of the application of each method.

By ostensive reduction I shall test EAO in the fourth, IAI in the third, AEE and AOO in the second figures.

| Fig. 4. | Fig. 1. |
|--------------------|---|
| E No A is B. | No B is A. (Simple Conversion.) |
| A All B is C. | Some C is B. (Conversion per acc.) |
| O Some C is not A. | Some C is not A. |
| Fig. 3. | Fig. 1. |
| I Some B is A. | All B is C. |
| A All B is C. | . · . Some A is B. (Simple Conversion.) |
| I Some C is A. | Some A is C. |
| | Some C is A. (Simple Conversion.) |
| Fig. 2. | Fig. 1. |
| A All A is B. | No B is C. (Simple Conversion.) |
| E No C is B. | All A is B. |
| E No C is A. | No A is C. |
| | . · . No C is A. (Simple Conversion.) · |
| Fig. 2. | Fig. 1. |
| A All A is B, | No A is not-B. (Permutation.) |
| | No not-B is A. (Simple Conversion.) |
| O Some C is not B. | Some C is not-B. (Permutation.) |
| O Some C is not A. | Some C is not A. |

The mark × shews that the premisses are transposed; the sign ... on the right-hand side of the page is here appropriated to express the employment of conversion or permutation. The last example is interesting, because AOO in fig. 2, and OAO in fig. 3, inasmuch as they contain O premisses, cannot be reduced by the ordinary methods of transposition of premisses and conversion. Hence the older logicians (who, with few exceptions, did not recognise permutation) applied to them the tedious method of reductio per impossibile (or, if we write it in full, reductio per deductionem ad impossibile). This method is equally applicable to all the imperfect moods, as the moods of the three last figures are often called. I now proceed

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to give an example of it, and shall select AAI in the third figure.

A All B is A,
A All B is C;
I ... Some C is A.

This conclusion must be true: for, if not, suppose it to be false;

Then its contradictory must be true, i. e.

No C is A.

But (from the premisses) All B is C. Syll. II.
... (By figure 1) No B is A.

But (from the premisses) All B is A.

Now these two (being contrary propositions) cannot both be true.

But the proposition All B is A is assumed to be true.

... The proposition No B is A must be false.

Hence, either the reasoning of Syll. II. is faulty, or one of the premisses is untrue.

But the reasoning (being in the first figure) must be valid.

...One of the premisses is false.

Now the premiss 'All B is C,' being one of the premisses of the original syllogism, is assumed to be true.

- ... The other premiss (No C is A) must be false.
- . . . Its contradictory (Some C is A) is true.

Q. E. D.

As the positive test of reduction confirms in every case the negative test of the syllogistic rules, it follows that six moods (though not the same six moods) are valid in each figure. These moods may be remembered by means of the mnemonic lines:—

Barbara, Celarent, Darii, Ferioque, prioris:
Cesare, Camestres, Festino, Baroko, secundæ:
Tertia, Darapti, Disamis, Datisi, Felapton,
Bokardo, Ferison, habet: Quarta insuper addit
Bramantip, Camenes, Dimaris, Fesapo, Fresison:
Quinque Subalterni totidem Generalibus orti,
Nomen habent nullum, nec, si bene colligis, usum.

In the above lines, the initial consonants, B, C, D, F, shew that the mood in the second, third, or fourth figure to which they are prefixed is to be reduced to the mood correspondingly marked in the first. Thus Disamis, when reduced, will become Darii. The vowels shew the moods; thus Disamis represents IAI in the third figure. The letter s, when it occurs after a vowel, shews that the proposition for which that vowel stands is to be converted simply, the letter p that it is to be converted per accidens.

^{*} It should be noticed that when these letters follow the conclusion, as is the case in Camestres, Disamis, Bramantip, Camenes, Dimaris, they apply not to the conclusion of the mood given for reduction but to the conclusion of the equivalent mood in the first figure, to which such mood is to be reduced. Thus, in reducing Bramantip, the student will find that the p affects not the I conclusion of Bramantip, but the A conclusion of the corresponding syllogism in Barbara. See, for other instances, p. 101.

The letter m shews that the premisses are to be transposed, k that the mood is to be reduced per impossibile. It will be noticed that & occurs only in two moods, Baroko and Bokardo, but I have shewn that the per impossibile method is equally applicable to all imperfect moods, and that these two moods can be reduced ostensively by means of permutation, so that any imperfect mood may be reduced either ostensively or per impossibile. The initial B in Baroko and Bokardo shews that the per impossibile method, in their case, assumes the validity of Barbara, but in other cases the operation may assume the validity of some one of the other moods in the first figure; thus, in the particular instance I have taken above, it is performed by means of Celarent. It is perhaps needless to add that all letters, not already explained in the mnemonic lines, are non-significant.

The nature of the *subaltern moods* has already been explained. They are, AAI, EAO in fig. 1, EAO, AEO in fig. 2, and AEO in fig. 4, included respectively in AAA, EAE, EAE, AEE, AEE. They cannot properly be regarded as illegitimate, inasmuch as the conclusions are valid, but they are superfluous, inasmuch as they infer less than is justified by the premisses.

. . !

^{*} If we take * to signify the employment of permutation, Baroko and Bokardo may be replaced respectively by Fassoso and Dossamoss. These terms are adapted from Whately's Logic, Bk. II. ch. iii. § 5.

The Special Rules.

Besides the general syllogistic rules, already enunciated and proved, certain Special Rules have been enunciated for each figure. I give them below as generally stated. Those for the first figure have been proved in establishing its canon; those for the other figures the student may verify for himself by applying the rules, already laid down, on the distribution of terms.

- Fig. 1. (a) The minor premiss must be affirmative.
 - (B) The major premiss must be universal.
- Fig. 2. (a) One or other premiss must be negative.
 - (3) The conclusion must be negative.
 - (γ) The major premiss must be universal.
- Fig. 3. (a) The minor premiss must be affirmative.
 - (β) The conclusion must be particular.
- Fig. 4. (a) When the major premiss is affirmative, the minor must be universal.
 - (β) When the minor premiss is affirmative, the conclusion must be particular.
 - (γ) In negative moods the major premiss must be universal.
 - (8) The conclusion cannot be an universal affirmative, nor either of the premisses a particular negative.

Note.—If, leaving out of consideration the conclusion, we regard the number of possible figures as three and that of possible moods as sixteen, we may proceed as follows.

Having enunciated the canon of the first figure, we may constitute the moods Barbara, Celarent, Darii, and Ferio. The subaltern moods, AAI and EAO, are not admissible, as the question here before us is not 'What conclusions are justified by such and such premisses,' but 'To what conclusions do such and such premisses lead?' Now, from this point of view, the conclusions of the subaltern moods are not directly inferred from the premisses, but are inferred by subalternation from the universal conclusions to which the premisses directly lead. The same observation will of course apply to the subaltern moods in the other figures.

If we take no account of the conclusion, we have no means of determining which is the major and which is the minor term. Consequently, the premisses may lead to two kinds of conclusions: 1st, those in which the predicate of the first premiss is predicated of the subject of the second; 2nd, those in which the subject of the second premiss is predicated of the predicate of the first. Now the canon of the first figure applies only to the first case; consequently we are bound to ask if any conclusions, falling under the second head, may be inferred from the premisses. These cannot be determined directly by the canon, but must be determined in the same manner as conclusions in the second and third

figures. Here we proceed by a method similar to that employed in the text. The syllogistic rules exclude seven of the sixteen possible moods, viz. EE, EO, OE, OO, II, IO, OI. When the moods are referred to their several figures, we find that, where the extreme employed in the first premiss becomes the predicate, and the extreme employed in the second premiss the subject of the conclusion, the results are, in the second figure, Cesare, Camestres, Festino, Baroko; in the third, Darapti, Disamis, Datisi, Felapton, Bokardo, Ferison, the subaltern moods of the second figure EAO, AEO, being inadmissible. Where the extreme employed in the first premiss becomes the subject, and the extreme employed in the second premiss the predicate of the conclusion, the results are, in the first figure, AAI, AEO, AII, EAE, IEO, which, when we transpose the premisses, become respectively Bramantip, Fesapo, Dimaris, Camenes, and Fresison in the fourth figure. Hence, according to this mode of treatment, the moods of the fourth figure are regarded as indirect moods of the first. Similarly, in the second figure we may constitute the indirect moods AEE, EAE, IEO, OAO. These, if we transpose the premisses, are merely a repetition of the ordinary moods of the second figure. This is also the case with the indirect moods of the third figure, viz. AAI, AEO, AII, AOO, IAI, IEO. It will therefore be seen that, with the exception of rejecting the subaltern moods, which even there we regarded as superfluous, we arrive practically at the same results as in the text. The moods

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of the fourth figure are recognised, but, instead of being regarded as moods of a distinct figure, they are treated as indirect moods of the first. By the expression 'indirect moods,' it will be seen, we mean moods in which the extreme employed in the first premiss becomes the subject, and the extreme employed in the second premiss the predicate of the conclusion.



CHAPTER IV.

On Trains of Reasoning. (The Sorites.)

SYLLOGISMS may be combined in what is called a Train of Reasoning. Thus the major and minor premisses, or either, of our ultimate syllogisms may themselves be proved by syllogisms; the major and minor premisses of these, or either, by other syllogisms, and so on, till at last we come to premisses not admitting of syllogistic proof. Such premisses are either assumed without any proof at all, or they are the result either of direct observation or of the testimony of others or of Induction.

In a train of reasoning, any syllogism proving a premiss of a subsequent syllogism is called with reference to the subsequent syllogism a *Pro-Syllogism*, and the subsequent syllogism with reference to it an *Epi-Syllogism*. It is obvious that the very same syllogism in different relations may be called a Pro-Syllogism or an Epi-Syllogism.

The Sorites (or, as it is sometimes called, the chainargument) is a common instance of a train of reasoning in a compressed form. It consists, in its proper and most usual form, of a series of propositions, in which the predicate of the preceding is always the subject of the succeeding premiss. The conclusion predicates the last predicate of the first subject. Thus,—All A is B,
All B is C,
All C is D,
All D is E;
... All A is E.

When expanded, the Sorites contains as many syllogisms as there are propositions intermediate between the first proposition and the conclusion. These syllogisms are in the first figure, and the conclusion of each becomes the minor premiss of the next. Thus, the above Sorites contains three syllogisms, viz.—

- (1) All B is C, All A is B; ... All A is C.
- (2) All C is D, All A is C;
 - . . . All A is D.
- (3) All D is E, All A is D; ∴ All A is E.

In a Sorites, only one premiss can be particular, viz. the first; and only one negative, viz. the last '.

'The first premiss, if particular, may be stated in the form 'Some B is A,' instead of in the usual form 'Some A is B'; the first syllogism of the expanded Sorites will then be in the third figure instead of the first. Similarly, the last premiss, if negative, may be stated in the form 'No E is D,' instead of in the form 'No D is E,' which will

For, if there were a particular premiss in any place except the first, there would be a particular major, which, in the first figure, is inadmissible.

Again, if any premiss except the last were negative, there would be a negative conclusion in one of the previous syllogisms; this conclusion would necessitate, in the following syllogisms, a negative minor, which, in the first figure, is inadmissible.

Note.—Besides the above form of Sorites, there is another called the Regressive or Goclenian Sorites (so called from Goclenius, who first noticed it). Its properties are exactly the reverse of those of the ordinary Sorites. The subject of each premiss becomes the predicate of the next, the conclusion predicates the first predicate of the last subject, the conclusion of each of the expanded syllogisms becomes the major premiss of the next, and the rules by which it is governed are that the first premiss only can be negative and the last particular. It may be stated thus:—

All E is F,
All D is E,
All C is D,
All B is C,
All A is B;
... All A is F.

make the last syllogism of the expanded Sorites a syllogism of the second figure. No advantage, however, is gained by this mode of statement, and it is not nearly so simple as the usual form.

CHAPTER V.

On Complex (Hypothetical) Propositions and Syllogisms.

they have been inaccurately termed, Categorical 1) propositions and syllogisms. A Complex (or, as it is commonly called, a Hypothetical) Syllogism is one in which one or more complex (or hypothetical) propositions occur. A complex proposition is a combination of two or more simple propositions in one sentence, the propositions being so related that the truth or falsity of one proposition or set of propositions is made to depend on the truth or falsity of the other proposition or set of propositions. If the two propositions or sets of propositions be associated together, so that the truth of one depends on the truth of the other, the complex proposition may be called Conjunctive 2. If they be dissociated,

¹ The word categorical (κατηγορικός) properly means affirmative, and is always used in that sense by Aristotle.

I have, in accordance with more ancient usage, employed the word 'conjunctive' in place of the word 'conditional,' which is employed by Aldrich and other logicians of his time. Instead of simple and complex propositions, they speak of categorical and hypothetical, subdividing hypothetical into conditional and disjunctive. Besides the improper use of the word categorical (noticed

so that the truth of one depends on the falsity of the other, and the falsity of one on the truth of the other, the complex proposition may be called *Disjunctive*. Thus we may take as instances of Conjunctive Propositions:—

If (or When, Where, Provided that, &c.) A is B, C is D; If A is not B, C is D; If A is not B, C is not D; If A is B and C is D, E is F; If A is B, either C is D or E is F or G is H; If either A is B or C is D, E is F.

It will be noticed in the second and third examples that negatives are introduced, but they are, notwithstanding, examples of conjunctive propositions, for C being D in the first case, and C not being D in the second, are made to depend on the truth of A not being B. As instances of Disjunctive Propositions we may take the following:—

Either A is B, or C is D; Either A is B, or C is D, or E is F; A is either B or C or D; Either A or B or C is D; Either A is not B, or C is not D; Either A is B, or C is not D.

This form of proposition implies that the truth of one member involves the falsity of the other, and, vice versa, the falsity of one member the truth of the other.

It should be noticed that both conjunctive and disjunctive propositions admit of being reduced to the simple form. Thus:—

above), it is extremely awkward to make hypothetical and conditional (which are synonyms) stand respectively for the genus and species. The words conjunctive and disjunctive serve also to point out that the division of complex propositions is exhaustive.

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'If A is B, C is D' becomes 'The case of A being B is a case of C being D' or 'A being B involves as a consequence C being D.'

The disjunctive proposition, when analysed, contains four conjunctive propositions, each of which may be reduced to a simple proposition. Thus, 'Either A is B, or C is D' is equivalent to the four conjunctive propositions: If A is B, C is not D; If A is not B, C is D; If C is D, A is not B; If C is not D, A is B. Of these four propositions, however, the third is implied in the first, and the fourth in the second.

I now proceed to consider Complex Syllogisms, i. e. syllogisms which contain Complex Propositions.

§ 2. I. Conjunctive Syllogisms.

A Conjunctive Syllogism is a syllogism, one or both of whose premisses are conjunctive propositions; if only one premiss be conjunctive, the other must be simple. If both premisses be conjunctive, inasmuch as all conjunctive propositions rank as universal affirmatives, the syllogism, to be valid, must be conformed to Barbara in the first figure. Thus,

If A is B, C is D,
If C is D, E is F;
... If A is B, E is F,

is a vallid syllogism; but the following would not be valid:

If A is B, C is D,
If A is B, E is F;
... If C is D, E is F.

Far the most common form however of a conjunctive syllogism is that in which the major is a conjunctive, and the minor a simple proposition. Of this form there are four possible varieties, of which two are valid and two invalid. These may be represented thus:—

If A is B, C is D. (Major premiss.)

- (1) A is B;
 - ... C is D.

- (β) C is D;
 - No conclusion.

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- (a) A is not B;
 No conclusion.
- (2) C is not D;
 ... A is not B.

Hence we obtain the rule that, if we affirm the antecedent, we must affirm the consequent, or, if we deny the consequent, we must deny the antecedent; but, if we deny the antecedent or affirm the consequent, no conclusion can be drawn. The reason of this rule will be obvious on a little reflexion. We assert that 'A being B involves as a consequence C being D'; hence, if we grant that A is B, it must follow that C is D; if we deny that C is D, it must follow that what involves it as a consequence must also be untrue; but C might still be D, though A were not B, nor would it follow from C being D that A was also B.

Syllogism (1) is called a *Constructive* conjunctive syllogism.

Syllogism (2) is called a Destructive conjunctive syllogism.

It may be useful to add a few examples of valid conjunctive syllogisms.

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(r) If A is B, C is not D.

C is D;

(2) If A is not B, C is D.

A is not B; C is not D;

... C is D. ... A is B.

(3) If A is not B, C is not D.

A is not B; C is D; \cdot C is not D. \cdot A is B.

(4) If A is B, either C is D or F is G.

A is B; Neither C is D nor F is G;
... Either C is D or F is G. ... A is not B.

(5) If either C is D or F is G, either X is Y or V is W. Either C is D or F is G; Neither X is Y nor V is W; ∴ Either X is Y or V is W. ∴ Neither C is D nor F is G.

§ 3. II. Disjunctive Syllogisms.

A Disjunctive Syllogism is a syllogism of which the major premiss is a disjunctive, and the minor a simple proposition, the latter affirming or denying one of the alternatives stated in the former.

We may indeed combine two disjunctive propositions, and draw conclusions from them, but we can only do so after reducing the disjunctive propositions to the conjunctive form. Thus from the two propositions Either A is B or C is D, Either A is B or E is F, we may draw four conclusions, viz. If C is D, E is F; If C is not D, E is not F; If E is F, C is D; If E is not F, C is not D. But, as these conclusions are really drawn from conjunctive propositions which are involved in the two disjunctive propositions, we are not justified in calling the syllogisms disjunctive. Hence, as will be noticed, my definition of disjunctive is not so wide as that of conjunctive syllogisms.

The disjunctive syllogism admits of four conclusions, which may be exhibited thus:—

Either A is B, or C is D.

I add a few examples:---

Either A is B, or C is not D.

 (1) A is B;
 (3) C is not D;

 ∴ C is D.
 ∴ A is not B.

 (2) A is not B;
 (4) C is D.

 ∴ C is not D.
 ∴ A is B.

Either A is B, or C is D, or E is F.

- (1) A is B; ... Neither C is D nor E is F.
- (2) A is not B; ... Either C is D or E is F.
- (3) Neither C is D nor E is F; ... A is B.

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- (4) Either C is D or E is F; ... A is not B.
- (5) Either A is B or C is D; ... E is not F.

He is either a fool or a knave.

- (1) He is a fool;
 - ... He is not a knave.
- (2) He is a knave;
 - ... He is not a fool.
- (3) He is not a fool;
 - ... He is a knave.
- (4) He is not a knave;
 - ... He is a fool.

Note.-Mr. Mill (in his Examination of Sir W. Hamilton's Philosophy, ch. xxiii.) maintains that a disjunctive proposition merely implies that the two alternatives cannot both be false, but that it does not exclude the possibility of both of them being true. Thus, in the last example, he would maintain that there is nothing in the form of the assertion to exclude the supposition of the man being both a fool and a knave. In this opinion he is preceded by many other logicians, but it seems to me that in the expression 'either ---- or ---- 'we distinctly exclude the possibility of both alternatives being true, as well as of both being false. In fact, when we do not wish to exclude the possibility of both being true, we add the words 'or both,' thus: 'He is either a fool or a knave, or both'; 'I shall come either to-day or to-morrow, or perhaps both days."

§ 4. The Dilemma.

There remains the case in which one premiss of the complex syllogism is a conjunctive and the other a disjunctive proposition, it being, of course, understood that the disjunctive proposition deals only with expressions which have already occurred in the conjunctive proposition. This form is called a *Dilemma*. The order of the premisses is different, but it seems more natural that the conjunctive proposition should be the major. If we consider the case in which the major consists of one antecedent and several consequents, there is only one valid form of argument, and that is destructive.

- (1) If A is B, C is D and E is F;But either C is not D or E is not F;
 - ... A is not B.

If we asserted in the minor 'C is D and E is F' there would be no conclusion, and if we asserted 'Neither C is D nor E is F,' the minor would not be disjunctive. The assertion 'Either C is D or E is F' is, according to my view of the significance of a disjunctive proposition, equivalent to the assertion 'Either C is not D or E is not F,' and leads to the same conclusion.

If the major consist of several antecedents, and one consequent, there is only one valid form of argument, and that is constructive.

(2) If A is B or if E is F, C is D; But either A is B or E is F; ∴ C is D.

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If we asserted in the minor 'C is not D,' it would not satisfy the requirements of the definition by being a disjunctive proposition.

In the remaining case, where there are several antecedents and several consequents, there are two valid forms, one constructive and the other destructive.

- (3) If A is B, C is D; and if E is F, G is H;
 But either A is B, or E is F;
 ∴ Either C is D, or G is H.
- (4) If A is B, C is D; and if E is F, G is H;
 But either C is not D, or G is not H;
 ∴ Either A is not B, or E is not F.

It is evident that we may form a Trilemma, Tetralemma, &c., by increasing the number of antecedents or consequents or both, thus:—

If A is B, or if E is F, or if G is H, C is D; But either A is B, or E is F, or G is H; ∴ C is D.

If A is B, C is D; and if E is F, G is H; and if I is J, K is L;

But either A is B, or E is F, or I is J;

... Either C is D, or G is H, or K is L.

It is not uncommon to mistake for dilemma what is really only a conjunctive syllogism. Thus the two following syllogisms, when examined, will be found to be, the first a constructive, the second a destructive conjunctive.

 (1) Whether geometry be regarded as a mental discipline or as a practical science, it deserves to be studied;

But geometry may be regarded as both a mental discipline and a practical science;

- ... It deserves to be studied.
- (2) If we go to war, we must either contract a debt, or increase the taxation, or indemnify ourselves at the enemy's expense;

We shall not be able to do any of these;

... We are not able to go to war.

In disputation, the adversary who is refuted by a dilemma is said to be 'fixed on the horns of a dilemma'; he is said to rebut the dilemma, if he meet it by another with an opposite conclusion. Thus (to tell an old story) Protagoras the Sophist is said to have engaged with his pupil, Euathlus, that half the fee for instruction should be paid down at once, and the other half remain due till Euathlus should win his first cause. Euathlus deferred his appearance as an advocate, till Protagoras became impatient and brought him into court. The Sophist then addressed his pupil as follows: 'Most foolish young man, whatever be the decision, you must pay your money; if the judges decide in my favour, I gain my fee by the decision of the court, if in yours by our bargain.' This dilemma Euathlus rebutted by the following: 'Most sapient master, whatever be the decision, you must lose your fee; if the judges decide in my favour, you lose it

by the decision of the court; if in yours, by our bargain, for I shall not have gained my cause.'

Note 1.—Of the four cases of dilemma which I have given, the first would not be admitted by Abp. Whately and Dr. Mansel, who define dilemma as 'A syllogism having a conditional (i.e. conjunctive) major premiss with more than one antecedent, and a disjunctive minor.' Having however a disjunctive minor, it cannot properly be regarded as a conjunctive syllogism, and it seems less arbitrary and more systematic to define dilemma as 'a syllogism of which one premiss is a conjunctive and the other a disjunctive proposition' than to limit it as above.

Note 2.—Few parts of Logic have occasioned more differences of opinion or nomenclature than the theory of complex (or hypothetical) propositions and syllogisms. Sir W. Hamilton (see his Lectures on Logic, Lecture xiii. and Appendix viii.) finally arrives at the opinion that 'hypothetical and disjunctive judgments' are not more complex than ordinary propositions, and that 'hypothetical and disjunctive reasonings' are really forms of immediate inference. Thus he would represent the conjunctive syllogism in the form:—

If A is B, C is D;
... A being B, C is D.

The disjunctive syllogism he would represent in the form:—

Either A is B, or C is D; ... A not being B, C is D.

The other inferences from the premisses would, of course, be drawn similarly.

The dilemma would assume the form:---

If A is B, C is D; and if E is F, G is H;

- ... Either A being B, or E being F, it follows that C is D, or G is H;
- or ... Either C not being D, or G not being H, it follows that either A is not B, or E is not F.

Without attempting to discuss the arguments that have been adduced on either side, I may express my own opinion that complex (or hypothetical) propositions and syllogisms are rightly so called, and that the latter are to be regarded as mediate, and not as immediate, forms of inference. Though no new term is introduced in the minor premiss, the major and minor premisses are entirely distinct propositions, and the conclusion is the result not of one proposition but of two propositions taken conjointly.



CHAPTER VI.

On the words 'Most,' 'Many,' &c., as expressing the Quantity of Propositions.

TO all particular propositions I have hitherto prefixed the word 'some.' Both in conversation and reasoning, however, it frequently happens that we use some other sign of particularity, such as 'many,' 'most,' &c. Nor does there seem any valid reason why these forms should not be recognised by Logic. From what has already been said of particular premisses, it will be seen that wherever one premiss is universal and the other modified by some sign of particularity, as 'some,' 'many,' 'most,'&c., the conclusion must be particular, the degree of particularity in no case transcending (though, in some cases, it may fall below) that denoted by the particular premiss. we state as our premisses 'All crimes are to be punished,' 'Many offences against individual persons are crimes,' we must draw the conclusion that 'Many offences against individual persons are to be punished.' But if we state as our premisses 'All crimes are to be punished,' 'Most crimes are offences against individuals,' we are only justified in drawing the conclusion that 'Some offences against individuals are to be punished.' The student will, from the principles already laid down, be easily able to distinguish between the two classes of cases.

'Two particular premisses prove nothing.' This is a general rule, and is strictly true where the premisses are quantified as 'some'——'some.' But there is one case in which two particular premisses necessitate a conclusion. I will begin with a simple instance of it. If two different predicates can both be predicated affirmatively of the greater number of individuals denoted by the same common term, there must be some individuals of which they can both be predicated, i. e. in certain cases the predicates must be predicable of each other. Thus, from the premisses

Most A are B, Most A are C,

we must necessarily infer that Some A is both B and C, and consequently that Some B are C and Some C are B.

But we may draw the same conclusion, even in those cases in which both premisses are not quantified by the word 'most,' provided that the sum of the quantities by which the subjects are affected exceeds unity. Thus from the premisses

Three-fourths of A are B, One-third of A is C,

it follows that at least one-twelfth of A is both B and C; but if B and C be both predicable of the same objects, either must be, partially, predicable of the other. If, for instance, three men out of four exceed a certain height and one out of three a certain weight, at least one out of twelve must exceed both the given height and the given weight, and we may affirm both that Some men who exceed a certain height also exceed a certain weight, and that Some men who exceed a certain weight also exceed a certain height.

Of course, when we use such an indefinite word as 'most' in either premiss, the other premiss must be quantified by an expression signifying at least one-half; else we cannot be sure that the quantities of the two premisses, when added together, exceed unity.

A conclusion of this kind can only be drawn where the subject in both premisses is the same term, i.e. in the third figure; for, in the mere form of a logical proposition, we have no data to guide us with regard to the quantity of the predicate. Thus, from the premisses

> Nineteen-twentieths of A are B, Nine-tenths of B are C,

we can draw no conclusion as to the relation of A and C; for the tenth of B which is not C might be precisely that portion which was coincident with, or which contained, the nineteen-twentieths of A. Though, however, these syllogisms are confined to the third figure, they may be either affirmative or negative. Thus, from the premisses

Three-fourths of A are not B,

Two-thirds of A are C,

we may infer that five-twelfths at least of A are C and not B, and consequently that some C is not B, and some things which are not B are C.

Note.—The propositions employed in the above chapter have usually been regarded as Particulars, though they have sometimes been classed with Universals. See Sir W. Hamilton's Lectures on Logic, vol. ii., first ed. p. 354; second ed. p. 361.



CHAPTER VII.

On Probable Reasoning.

IN discussing the copula, it was maintained that any modification of our assertions, such as the qualifications introduced by the words 'probably,' 'possibly,' &c., was, in the ultimate analysis of the proposition, to be referred to the predicate and not to the copula. Thus such a proposition as 'A is probably B,' when stated in its strictly logical form, would become 'That A is B is a probability.' It would however be tedious and practically useless to reduce all our propositions to such a form. I may therefore proceed to lay down rules for reasoning from propositions whose copula is modified, remembering however that they are not stated in strictly logical language.

The correctness of the following rule will be apparent. If a premiss whose copula is modified be combined with another premiss whose copula is unmodified, the copula of the conclusion must be modified also; the modality, of course, never transcending that of the premiss. Thus from the premisses 'All true poets are men of genius,' 'Sophocles is probably (certainly, possibly, &c.) a true poet,' I infer that Sophocles is probably (certainly, possibly, &c.) a man of genius. From a certain and a

probable premiss, therefore, arranged according to the ordinary laws of syllogism, we can never infer more than a probable conclusion. To this head may most conveniently be referred those syllogisms in which the major is a particular proposition introduced by the word 'most,' and the minor a singular proposition. Thus from the premisses, 'Most philosophers are men of vivid imagination,' 'A B is a philosopher,' I infer, as the conclusion, A B is probably a man of vivid imagination. If most philosophers possess certain characteristics, any particular philosopher will probably possess them, so that the major premiss is, in fact, equivalent to the proposition, 'A philosopher is probably a man of vivid imagination.'

Using the word 'probable' in the sense of 'more likely than not,' two probable premisses do not lead to a probable conclusion. This fact will be obvious from an easy example. Suppose there are in a bag four red, five blue, and six white balls: I may say with truth 'Any ball drawn at random from the bag is probably a red or blue ball'; I may also say with truth 'Any ball drawn at random from the red and blue balls is probably a blue ball'; but I cannot infer that 'Any ball drawn at random from the bag is probably a blue ball.' I shall only be justified in drawing the conclusion 'Any ball drawn at random from the bag is possibly a blue ball.' But, where our information is so special as in the above instance, a conclusion of this kind is far too vague. there no method which will enable me to state in the conclusion the exact value of the expectation that any

particular ball drawn at random may be blue, red, or white? For such a method I must have recourse to mathematics.

Though the word 'probable' is used in the sense of 'more likely than not,' the word probability is used as the equivalent of 'chance' or 'expectation.' If it be three to two that a certain event will happen, 3:2 is called the odds for, 2:3 the odds against the event. Now the 'probability' or 'chance' of the event happening would be expressed by \$, that of its not happening by \$, the denominator in both cases being expressed by the sum of the terms of the odds, the numerator in the first case by the term of the odds for, in the latter case by the term of the odds against. If two events are independent of each other, the joint or compound probability that they will both happen must be much smaller than the probability that either of them will happen alone, and it is discovered by multiplying together the fractions which express the probabilities of their happening separately1. Thus, in the above instance, the chance of my drawing a red or blue ball $=\frac{9}{18}$; the chance of my drawing out of the red and blue balls a blue ball = \ : ... the chance of my drawing a blue ball out of a bag which contains all = $\frac{9}{18} \times \frac{5}{9} = \frac{3}{8}$, a result at which, in this particular instance, I could of course have arrived more directly. Hence, when both premisses are affected by words like 'probably,' 'possibly,' &c., the probability of the conclusion

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¹ The truth of this proposition, with regard to two, three, or any number of events, is proved at length in Peacock's *Arithmetical Algebra*, § 469.

may always be discovered by multiplying together the probabilities of the premisses, the conclusion being therefore less probable than either premiss. I append a few instances of conclusions drawn from probable premisses:—

- (1) This plant will probably sprout up during the winter months. (Let the probability = \frac{3}{5}.)
 - Whatever plant sprouts up during the winter will probably be bitten by the frost. (Let the probability = ‡.)
 - ... This plant may sprout up and be frost-bitten. (Here the probability = $\frac{2}{3} \times \frac{4}{3} = \frac{12}{3}$.)
 - ... The odds against the event are 23 to 12, and those in favour of it 12 to 23.
- (2) Two thirds of these men will be enlisted. Half the men enlisted are killed in battle.
 - ... The probability of any particular man being enlisted and killed in battle = $\frac{3}{5} \times \frac{1}{2} = \frac{1}{8}$.
 - ...It is two to one against any particular man here being enlisted and killed in battle.
- (3) A warm day may possibly be a rainy day. (Let the probability = ⅓.)
 - A rainy day is probably a calm day. (Let the probability = \{\frac{1}{2}}.)
- ... A warm day may possibly be both rainy and calm³.
 (The probability = ⁴₅.)
- * I am indebted to Professor Shaw, of Derry, for pointing out an inaccuracy in the conclusion of this example, as stated in the earlier editions, and to Professor Park for the suggestion that it is a peculiarity of all arguments of this kind that, strictly speaking, both premises should be expressed in the conclusion.

N. B.—It is most important for the student to bear in mind the ambiguous use of the words 'probably,' 'probable,' 'probability.' The adverb 'probably' we seem always to use in the sense of 'more likely than not.' The adjective 'probable,' when employed as a predicate, seems also to be invariably used in the same sense; thus we say 'It is probable that he will do so and so,' 'This event is probable.' But when used to qualify a substantive, as in such expressions 'probable premisses,' 'probable reasonings,' &c., it may be employed either in the above sense or simply as contrasted with certainty, and in the latter case the 'probability,' as we say, may vary from certainty to zero. Lastly, the word 'probability' may simply be equivalent to 'chance,' as explained above, or in some expressions it may have the meaning of 'being more likely than not,' as when we say 'The probability is that he will do so and so.' By 'probable reasoning' at the head of this section I of course mean reasoning which falls short of certainty, and the value of which may vary to any extent so long as it does not rise to certainty or fall to zero.

On the Combination of Probable Arguments.

[Cumulative or Corroborative Evidence, including Circumstantial Evidence.]

Probable arguments may be combined together in a chain a (or, as it has been more appropriately called, a coil) of reasoning, each argument leading to the same conclusion. Instead of weakening each other, as is the case with probable premisses, such arguments, being all independent testimonies to the truth of the same conclusion, mutually strengthen each other. If the value of any single argument amounts to certainty, the conclusion must be true. In this case therefore we have to calculate the chances of failure in each separate argument; these, when multiplied together, give the probability of all the arguments together failing to prove the conclusion; and this fraction, when subtracted from unity (which represents certainty), gives the probability, resulting from all the arguments jointly, in favour of the conclusion. suppose the probabilities in favour of certain probable arguments to be represented respectively by 1, 2, 2;

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^{*} Chain-reasoning would be the proper designation for a series of arguments (or links of evidence) which are all inter-dependent, so that, if one argument fails (or one link snaps), the reasoning breaks down altogether. Much legal evidence is of this kind, as when A testifies that he received a certain parcel from B, B that he received it from C, and so on. In this case, any one untrustworthy witness would invalidate the whole evidence. On the other hand, in corroborative evidence the various parts strengthen one another.

the chances of their failing to prove the conclusion will be represented respectively by $\frac{3}{3}$, $\frac{1}{6}$, $\frac{1}{4}$ (or the differences between the favourable chances and unity); the chance therefore of their all failing to prove the conclusion $=\frac{3}{3}\times\frac{1}{6}\times\frac{1}{4}=\frac{1}{30}$; consequently the probability in favour of the conclusion, as based upon all the arguments jointly, is $\frac{1}{80}$, i. e. the odds in favour of it are 29 to 1.

I may illustrate this case by an example, which will also serve to shew the characteristic uncertainty attaching to this method of reasoning. Suppose a man to be found lying dead on a road from the effects of a wound. On the same evening on which he died, another man was seen running away from the neighbourhood of the place. On this man's house being searched, his clothes are found to be stained with blood; his footsteps correspond with those leading to and from the place where the dead man was lying; and moreover he is known to have possessed a weapon, now not to be found, which was capable of inflicting the wounds. The presumption in favour of his guilt is very great; each argument, taken alone, possesses some cogency, and when all the arguments are taken together they appear to be irresistible. But suppose the suspected man, when arrested, to give this account of the affair: he was walking along the road, armed with a dagger; he was suddenly attacked by another man; a scuffle ensued, and in the scuffle he killed his assailant; finding that he had killed him, he was seized with a sudden panic, threw away his weapon, and ran home. Such an account, in the case

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of a timid and secretive man, might possibly be true, and, in estimating the counter-probabilities, we should have to consider the characters of the accused and the dead man, and the nature of the motive, if any, which could have led to the supposed crime. Suppose the dead man's pockets were rifled, and the accused (who had been previously convicted of a felony) were in possession of his money, there could be little doubt that he had committed a murder; but suppose that the character of the accused was good, and no likely motive could be assigned for the commission of the crime, his own version of the affair might be accepted as probably true, or at least as throwing considerable doubt on the supposition of his guilt.

- * As illustrating the danger of exaggerating the value to be attached to this kind of evidence, I could hardly adduce a more forcible example than the following passage from Lord Coke (quoted by Bentham' in his Rationale of Judicial Evidence, Bk. V. ch. xv. § 2):—
- 'Violenta presumptio is many times plena probatio; as if one be run thorow the bodie with a sword in a house, whereof he instantly dieth, and a man is seen to come out of that house with a bloody sword, and no other man was at that time in the house.'

To this Bentham replies by two counter-suppositions:-

- '1. The deceased plunged the sword into his own body, as in the case of suicide; the accused, not being in time to prevent him, drew out the sword, and so ran out, through confusion of mind, for chirurgical assistance.
- '2. The deceased and the accused both wore swords. The deceased, in a fit of passion, attacked the accused. The accused, being close to the wall, had no retreat, and had just time enough to draw his sword, in the hope of keeping off the deceased; the deceased, not seeing the sword in time, ran upon it, and so was killed.
 - Other suppositions might be started besides these; nor do these

The commonest example of evidence of this kind (which may be called Cumulative or Corroborative Evidence) is Circumstantial Evidence, so called from the fact that

exculpative ones either of them seem in any considerable degree less probable than that criminative one: if so, the probability of delinquency, instead of being conclusive, is but as 1 to 2.

Sometimes the individual arguments in evidence of this kind are of so little value that, even when several of them are accumulated, they have no practical force. 'Presumptio probabilis,' Lord Coke says rightly, 'moveth but little, but presumptio levis sen temeraria moveth not at all.'

On the other hand, the force of this evidence may amount to that of moral certainty. 'If,' says Mr. Wills, 'it be proved that a party charged with crime has been placed in circumstances which commonly operate as inducements to commit the act in question,that he has so far yielded to the operation of those inducements as to have manifested the disposition to commit the particular crime; -that he has possessed the requisite means and opportunities of effecting the object of his wishes,-that recently after the commission of the act he has become possessed of the fruits or other consequential advantages of the crime,—if he be identified with the corpus delicti by any conclusive mechanical circumstances, as by the impressions of his footsteps, or the discovery of any article of his apparel or property at or near the scene of the crime, -if there be relevant appearances of suspicion, connected with his conduct, person, or dress, and such as he might reasonably be presumed to be able, if innocent, to account for, but which, nevertheless, he cannot or will not explain,-if, being put upon his defence recently after the crime, under strong circumstances of adverse presumption, he cannot shew where he was at the time of its commission,-if he attempt to evade the force of those circumstances of presumption by false or incredible pretences, or by endeavours to evade or pervert the course of justice,-the concurrence of all or many of these cogent circumstances, inconsistent with the supposition of his innocence and unopposed by facts leading to a counter-presumption, naturally, reasonably, and satisfactorily establishes the moral certainty of his

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several circumstances are adduced as all supporting the same conclusion. It will be readily seen that the utmost caution is required in estimating its value. We are bound to consider not only the circumstances which point to the conclusion, but also those which make against it, or in favour of any counter-supposition. It is only when we feel certain that we have exhausted all possible suppositions, consistent with the circumstances of the case, and considered carefully the value of the arguments, or series of arguments, pointing to each of them, that we are entitled to pronounce with confidence in favour of any particular conclusion.

Any single syllogism in a coil of circumstantial evidence may be represented as an argument with one probable and one certain premiss, thus:

A man who was seen running away, in order to escape observation, from the place where the dead man was lying, immediately after his death, was probably the murderer,

This man was seen running away, &c.;

... He was probably the murderer.

The major premiss of each of these syllogisms is the result of an analogical argument; and its value must be estimated according to the rules of analogy, already explained.

guilt,—if not with the same kind of assurance as if he had been seen to commit the deed, at least with all the assurance which the nature of the case and the vast majority of human actions admit.' Wills on Circumstantial Evidence, 4th ed., pp. 276, 7.

Note 1.—It is more usual to regard the separate syllogisms in a coil of circumstantial evidence as syllogisms in the second figure, involving an undistributed middle, and justifying a probable conclusion. Thus the above syllogism would be represented in the form:

The murderer would, to escape observation, run away, &c.,

This man, to escape observation, ran away, &c.;

It seems however extremely awkward to represent such reasonings as fallacies, and then, by way of compensation, to regard them as probable arguments. This mode of treatment, no doubt, originated in the desire to conform the arguments in circumstantial evidence to those Enthymematic syllogisms of Aristotle which employ the onusion in the second figure. For an account of the Enthymeme and its subdivisions, the student is referred to Trendelenburg's Elements, § 37, and Dr. Mansel's Appendix to Aldrich, Note F.

Note 2.—There are some cases, as, for instance, those in which the witnesses may be suspected of lying, or in which they are actuated by violent passions, where circumstantial evidence may be of far greater value than direct evidence. See some remarks on this subject in an article contributed to the Fortnightly Review for January, 1873, by Sir H. Maine, and since reprinted at the end of Village Communities. On circumstantial evidence, generally, the student would do well to consult Sir Fitzjames Stephen's Introduction to the Indian Evidence Act, Wills

on Circumstantial Evidence, and Taylor's Treatise on the Law of Evidence, Pt. I. ch. 4. In Direct Evidence, the witness testifies to the precise fact alleged; in Indirect or Circumstantial Evidence to some fact or facts indicative of the fact alleged. The rules for estimating the logical value of circumstantial evidence apply also to direct evidence in all those cases in which we have any reason for questioning either the veracity or the competence of the principal witness, and in which, therefore, his evidence requires corroboration from independent testimony.

The work of Mr. Wills is exceedingly interesting and instructive;
 but the reader must be on his guard against an erroneous statement
 on the mathematical value of a coil of circumstantial evidence.

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CHAPTER VIII.

On Fallacies.

- § 1. A FALLACY is, strictly speaking, a defective inference, but the word is, by common usage, extended to any error either in the premisses or in the conclusions of our arguments. In deductive Logic (for we are not here concerned with the fallacies incident to induction ¹
- ¹ The fallacy of False Analogy (which consists either in overestimating, in some particular case, the value of the argument from analogy, or in supposing an analogy where none exists) falls properly within the domain of Inductive Logic, and is discussed in the author's 'Elements of Inductive Logic,' ch. vi. It is not to be confounded with the fallacy arising from the employment in a syllogism of a word used analogously, as if it were used univocally, which, as already noticed, is one case of the fallacy of ambiguous terms. Thus to argue, because there are certain points of resemblance between the development of the individual and the development of the race, that, therefore, since the individual dies, the race will probably die also, or, because there are certain points of resemblance between the earth and the other planets, that, therefore, the other planets are certainly, or very probably, inhabited, would both be instances of false analogy, the former being the assumption of an analogy which appears to have no existence, the latter being an exaggeration of the value, in that particular case, of the probable argument. But to argue, because art (i.e. artistic skill) requires the highest intellectual gifts, and dissimulation is art (i.e. deceit), that, therefore, dissimulation requires the highest intellectual gifts, is obviously a mere play upon words, and owes its semblance of reasoning simply to the ambiguity of language.

or to the operation subsidiary to it, observation) these errors are traceable to one of four sources: the assumption of a false premiss, neglect of the laws of deductive inference, irrelevancy, and ambiguity of language. Any conclusions, therefore, or series of conclusions, which transgress no law of inference, which are derived from true premisses, which are relevant to the matter under discussion, and which, with their premisses, are expressed in unambiguous language, may be regarded as faultless.

§ 2. I. A false premiss, borrowed from some science which is not under investigation, can only be detected by a special knowledge of the science from which it is taken. Many fallacies, described in the old books on Logic, are really instances of the assumption of a false premiss, and therefore specially concern other sciences rather than logic. Thus the celebrated fallacy of Achilles and the tortoise (see p. 175) rests upon a false assumption, viz. that when the distances between the two become infinitesimal they will be traversed by Achilles in finite and equal (and not, as will actually be the case, in infinitesimal and rapidly diminishing) times.

The phrase 'False Analogy' is also applied to a perversion of the Analogy of Aristotle (see p. 72); namely, to those cases in which the conclusion is based upon relations wherein the two sets of terms compared do not agree. Thus, though, in many respects, the relation of a king to his subjects is the same as that of a father to his children, it is plain that invalid conclusions might be based on this general relation, by extending it to points in which it does not subsist. Such invalid conclusions would be called 'False Analogies.'

§ 3. II. The fallacies due to the neglect of the laws of deductive inference (which, strictly speaking, are the only fallacies to be detected by a mere knowledge of Deductive Logic) have already, to some extent, been discussed. The principal sources of fallacy in a single inference are illicit process and undistributed middle.

Undistributed middle often occurs in the following form:

All Conservatives (or Liberals, Roman Catholics, Protestants, Englishmen, Frenchmen, &c.) hold such and such opinions, do such and such things, or possess such and such characteristics;

A B holds such and such opinions, does such and such things, or possesses such and such characteristics;

... A B is a Conservative (Liberal, Roman Catholic, &c.). We might, of course, argue quite as legitimately that, because both men and cats are animals, all men are cats. If, however, the argument assumed this shape,—

None but Liberals (Roman Catholics, &c.) hold such and such opinions, or do such and such things;

This man holds such and such opinions, or does such and such things;

... He is a Liberal (Roman Catholic, &c.), it would be perfectly legitimate.

The major premiss in this case (see p. 83) is equivalent to the proposition 'All men who hold such and such opinions, or do such and such things, are Liberals (Roman Catholics, &c.).' As was shewn in the Chapter on Probament of the following kind: 'A man who holds such and such opinions, or does such and such things, is probably a Liberal (Roman Catholic, &c.); this man holds such and such opinions, or does such and such things; therefore he is probably a Liberal (Roman Catholic, &c.).'

Of Illicit Process the following syllogisms may serve as examples:

No form of democracy excludes the great mass of the people from political power,

Any form of government which excludes the great mass of the people from political power is subject to violent revolutions;

... No form of democracy is subject to violent revolutions.

The early history of some nations is full of incredible events,

A history which is full of incredible events is not worthy of serious study;

... The early history of any nation is not worthy of serious study.

The former syllogism (AEE in the first figure) involves illicit process of the major, the latter (EIE in the first figure) illicit process of the minor. It will be observed that the various propositions are not stated in strictly logical form, though they easily admit of being so stated, and the premisses of both syllogisms require to be transposed.

Where there is a long train of reasoning in which one

syllogism is employed to prove the premiss of another, and so on, a fallacy frequently occurs, which often escapes detection. This is called the Argument in a Circle. A book is written, or a speech is made, with the object of proving some controverted opinion. The author or speaker, being full of one idea, after a little preliminary matter, assumes the proposition to be proved, slightly disguised, probably, under some equivalent form; from this proposition he deduces various conclusions, and these conclusions, when put together, of course triumphantly establish, from various sides, his view of the controversy. This is not an unfair analysis of many elaborate arguments, the fallacy being, in the great majority of instances, undesigned, and imposing on the author or speaker himself quite as much as on his readers or hearers. The fallacy, when expressed in its naked form, may be described as the assumption, in a train of reasoning, of the conclusion of a subsequent syllogism as a premiss of a precedent syllogism. It may be represented thus:-

Thus, when asked why B is A, we reply, because C is A; and when asked why C is A, we reply, because B is A.

Of course, in actual argument, hundreds of intermediate syllogisms might occur between syll. (1) and syll. (2). The larger the number of intermediate steps, the more likely is the fallacy to escape detection, and, conversely,

the true mode of exposing the fallacy, as Whately observes, is to narrow the circle by cutting out the intermediate steps, and exhibiting the assumption of the conclusion in its naked form. The fallacy is to be regarded as a breach of the laws of inference, because, when reduced to its simplest terms, it is a proving of the conclusion by means of itself, instead of by means of premisses which jointly necessitate it. But, unlike the fallacies of illicit process, &c., already treated, it cannot be detected from the inspection of a single syllogism, but requires the comparison of two syllogisms or more.

The argument in a circle is the most important case of the fallacy called *Petitio Principii* (or, as it is more properly called, *Petitio Quasiti*, *begging the question*). The other cases of petitio principii generally enumerated, though the enumeration is by no means exhaustive, are (2) when the conclusion simply re-asserts a premiss of the same syllogism², (3) when it is exactly synonymous with³

If a syllogism, in which one of the simpler forms of petitio principii occurs, were stated at length, one of the premisses would be otione (i.e. would not contribute towards the conclusion), but, as already noticed, in our reasonings, as actually expressed, we generally suppress one of the premisses.

^{*} The English language, says Archbishop Whately (Elements of Logic, Bk. III. § 13), 'is perhaps the more suitable for the fallacy of petitio principii, from its being formed from two distinct languages, and thus abounding in synonymous expressions which have no resemblance in sound and no connexion in etymology; so that a sophist may bring forward a proposition expressed in words of Saxon origin, and give as a reason for it the very same proposition stated in words of Norman origin; s.g. "to allow every man an unbounded

one of the premisses, (4) when one of the premisses is equally unknown with the conclusion, (5) when it is more unknown. Cases (4) and (5) are really instances of the assumption of a false premiss, or at least of a premiss which is not known to be true. Cases (2) and (3) arise from a neglect of the laws of syllogism, for, instead of proving the conclusion from the two premisses jointly, we simply re-assert one of the premisses 4.

Connected with this fallacy is the rhetorical device of question-begging epithets. Thus, though the matter we are discussing is open to dispute, we may speak of a nefarious project, a laudable ambition, an astute act, a farsighted policy, and so on, attempting, by means of a carefully-selected epithet, to assume the point at issue, or at least to create an unfair prejudice in the mind of the hearer or reader whom we address.

freedom of speech must always be, on the whole, advantageous to the State; for it is highly conducive to the interests of the community that each individual should enjoy a liberty, perfectly unlimited, of expressing his sentiments."

It has sometimes been maintained that every syllogism is a petitio principii. Of course the controversy entirely turns upon the meaning of the terms, but, according to the account I have given of the two, a syllogism is so far from being a petitio principii, that every petitio principii is a distinct breach of the laws of syllogism. The conclusion of a syllogism is indeed implied by the two premisses taken in combination, and is, in fact, the compression into a single proposition of what, as premisses, were two distinct propositions, but, in a petitio principii, the conclusion is merely a re-assertion of one of the premisses; in the simpler cases, of a premiss in the same syllogism; in the argument in a circle, of a premiss in one of the preceding syllogisms of the series.

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§ 4. III. The fallacy of Irrelevancy (or, as it is sometimes called, shifting ground) is technically termed Ignoratio Elenchi, i. e. ignorance of the syllogism required for the refutation of an adversary. Thus, in the strictest sense of the words, ignoratio elenchi is committed by a person who in a disputation does not confine himself to proving the contradictory or contrary of his adversary's assertion, or who proves a proposition other than the contradictory or contrary. But, like many other terms borrowed from the dialectical disputations of the ancients, this has now received a wider meaning. Whenever an argument is irrelevant to the object which a speaker or writer professes to have in view, it is called an ignoratio elenchi. Thus, if I am endeavouring to convince a person that some particular measure is for his personal interest, and I adduce arguments to prove that it contributes to the general utility, or that it is the necessary consequence of other acts of legislation, I am guilty of an ignoratio elenchi, as I should also be if, when it was my object to establish either of the other two conclusions, I were to appeal to his personal interest. When the question at issue is the truth of an opinion, it is an ignoratio elenchi to attack it for its novelty, or for its coming from a foreign source, or for any supposed consequences which may result from it, or to try to throw discredit on its author by saying that it has often been started before, and so is no discovery of his.

This fallacy is more common in spoken addresses than in books, as the feelings both of speaker and hearers

being more excited, and their judgment less critical, they are less likely to insist on relevancy of argument. On such occasions it most commonly takes the form of an argumentum ad hominem, whereby the speaker, in support of the truth of his assertions, or to throw discredit on an adversary, appeals, not to the unbiassed judgment of his auditors, but to their passions, interests, prejudices, sentiments and associations. The argumentum ad hominem, however, is not confined to set speeches; it sometimes occurs in writings, and frequently in debates. In the latter, it often assumes the shape of an appeal to the previous acts, or the previously expressed convictions of the opponent; 'That measure, or that argument, or that proposal does not come well from you, who once proposed such a measure, or expressed such an opinion, or advanced such an argument, or did such and such acts.' There are occasions when the argumentum ad hominem may legitimately be used as a retort, but it must be advanced as such, and not as an argument. It is so called in opposition to the argumentum ad rem or ad judicium. Similar phrases are used to express other forms of the ignoratio elenchi, as e.g. the argumentum ad verecundiam, argumentum ad baculum, &c. The argumentum ad populum I have treated as identical with the argumentum ad hominem; if called on to distinguish them, which seems unnecessary, I should refer the first to addresses made in the presence of a large auditory, the second to disputations with one or a few individuals.

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⁵ The student will find some amusing examples of ignoratio

§ 5. IV. The fallacy originating in ambiguity of language I noticed when warning the student against the employment of equivocal terms. This fallacy (whether we call it that of equivocal terms, of ambiguous terms, or of ambiguity of language) of course includes fallacies arising from any ambiguity which may attach to the quantity of the subject, as e.g. the fallacy arising from the ambiguous use of the word 'all,' which will be noticed below.

I now proceed to notice one or two common cases of this fallacy. The same term may often be used in one place distributively and in another collectively, and we may argue as if the term in both places had the same meaning. This is called the fallacy of Composition or Division; of composition, if we argue from a term taken distributively as if it were taken collectively; of division, if we argue from a term taken collectively as if it were taken distributively. Thus (to give common instances) 7 and 2 are (distributively) odd and even, nine is 7 and 2 (collectively); ... nine is odd and even. Here we argue from 7 and 2 taken distributively, as if they had been taken collectively, and the fallacy is one of composition. Five is one number, 3 and 2 (collectively) are five; ... 3 and 2 (distributively) are one number. Here the fallacy is one of division. Again, The people of England have a prejudice against the French, he is one of the people of England; ... he has a prejudice elenchi, or irrelevant argument, in Sydney Smith's well-known jeu d'esprit, the Noodle's Oration.

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against the French. The major premiss might be quite true, and still the particular man spoken of might have a strong sympathy with the French, and be a warm admirer of their institutions. Here we argue from the term 'people,' taken collectively, as if it had a distributive signification and whatever were predicable of the English people might be predicated of every single individual amongst them; hence the fallacy is one of division. The last instance is an example of a very common source of deception. A certain people, corporation, or society, in its collective capacity, has certain characteristics, has performed certain acts, passed certain resolutions, or is known to have expressed certain sentiments; hence it is unreflectingly supposed that any particular individual belonging to the class has the same characteristics, participates in the same sentiments, and has joined in the same acts. In many cases, of course, he may be a strong dissentient, and may have actively opposed the measures adopted.

The ambiguous use of the word 'all' furnishes a good instance of the fallacies of composition and division. We may argue from 'all,' meaning all taken together, as if it meant all severally, and thus commit the fallacy of division; or from 'all,' meaning all severally, as if it meant all taken together, and thus commit the fallacy of composition. Thus, when I say, 'All these boxes weigh so much,' or 'All these men can eat so much,' I leave it doubtful whether I mean all taken together or all taken severally. The ambiguity may be removed by substituting

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for the word 'all,' when used in a distributive sense, 'every,' and, when used in a collective sense, 'the whole of.'

Another pair of fallacies which falls under the head of 'ambiguous terms' is the pair known as the Fallacia Accidentis (or the Fallacia a dicto simpliciter ad dictum secundum quid) and the Fallacia a dicto secundum quid ad dictum simpliciter. In the first we argue from what is true as a general rule (i. e. unless there be some modifying circumstances) as if it were true under all circumstances; in the second from what is true under certain special circumstances as if it were true as a general rule. Thus a particular walk may be an agreeable one, but it does not follow that it would be so in wet or windy weather; plain-speaking, frugality, generosity, may all be virtues, but it does not follow that it would be virtuous to practise them on all possible occasions. Or, to take instances of the second fallacy, a political revolution may, under particular circumstances, be necessary to the welfare or existence of a country, but it does not follow that a state of society, in which political revolutions are frequent, is either necessary or desirable; it may be necessary if I am suffering from a particular disease that I should take opium or abstain from labour, but it does not follow that these practices would be good for me when I am restored to health. The fallacies are due to our not sufficiently qualifying the terms which we use, and, by insisting on precision of language, they may always be avoided.

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Though the definitions I have given of this pair of fallacies are conformable to the usage of most modern logicians, and are stated in a form which is most likely to be of practical service to the student, they do not exactly correspond with the original meaning of the expressions. The 'Fallacia Accidentis' and the 'Fallacia a dicto secundum quid ad dictum simpliciter,' according to their original usage, applied to those cases in which a term, when not implying accidents, was confounded with the same term, when implying accidents. Thus, to take the common instance (which is sufficiently absurd): 'What you buy in the market you eat; raw meat is what you buy in the market; ... raw meat is what you eat.' Here it may be replied that what we buy in the market we do indeed eat, but not necessarily in the same state in which we buy it at market 7. This particular instance is an

^{*} As, for instance, Mill (Logic, Bk. V. ch. vi. § 4), Port Royal Logic (Part III. ch. xix. § 5, 7). The latter virtually treats both fallacies as if they were a dicto secundum quid ad dictum simpliciter.

¹ Mr. de Morgan adduces one of Boccaccio's stories as affording an amusing instance of the fallacia accidentis. It is the old example of the 'raw meat' in another form:—

^{. &#}x27;A servant who was rousting a stork for his master was prevailed upon by his sweetheart to cut off a leg for her to eat. When the bird came upon table, the master desired to know what was become of the other leg. The man answered that storks had never more than one leg. The master, very angry, but determined to strike his servant dumb before he punished him, took him next day into the fields where they saw storks, standing each on one leg, as storks do. The servant turned triumphantly to his master, on which the latter shouted, and the birds put down their other legs and flew away. "Ah, sir," said the servant, "you did not shout to the stork at dinner

example of the Fallacia Accidentis. From their technical meaning, these fallacies would easily pass into their present signification, which is both more intelligible and of greater practical service.

I may notice one more example of the errors due to ambiguous language, viz. the fallacy of what may be called Paronymous Terms. The same word may often assume different forms, as substantive, adjective, adverb, or verb, but it does not follow, when it has assumed these different forms, that they all retain corresponding meanings. It has been already noticed that the words probably, probable, probability, though the two last are themselves ambiguous, vary in meaning according as we use the adverb, the adjective, or the substantive. Thus, if I hear some one ask the question 'What is the probability of my throwing an ace with a die at a single throw?' I cannot infer that in any single throw I shall probably throw an ace. Again, because a man has done something unjust (i.e. has committed an act which in its results is unjust), I cannot infer that he has acted unjustly (i.e. with intentional injustice), nor, even if he has acted unjustly (i.e. in one or more instances), can I infer that he is an unjust man (i.e. a man of unjust habits or character). To take an old instance, because projectors are unfit to be trusted, and this man has formed a project, it does not follow that he is unfit to be trusted. Nor from the meaning attached to the expressions, kingly, yesterday: if you had done so, he would have shewn his other leg too.***

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nobly, gentlemanly, can we argue to the usual qualities of a king, a nobleman, or a gentleman; nor, on the meanings of the words 'to trow,' 'to represent,' can we base any sound argument as to the nature of truth, or the duties of a representative. All instances of this fallacy, when stated syllogistically, involve four terms, and so offend against the rules for the construction of a syllogism, but, as we do not ordinarily state our arguments in a syllogistic shape, and these fallacies undoubtedly impose on us through the ambiguity of language, it is better to consider them here rather than under the second head.

Many other forms of fallacy may be regarded as due to ambiguities of language, but it has perhaps been the tendency of modern logicians, and especially of Whately, to overload this division of fallacies, and to treat as merely differences of language what are in reality radical differences of opinion. At the same time it cannot be denied that terms expressive of fundamental conceptions in their several sciences, such as faith, church, election, law, loyalty, federation, justice, value, capital force, nature, natural, &c., are frequently used, in the same discussion, in the most widely divergent senses, and are consequently the source of endless confusion in our reasonings. Thus the term 'faith' may mean either a belief in certain propositions, or confidence, trust, and repose in a certain person; the word 'church' may mean the whole body of Christians (and, of course, in this sense its signification will vary according to the meaning attached to the term Christian), a

particular section of Christians, a congregation meeting in a certain place, the place of meeting, and, lastly, by a strange perversion of the term, the clergy as distinguished from the laity; the term 'loyalty' may mean either attachment to the laws of a country in general, special attachment to some particular portion of the laws, or, in its most restricted sense, personal attachment to the supreme ruler; 'capital' may mean either the amount of money possessed by a trader, or his whole stock of commodities available for future production; 'natural' may express either the original condition of a thing, or the state into which it is ultimately developed, besides having countless other meanings. On account of the various significations which may be attached to the same term, it is necessary, in entering on any investigation, carefully to define the terms to be employed, and never, without express notice, to deviate from the sense thus imposed upon them 8.

^{*} The so-called 'Fallacia plurium interrogationum' has not been noticed in the text, because it is a rhetorical artifice, rather than a logical fallacy. It consists in covertly putting as a single question what is in reality two, as for instance, 'Are gall and honey sweet?' 'Have you cast your horns?' (known as 'cornutus'). 'What did you take, when you broke into my house last night?' 'Have you given up beating your father?' The object is to entrap the respondent into an admission which he would otherwise not be likely to make.

CHAPTER IX.

On Method as applied to the arrangement of Syllogisms in a Train of Reasoning.

I DO not propose to treat of Method in general (for this would involve a discussion of induction and the various relations in which it stands to deductive inference), but it may be useful to the student if I offer a few remarks on Method under the limitation stated in the heading of this chapter. When syllogisms are combined in a train of reasoning, we may either commence with the conclusion, and ask what reasons we have for believing it, and then go on to ask the reason for believing the premisses, and so on, till at last we arrive at some propositions of which there is no doubt, or in which we at least can acquiesce; or else we may follow the reverse process, and commencing with propositions which are the result of some previous investigation, or which we at all events accept as true, may go on combining them with each other, till at last we arrive at some conclusion which we regard as sufficiently important to terminate our enquiries. The former method will be familiar to my readers as that by which we solve what are called 'geometrical deductions,' and in fact as the method which we generally though not

universally employ when we are attempting to resolve difficulties for ourselves; the latter as the method by which the propositions in Euclid are proved, and in fact as the method which we generally though not universally employ, when it is our object to teach others, either orally or by book. Now the former method is called Analytical (from the Greek word dodnous), because it may be regarded as the breaking up of a whole into its parts, the resolution of the final conclusion of a series of syllogisms into the various premisses on which it depends, and of which it is, as it were, the total expression. The latter method is called Synthetical (from the Greek word σύνθεσιε), because it may be regarded as the putting together of the parts into a whole, the combination of the various premisses into a conclusion which is, as it were, their total result. The Synthetical Method is also sometimes called Progressive, and the Analytical Method Regressive, for reasons which will be apparent from what has already been said.

The words a priori and a posteriori may also be used to express the same distinction. In inductive inference (to which these terms are more properly applied) we are said to proceed a posteriori, when, a certain event having taken place, we attempt to trace the steps by which it came about, or, a certain phenomenon being presented to us for examination, we attempt to infer the mode of its production; and, vice versa, we are said to proceed a priori, when, from our knowledge of certain circumstances, we attempt to predict an event, or, by putting in

operation certain causes, we attempt to discover their effect. Similarly, in deductive inference, if, a conclusion being assumed as provisionally true, we attempt to discover reasons for it, we may be said to proceed a posteriori; if, starting with the premisses, we go on combining them to see whither they will lead us, we may be said to proceed a priori. In the former method of reasoning, we are peculiarly liable to impose on ourselves or others by availing ourselves of premisses which are fanciful, obscure, incapable of proof, questionable, or untrue, especially if the conclusion express some cherished conviction or some position which it is the interest of ourselves, our class, or our party to accept and to disseminate. Whenever, therefore, we argue from our conclusions backwards, especial caution is required, if it be our sincere desire to test our convictions impartially.

There is also a more general employment of these latter expressions, according to which the term a posteriori is appropriated to designate inductive reasoning, which ought always to be based on individual facts of observation; a priori to designate deductive reasoning, which proceeds from general principles. The expression a priori is often applied by way of censure to deductive reasoning, when the general principles from which it proceeds are supposed to rest on no ultimate inductions from fact, but to be mere assumptions arbitrarily taken for granted by the author who employs them.

OF SYLLOGISMS IN A TRAIN OF REASONING. 159

Note.—For an account of the various senses in which the words 'analysis' and 'synthesis' are or have been employed, the student is referred to Sir W. Hamilton's Lectures on Logic, Lect. xxiv, and Dr. Mansel's edition of Aldrich, Appendix G.

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APPENDIX.

On the Five Words 'Genus,' 'Species, 'Differentia,' 'Property,' 'Accident.'

WHEN two classes are so related to each other that one is contained under the other, the larger or containing class is called the *Genus*, and the smaller or contained class is called the *Species*. Thus, if we compare animal and man, man is a species, and animal the genus; if a man and Englishman, man is the genus, and Englishman a species: if we compare moss-rose and rose, moss-rose is a species, and rose the genus; if rose and flower, flower is the genus, and rose a species.

Genera and Species are denoted by Common Terms, which themselves also, as well as the groups which they denote, are called Genera and Species.

In the A proposition, a genus can be predicated of a species, but not a species of a genus. Thus we can say 'All men are animals,' or 'Man is an animal,' but not 'All animals are men,' or 'An animal is a man.' In the I proposition, on the other hand, the genus may be the subject, and in the O proposition, if the terms compared are genus and species, must be.

The distinction between Differentia, Property, and Accident is more difficult, but may be explained by reference to what has been said (Pt. I. ch. ii.) on the Connotation of Terms.

As the former distinction was applicable to classes and the common terms which denote them, so this is applicable to

attributes and the attributives by which attributes are expressed. It may be noticed also that a Differentia, Property, or Accident, being expressed by an Attributive, must be a predicate and cannot be a subject. Now, taking any common term, or any abstract term used as a common term, like triangle, an attributive predicated of it may express either part of its connotation or not. Thus, if we assert that 'A triangle is a three-sided rectilineal figure,' the term 'three-sided,' like the genus 'figure,' is connoted by the very term 'triangle.' Moreover, the term 'three-sided' serves to differentiate or distinguish 'triangle' from all other rectilineal figures, such as quadrilateral, pentagon, &c. Hence we may define differentia as on p. 45. Here however a difficulty occurs. Two or more species falling under the same genus may be distinguished by more than one differencing attribute. In this case we should speak of the differentiæ, or we might speak of the differentia as the sum of the differentia.

But, in case the attributive does not express any part of the connotation of the term, it may, nevertheless, express some attribute which follows from the connotation. Thus, if we say 'A triangle is a rectilineal figure having the sum of its angles equal to two right angles,' we are predicating by the expression 'having' &c., not part of the connotation of the word triangle, but an attribute which may be directly inferred from part of the connotation. Or, again, if we were dealing with some moral or physical phenomenon, the attribute might follow, not as a conclusion from a premiss, but as an effect from a cause. Thus we might predicate of man that he is 'capable of progress,' this capability being regarded as an effect of his rationality; or of animal and vegetable tissues that they are liable to decay, this liability being regarded as an effect of the material of which they are composed and the influences to which they are subject. Hence the definition of Property on p. 45.

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Lastly, the attributive may neither express any part of the connotation of the term, nor any attribute which follows from part of the connotation. In this case it is called an Accident. But accidents are of two kinds. If an accident may be predicated of all the individuals denoted by a common term, as, to take the conventional instance, blackness of crows, it is called an Inseparable Accident. In the most common case, where it is predicable of some of the individuals and not of others, as, for instance, blackness of men, it is called a Separable Accident.

The student is recommended to compare, throughout, this explanation with the definitions given on p. 45.



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EXAMPLES.



EXAMPLES.

- EXAMINE the following Definitions or Descriptions (pointing out their faults, if any, and, where they are sufficient, stating under what head of Definition or Description they fall).
 - (1) A square is a four-sided rectilinear figure, having all its sides equal.
 - (2) Monarchy is a form of political government in which one man is sovereign.
 - (3) An University is a corporation which grants learned degrees.
 - (4) Logic is the Art of Reasoning.
 - (5) A plane triangle is a figure generated by the section of a cone passing through the vertex and perpendicular to the base.
 - (6) Wealth is the sum of things useful, necessary, and agreeable.
 - (7) Man is a mammal having hands and cooking his own food.
 - (8) An animal is a sentient organised being.
 - (9) A liquid is that which can be poured out.
 - (10) A Federation is a political union the members of which are bound together for purposes of offence and defence.
 - (11) Man is a mammal possessing the power of articulate speech.
 - (12) Political Philosophy is the science of the laws which govern the equilibrium and development of human society.

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Examine the following Divisions, substituting, where they are incorrect, one or more correct ones.

- (1) Men into Aryans, Mongolians, Africans, and Americans.
- (2) Quadrilateral Figures into Squares, Rectangles, Parallelograms, and Rhomboids.
- (3) The Fine Arts into Painting, Drawing, Sculpture, Architecture, Poetry, and Photography.
- (4) Governments into Monarchies, Tyrannies, Oligarchies, and Democracies.
- (5) Books into entertaining and unentertaining.
- (6) Men into those who lend and those who borrow.
- (7) The Sciences into Physical, Social, Ethical, Logical, and Metaphysical.
- (8) Plants into Flowering Plants, Mosses, Ferns, and Pines.
- (9) The origin of Colonies is to be traced either to the necessity for frontier garrisons (as amongst the Romans) or to the poverty or discontent of the inhabitants of the mother-country (as amongst the Greeks and ourselves).
- (10) 'The general stock of any country or society is the same with that of all its inhabitants or members, and therefore naturally divides itself into the same three portions, each of which has a distinct function or office:
 - 1st, that portion which is reserved for immediate consumption, and of which the characteristic is that it affords no revenue or profit;
 - and, the fixed capital, of which the characteristic is that it affords a revenue or profit without circulating or changing masters;
 - 3rd, the circulating capital, of which the characteristic is that it affords a revenue only by circulating or changing masters.'—Adam Smith's Wealth of Nations, Vol. ii. ch. i.

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Convert the following propositions (previously permuting them, where necessary).

- (1) All plane triangles are rectilinear figures.
- (2) All plane triangles are three-sided rectilinear figures.
- (3) All plane triangles may be defined as three-sided rectilinear figures.
- (4) Some branches of Mathematics admit of a direct practical application.
- (5) Men of fair promises are often not to be trusted.
- (6) Some members of the Government are not prepared to accept the measure.
- (7) Virtue is a condition of Happiness.
- (8) Virtue is the condition of Happiness.
- (9) A syllogism is a form of inference.
- (10) With man many things are impossible.
- (11) Some men of great powers of imagination are not poets.
- (12) None but persons of great powers of imagination are poets.
- (13) What I have written, I have written.
- (14) Propositions are either simple or complex.,
- (15) The proper study of mankind is man.
- (16) Only the ignorant affect to despise knowledge.
- (17) He can't be wrong whose life is in the right.

State in logical form (where necessary) and examine the following arguments.

- Every book is liable to error,
 Every book is a human production;
 - ... All human productions are liable to error.
- (2) All tulips are beautiful flowers, No roses are tulips;
 - .. No roses are beautiful flowers.

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- (3) Some men are wise, Some men are good;
 - ... Some wise men are good,
- (4) All wise men are good, Socrates was a wise man;
 - ... He was good.
- (5) Some mathematicians are logicians, No logicians are unacquainted with the works of Aristotle;
 - ... Some mathematicians are not unacquainted with the works of Aristotle.
- (6) No persons destitute of imagination are true poets, Some persons destitute of imagination are good logicians;
 - ∴Some good logicians are not true poets.
- (7) No persons destitute of imagination are true poets, Some persons destitute of imagination are good ' logicians;
 - ... Some true poets are not good logicians.
- (8) If Cæsar was a tyrant, he deserved to die, Cæsar was not a tyrant;
 - ... He did not deserve to die,
- (9) If virtue is involuntary, vice is also involuntary, Vice is voluntary;
 - .. Virtue is also voluntary.
- (10) All valid syllogisms have three terms, This syllogism has three terms;
 - .. It is a valid syllogism.
- (11) Some learned men have become mad, He is not a learned man;
 - ... He will not become mad.
- (12) The Reformers were bitter enemies of the Papal Supremacy,

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- A B was a Reformer (for he was prominent in supporting the Reform Bill of 1832);
- ... He was a bitter enemy of the Papal Supremacy.
- (13) Logic is either a science or an art, It is a science;
 - .. It is not an art.
- (14) Six and seven are even and uneven, Thirteen is six and seven;
 - ... Thirteen is even and uneven.
- (15) He must be a Mahommedan, for only Mahommedans hold these opinions.
- (16) He must be a Mahommedan, for all Mahommedans hold these opinions.
- (17) To reject this proposal would be unreasonable, and consequently to accept it is reasonable.
- (18) This event happened either at Rome, Naples, or Florence; it did not happen at Rome or Naples, and consequently it must have happened at Florence.
- (19) Logic is indeed worthy of being cultivated, if Aristotle is to be regarded as infallible; but he is not: Logic therefore is not worthy of being cultivated.
- (20) An indissoluble association of ideas commands belief, and consequently every belief is the consequence of an indissoluble association of ideas.
- (21) This measure would be destructive of the national prosperity, and I cannot adduce a more cogent argument than that, five years ago, you were yourself of the same opinion.
- (22) If a man cannot make progress towards perfection, he must either be a brute or a divinity; but no man is either: therefore every man is capable of such progress.
- (23) Lias lies above New Red Sandstone, New Red Sand-

- stone lies above coal; therefore Lias lies above Coal.
- (24) My hand touches the pen; the pen touches the paper: therefore my hand touches the paper.
- (25) A, B, C, D, and E, are the only German students I know: they are all men of considerable intellectual attainments, and consequently I may infer that all German students are men of considerable intellectual attainments.
- (26) All equilateral triangles are equiangular, and therefore all equiangular triangles must be equilateral.
- (27) These two figures are equal to the same figure, and therefore to one another.
- (28) For those who are bent on cultivating their minds by diligent study, the incitement of academical honours is unnecessary; and it is ineffectual for the idle and such as are indifferent to mental improvement: therefore the incitement of academical honours is either unnecessary or ineffectual.
- (29) He has no appreciation of beauty, for he has no taste for Pictures.
- (30) Warm countries alone produce wines, Spain is a warm country; therefore Spain produces wines.
- (31) The Germans are a literary nation; therefore A B, who is a German, is a literary man.
- (32) We must increase the income-tax, for war has become a necessity, and we cannot go to war without money, and money can only be raised by taxation, and the only tax which the resources of the country can bear is the income-tax, which will fall on the richer part of the population.
- (33) Governors of dependencies should be vested with absolute power, for otherwise it is impossible to crush rebellion.

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- (34) A is larger than B, and B is larger than C; therefore, a fortiori, A is larger than C.
- (35) Alexander is the son of Philip, and therefore Philip is the father of Alexander.
- (36) If 'to improve is to change, and to be perfect is to have changed often,' what hope can we entertain of those who oppose change?
- (37) Luxury is at once beneficial and injurious to society; for luxury is the using the gifts of Providence, either to the injury of the user, or to the injury of others towards whom the user stands in any relation which obliges him to aid and assistance; but luxury causes expenditure of money, and therefore is beneficial to society.
- (38) Old age is wiser than youth; therefore it is only reasonable that we should be guided by the decisions of our ancestors.
- (39) A man cannot always be right in his opinions, and therefore we ought continually to distrust our judgments.
- (40) Had an armistice been beneficial to France and Germany, it would have been agreed upon by those powers; but such has not been the case: it is plain, therefore, that an armistice would not have been advantageous to either of the belligerents.
- (41) If education is popular, compulsion is unnecessary; if unpopular, compulsion will not be tolerated.
- (42) I will not do this act, because it is unjust; I know that it is unjust, because my conscience tells me so, and my conscience tells me so, because the act is wrong.
- (43) This proposition is too good to be practicable.
- (44) Such and such a system of education has produced several distinguished men; therefore it does not admit of any improvement.

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- (45) Slavery is a natural institution; but what is natural is just, and what is just it is unjust to abrogate; and consequently it would be unjust to abrogate slavery.
- (46) 'Mercy but murders, pardoning those that kill.'

 Romeo and Juliet, Act iii. Sc. 1.
- (47) A, B, and C have distinguished themselves both in athletic sports and intellectual pursuits; therefore those who are most famous for their excellence in athletic sports are generally most famous for their intellectual attainments as well.
- (48) What is called a 'constitutional monarchy' is impossible, for the sovereign authority of a state cannot be limited by law; now the king is sovereign, and, as such, cannot be subject to any superior authority.
- (49) Parallel lines are equi-distant; for, if from two points in one of them perpendiculars be drawn to the other, these perpendiculars are parallel (Euc. I. 28), and the two lines intercepted between them are parallel; therefore a parallelogram is formed, of which the perpendiculars are opposite sides and therefore equal.
- (50) If Bacon's opinion is right, it is improper to stock a new colony with the refuse of jails: but this course we must allow not to be improper, if our method of colonising New South Wales be a wise one: if this be wise, therefore, Bacon's opinion is not right.
- (51) 'Profit' is interpreted in the dictionary 'advantage'; to take profit, then, is to take advantage: it is wrong to take advantage of one's neighbour: therefore it is wrong to take profit.
- (52) Romulus must be a historical person, because it is not at all likely that the Romans, whose memory was only burdened with seven kings, should have forgotten the most famous of them, namely, the first.
- (53) You maintain that an action can only be called virtuous,

if it contribute to the welfare of mankind or of some section of mankind: hence you are bound to regard every convenient object, for instance a horse, a tree, or a chair, as virtuous.

- (54) The knowledge of things is more useful than the knowledge of words; and, therefore, the study of nature is more improving to the mind than the study of language.
- (55) In a lottery it is improbable that any particular ticketholder will draw the prize. But some one must draw the prize. Therefore something improbable must happen.
- (56) My informant A heard his story from B, who would certainly tell it as originally told to him; B heard it from C, who would probably tell it accurately; C from D, who would also probably tell it accurately; D from E, who, I have no reason to suppose, would tell it inaccurately: I may consequently receive A's story as probably accurate.
- (57) Large colonies are as detrimental to the power of a state as overgrown limbs to the vigour of the human body.
- (58) All law is an abridgment of liberty, and consequently of happiness.
- (59) I am under an obligation to do it, but he who is obliged has no power of resistance; consequently I have no choice about the matter.
- (60) You never give an opinion without believing yourself to be right, and therefore you must suppose yourself to be infallible.
- (61) If man be not a necessary agent, determined by pleasure and pain, there is no foundation for rewards and punishments. These would be useless, unless men were necessary agents, and were determined by pleasure and pain: because, if men were free and

- indifferent to pleasure and pain, pain could be no motive to cause men to observe the law.
- (62) Night invariably precedes day, and therefore night must be the cause of day.
- (63) The planet Mars resembles the Earth in the possession of an atmosphere, clouds, and water, and has a temperature in which terrestrial life might exist, and, therefore, it is probably inhabited as the earth is.
- (64) 'If it be fated that you recover from your present disease, you will recover, whether you call in a doctor or not; again, if it be fated that you do not recover from your present disease, you will not recover, whether you call in a doctor or not: but one or other of these contradictories is fated, and therefore it can be of no service to call in a doctor.'—(Ignava Ratio.)
- (65) The story of the formation of the human race by Prometheus must be true, for the clay from which he formed it was shown in Greece within historical times.
- (66) The Latin word 'virtus' originally meant 'manliness'; hence the virtue of manliness or courage is the highest virtue and the type of all other virtues.
- (67) This person may reasonably be supposed to have committed the theft, for he can give no satisfactory account of himself on the night of the alleged offence; moreover he is a person of bad character, and, being poor, is naturally liable to a temptation to steal.
- (68) Opium produces sleep, for it possesses a soporific virtue.
- (69) The student of History is compelled to admit the truth of the Law of Progress, for he finds that Society has never stood still.
- (70) You are inconsistent with yourself, for you told me yesterday that there was a presumption of this man's guilt, and now, when I say that I may presume his guilt, you contradict me.
 - 71) 'Suppose one man should by fraud or violence take from

another the fruit of his labour with intent to give it to a third, who, he thought, would have as much pleasure from it as would balance the pleasures which the first' possessor would have had in the enjoyment and his vexation in the loss of it; suppose also that no bad consequences would follow; yet such an action would surely be vicious.' Butler, On the Nature of Virtue.

- (72) There exist many differences of opinion and much uncertainty with regard to many questions connected with Geology; consequently Geology is not a science, and any arguments which assume the truth of geological theories must invariably be regarded with considerable suspicion.
- (73) 'Suppose Achilles to move ten times as fast as the Tortoise, but the Tortoise to have the start of Achilles, say, by one-tenth of the distance to be traversed: when Achilles has arrived at the point from which the Tortoise started, the Tortoise will still be one-hundredth part of the whole distance in advance of him; when Achilles has reached this point, the Tortoise will still be one-thousandth part of the whole distance in advance of him; and so on. Thus Achilles will never be able to pass the Tortoise.'

(Fallacy of Achilles and the Tortoise.)

- (74) 'Epimenides the Cretan says that "all the Cretans are liars," but Epimenides is himself a Cretan; therefore he is himself a liar. But if he be a liar, what he says is untrue, and consequently the Cretans are veracious; but Epimenides is a Cretan, and therefore what he says is true; hence the Cretans are liars, Epimenides is himself a liar, and what he says is untrue. Thus we may go on alternately proving that Epimenides and the Cretans are truthful and untruthful.'—(Fallacy of Mentions.)
- (75) The idea of the obligation to virtue is innate, for it is

found in all men, and it could not be universal if it were acquired by experience.

- (76) Berkeley's Theory of the Non-existence of Matter is palpably absurd, for it is impossible even to place one's foot on the ground without experiencing the resistance of matter.
- (77) I have no hesitation in saying that the proposition, however good in theory, is in practice utterly absurd.
- (78) If any objection that can be urged would justify a change of established laws, no laws could reasonably be maintained; but some laws can reasonably be maintained: therefore no objection that can be urged will justify a change of established laws.
- (79) I cannot accept your opinion as true, for it seems to me that its general recognition would be attended with the most injurious consequences to society.
- (80) Why should any but professional moralists trouble themselves with the solution of moral difficulties? For, as we resort to a physician in case of any physical disease, so, in the case of any moral doubt or any moral disorganisation, it seems natural that we should rely on the judgment of some man specially skilled in the treatment of such subjects.
- (81) 'Wood, stones, fire, water, flesh, iron, and the like things, which I name and discourse of, are things that I know. And I should not have known them but that I perceived them bymy senses; and things perceived by the senses are immediately perceived; and things immediately perceived are ideas; and ideas cannot exist without the mind; their existence therefore consists in being perceived; when, therefore, they are actually perceived there can be no doubt of their existence.'
- Berkeley, Third Dialogue between Hylas and Philonous.

 (82) 'And because the greatest part of men are such as prefer their own private good before all things, even

that good which is sensual before whatsoever is most divine; and for that the labour of doing good, together with the pleasure arising from the contrary, doth make men for the most part slower to the one and proner to the other, than that duty prescribed them by law can prevail sufficiently with them: therefore unto laws that men do make for the benefit of men it hath seemed always needful to add rewards, which may more allure unto good than any hardness deterreth from it, and punishments, which may more deter from evil than any sweetness thereto allureth.'

Hooker, Eccl. Pol. Bk. I. x. (6.)

(83) 'The scarcity of a dear year, by diminishing the demand for labour, tends to lower its price, as the high price of provisions tends to raise it. The plenty of a cheap year, on the contrary, by increasing the demand, tends to raise the price of labour, as the cheapness of provisions tends to lower it. In the ordinary variations of the price of provisions, those two opposite causes seem to counterbalance one another; which is probably in part the reason why the wages of labour are everywhere so much more steady and permanent than the price of provisions.'

Adam Smith, Wealth of Nations, Bk. I. ch. viii.

(84) 'I am a Jew. Hath not a Jew eyes? hath not a Jew hands, organs, dimensions, senses, affections, passions? fed with the same food, hurt with the same weapons, subject to the same diseases, healed by the same means, warmed and cooled by the same winter and summer, as a Christian is? If you prick us, do we not bleed? If you tickle us, do we not laugh? If you poison us, do we not die? and if you wrong us, shall we not revenge? If we are like you in the rest, we will resemble you in that.'

Merchant of Venice, Act iii. Sc. 1.

(85) The most striking and important of the effects of heat consist, however, in the liquefaction of solid substances, and the conversion of the liquids so produced into vapour. There is no solid substance known which, by a sufficiently intense heat, may not be melted, and finally dissipated in vapour; and this analogy is so extensive and cogent, that we cannot but suppose that all those bodies which are liquid under ordinary circumstances, owe their liquidity to heat, and would freeze or become solid if their heat could be sufficiently reduced. In many we see this to be the case in ordinary winters; for some, severe frosts are requisite; others freeze only with the most intense artificial colds; and some have hitherto resisted all our endeavours; yet the number of these last is few, and they will probably cease to be exceptions as our means of producing cold become enlarged. A similar analogy leads us to conclude that all aëriform fluids are merely liquids kept in the state of vapour by heat. Many of them have been actually condensed into the liquid state by cold accompanied with violent pressure; and as our means of applying these causes of condensation have improved, more and more refractory ones have successively yielded. Hence we are fairly entitled to extend our conclusion to those which we have not yet been able to succeed with; and thus we are led to regard it as a general fact, that the liquid and aëriform or vaporous states are entirely dependent on heat, that were it not for this cause, there would be nothing but solids in nature; and that, on the other hand, nothing but a sufficient intensity of heat is requisite to destroy the cohesion of every substance, and reduce all bodies, first to liquids, and then into vapour.'

Herschel, On the Study of Natural Philosophy.

(86) 'We are not inclined to ascribe much practical value to

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that analysis of the inductive method which Bacon has given in the second book of the Novum Organum. It is indeed an elaborate and correct analysis. But it is an analysis of that which we are all doing from morning to night, and which we continue to do even in our dreams.'

Macaulay, Essay on Bacon.

(87) 'Promises are not binding where the performance is unlawful. There are two cases of this: one, where the unlawfulness is known to the parties, at the time of making the promise; as where an assassin promises his employer to despatch his rival or his enemy; or a servant to betray his master. The parties in these cases are not obliged to perform what the promise requires, because they were under a prior obligation to the contrary. From which prior obligation what is there to discharge them? Their promise, their own act and deed. But an obligation, from which a man can discharge himself by his own act, is no obligation at all. The guilt therefore of such promises lies in the making, not in the breaking of them; and if, in the interval betwixt the promise and the performance, a man so far recover his reflection, as to repent of his engagements, he ought certainly to break through them."

Paley, Moral and Political Philosophy,

Bk. III. Part I. ch. v.

(88) 'This, I think, any one may observe in himself, and others, that the greater visible Good does not always raise men's desires in proportion to the greatness, it appears, and is acknowledged to have: Though every little Trouble moves us, and sets us on work to get rid of it. The Reason whereof is evident from the Nature of our Happiness and Misery itself. All present Pain, whatever it be, makes a part of our present Misery: But all absent Good does not at any time

make a necessary part of our present Happiness, nor the absence of it make a part of our Misery. If it did, we should be constantly and infinitely miserable; there being infinite degrees of Happiness, which are not in our possession. All Uneasiness therefore being removed, a moderate portion of Good serves at present to content men; and some few degrees of pleasure in a succession of ordinary Enjoyments make up a Happiness, wherein they can be satisfied. If this were not so, there could be no room for those indifferent, and visibly trifling Actions, to which our Wills are so often determined; and wherein we voluntarily waste so much of our Lives; which remissness could by no means consist with a constant determination of Will or Desire to the greatest apparent Good.'

Locke, Essay concerning Human Understanding, Bk. II. ch. xxi. § 44.

(89) 'There is only one part of the Protectionist scheme which requires any further notice: its policy towards colonies, and foreign dependencies; that of compelling them to trade exclusively with the dominant country. A country which thus secures to itself an extra foreign demand for its commodities, undoubtedly gives itself some advantage in the distribution of the general gains of the commercial world. Since, however, it causes the industry and capital of the colony to be diverted from channels, which are proved to be the most productive, inasmuch as they are those into which industry and capital spontaneously tend to flow; there is a loss, on the whole, to the productive powers of the world, and the mother country does not gain so much as she makes the colony lose. If, therefore, the mother country refuses to acknowledge any reciprocity of obligation, she imposes a tribute on the colony in an indirect mode, greatly more oppressive and in-

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jurious than the direct. But if, with a more equitable spirit, she submits herself to corresponding restrictions for the benefit of the colony, the result of the whole transaction is the ridiculous one, that each party loses much, in order that the other may gain a little.'

Mill's Political Economy, Bk. V. ch. x. § 1.

(90) 'The money to replace what has been burned will not be sent abroad to enrich foreign manufactures; but, thanks to the wise policy of protection which has built up American industries, it will stimulate our own manufactures, set our mills running faster, and give employment to thousands of idle workmen. Thus in a short time our abundant natural resources will restore what has been lost, and in converting the raw material our manufacturing interests will take on a new activity.'

New York Tribune of Oct. 24, 1871, quoted by Professor Cairnes in 'Some Leading Principles of Political Economy.'

** A syllogism, when not stated in logical form, usually appears to contain four, or perhaps more, terms. We must not, however, reject it on that account, till we have previously attempted to translate the propositions of which it is composed into equivalent propositions, containing among them three terms only. The cases in which this cannot be done are either those in which the terms of the conclusion, or at least one of them, are distinct, not in form only, but in meaning, from any of the terms employed in the premisses, or those in which there is no term common, or capable of being represented as common, to the two premisses. Thus the syllogism 'Lias lies above New Red Sandstone, New Red

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Sandstone lies above Coal; therefore Lias lies above Coal,' obviously admits of being stated in the form, 'Whatever lies above New Red Sandstone lies above Coal, Lias lies above New Red Sandstone; therefore Lias lies above Coal,' and consequently ought not to be rejected as having four terms. But the premisses 'Lias lies above New Red Sandstone, the Cretaceous System lies above the Oolitic,' contain no term common, nor any term capable (from a mere inspection of the language) of being represented as common, to the premisses, and hence they might fairly be rejected as containing four terms, and consequently leading to no conclusion. Even here, however, by any one who possessed sufficient special knowledge of Geology to be aware that the Oolitic System lies above Lias, the premisses might be represented as containing three terms only, and as necessitating the conclusion 'The Cretaceous System lies above New Red Sandstone.' But from such premisses as 'Lias lies above New Red Sandstone,' 'A Painting should represent beauty of colour as well as beauty of form,' no conclusion whatever could be drawn by means of either logical or special knowledge. The premisses are, in fact, utterly alien to each other, or, in other words, they are not in pari materia. In examining an argument, the student may always avail himself of any special knowledge which he may possess, provided that, in his answer, he carefully distinguish between what is due to such special knowledge and what to a knowledge of the ordinary usages of language and of the rules of Logic.

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In the first example given above, a mere knowledge of the rules of Logic, without any reference whatever to the usages of language, would not justify us in drawing any conclusion from the premisses; the slightest acquaintance with the usages of language would however enable us to represent the terms, which are apparently four, as three, and to infer the conclusion 'Lias lies above Coal.' But in the second example no acquaintance either with the rules of Logic or with the ordinary usages of language would enable us to draw the conclusion, 'The Cretaceous System lies above New Red Sandstone;' such a conclusion, though valid, is only justified by a special knowledge of Geology: no person, unacquainted with the facts of Geology, would be justified in admitting the conclusion as an inference from the premisses.

Where it is obvious that an argument is intended to be syllogistic, and only one premiss is stated, it is of course expected that the student will supply the other premiss.

In some of the examples, it may be an useful exercise to discuss the truth of the premisses as well as the legitimacy of the conclusion.



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DESIGNED MAINLY

FOR THE USE OF STUDENTS IN THE UNIVERSITIES

BY

THOMAS FOWLER, D.D.

President of Corpus Christi College Wykaham Professor of Logic in the University of Oxford And Honorary Dotter of Laws in the University of Edinburgh

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PREFACE TO THE FIRST EDITION.

THE object of the following work is to serve as an introduction to that branch of scientific method which is known as Induction. It is designed mainly for the use of those who have not time or opportunity to consult larger works, or who require some preliminary knowledge before they can profitably enter upon the study of them.

To the works' of Mr. Mill, Dr. Whewell, and Sir John Herschel, the Author must, once for all, express his obligations. 'He has, however,' if he may be allowed to repeat the language already employed in the Preface to his *Manual of Deductive Logic*, 'endeavoured, on all disputed points, to reason out his own conclusions, feeling assured that no manual, however elementary, can be of real service to the student, unless it express what may be called the "reasoned opinions" of its author.'

The analysis of Induction presents far more difficulties than that of Deduction, and requires to be illustrated by far more numerous and intricate examples. But, on the other hand, it is more interesting both to the

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teacher and to the student; and, being a comparatively recent study, is less hampered by conventionalities of treatment. Since the time of Bacon, it has always, with more or less of success, claimed a place in liberal education, and many, to whom the technical terms and subtle distinctions of the older logic are justly repulsive, have experienced a peculiar delight in attempting to discover and test the grounds on which the results of modern science mainly rest.

The study of Deductive Logic can be of little service unless it be supplemented by, at least, some knowledge of the principles of Induction, which supplies its premisses. Many of the objections directed against the study of Logic are due to the narrow conceptions which are entertained of its province, and might be easily met by showing that the study, when we include both its parts, has a much wider range than is popularly assigned to it.

Though the present work is mainly intended for students in the Universities, it is hoped that it will be found to present some interest for the general reader, and that it may be useful to students of medicine and the physical sciences, as well as to some of the more advanced scholars in our Public Schools.

The number of scientific examples adduced throughout the work renders it necessary, perhaps, that the Author should state emphatically that the work is intended as an

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introduction, not to science, but to scientific method. Its object is not to give a résumé of the sciences, physical or social, a task for which the Author would be wholly incompetent, but to show the grounds on which our scientific knowledge rests, the methods by which it has been built up, and the defects from which it must be free. Notwithstanding its frequent incursions into the domain of science, the purport of the work must be regarded as strictly logical.

The examples have, as a rule, been selected from the physical rather than the social sciences, as being usually less open to dispute, and lying within a smaller compass. Wherever it has been possible, they have been given in the exact words of the author from whom they are taken.

Some of the more complicated cases of inductive reasoning, such as those which deal with Progressive Causes or Intermixture of Effects, have, if alluded to at all, been only briefly noticed. Any detailed examination of these more intricate questions seemed to lie without the scope of the treatise. The student who has leisure to pursue the subject will find ample information in the pages of Mr. Mill's Logic.

It only remains for the Author to express his grateful acknowledgments to those who have assisted him in the execution of the work. These are, in the first place, due to Dr. Liddell, Dean of Christ Church, through whose hands the sheets have passed, and who, in addition to

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revising the proofs, has, from time to time, offered many very valuable suggestions. They are due also, in no small degree, to Sir John Herschel and Professor Bartholomew Price, who most kindly undertook to revise the scientific examples; to Professors Rolleston and Clifton, who have frequently allowed the Author to consult them on questions connected with the subjects of their respective chairs, and to the Rev. G. W. Kitchin, the Organising Secretary of the Clarendon Press Series. The Author must, however, be regarded as alone responsible for any errors which may occur either in the theoretical portion of the work or in the examples.

Lincoln College, Oct. 30, 1869.

PREFACE TO THE THIRD EDITION.

[The student is requested to read this Preface in connexion with Chapter III.]

SINCE the publication of my second Edition, there has appeared an important work on Scientific Method, entitled 'The Principles of Science,' by Professor Stanley Jevons, of Owens College, Manchester. To this book I have made occasional references in the foot-notes to my present edition. But, as I differ entirely from Professor Jevons on the fundamental question of the validity of our inductive inferences, I think it desirable to offer a few remarks on this point in the present place, rather than to introduce controversial matter into the body of the work.

Mr. Jevons over and over again asserts the uncertainty, or the mere probability, of all inductive inferences. Thus, for instance, in his chapter on the Philosophy of Inductive Inference, he says:—'I have no objection to use the words cause and causation, provided they are never allowed to lead us to imagine that our knowledge of nature can attain to certainty'.' And again: 'We can never recur too often to the truth that our knowledge of

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the laws and future events of the external world is only probable. Once more: 'By induction we gain no certain knowledge; but by observation, and the inverse use of deductive reasoning, we estimate the probability that an event which has occurred was preceded by conditions of specified character, or that such conditions will be followed by the event.'

At the same time, I am quite unable to reconcile with these passages other passages, such as those in which Mr. Jevons says: 'We know that a penny thrown into the air will certainly fall upon a flat side, so that either the head or tail will be uppermost',' or, 'I can be certain that nitric acid will not dissolve gold, provided I know that the substances employed really correspond to those on which I tried the experiment previously '.'

But, waiving the question of inconsistency, I maintain as against Mr. Jevons that many of our inductive inferences have all the certainty of which human knowledge is capable. Is the law of gravitation one whit less certain than the conclusion of the 47th Proposition of the First Book of Euclid? Or is the proposition that animal and vegetable life cannot exist without moisture one whit less certain than the truths of the multiplication table? Both these physical generalisations are established by the

⁴ Id. p. 228. Mr Jevons, however, curiously enough is not certain about the truth of the Law of Gravitation. See below.

⁸ Id. p. 270.

Method of Difference, and, as actual Laws of Nature, admit, I conceive, of no doubt. But it may be asked if they will always continue to be Laws of Nature? I reply that, unless the constitution of the Universe shall be changed to an extent which I cannot now even conceive, they will so continue, and that no reasonable man has any practical doubt as to their continuance. And why? Because they are confirmed by the whole of our own experiences, which in both these cases is of enormous extent and variety, by the experience of our ancestors, and by all that we can ascertain of the past history of nature, while their reversal would involve the reversal of almost all the other laws with which we are acquainted. Still, it must be confessed that all our inferences from the present to the future are, in one sense, hypothetical, the hypothesis being that the circumstances on which the laws themselves depend will continue to be the same as now, that is, in the present case, that the constitution of nature, in its most general features, will remain unchanged; or, to put it in still another form, that the same causes will continue to produce the same effects. What would happen if this expectation were ever frustrated, it is absolutely impossible for us to say, so completely is it assumed in all our plans and reasonings.

We may say, then, that there are many inductions as to the *actual* constitution of nature which we may accept with certainty, while, with respect even to the distant

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future, we may accept them with equal certainty, on the hypothesis that the general course of nature will not be radically changed. And if the general course of nature were changed, might not the change affect our faculties as well as the objects of our knowledge; and, in that case, are we certain that we should still regard things that are equal to the same thing as equal to one another, or assume that a thing cannot both be and not be in the same place at the same time? There is, in fact, no limit to the possibility of scepticism with regard to the persistency either of the laws of external nature or of the laws of mind. But all our reasonings depend on the hypothesis that the most general laws of matter and the most general laws of mind will continue to be what they are, and of the truth of this hypothesis no reasonable man entertains any practical doubts.

There is, then, I contend, no special uncertainty attaching to the truths arrived at by induction. They are, indeed, like all other truths, relative to the present constitution of nature and the present constitution of the human mind, but this is a limitation to which all our knowledge alike is subject, and which it is vain for us to attempt to transcend. Syllogistic reasoning implies a particular constitution of the mind, as much as induc-

Thus Mr. Jevons, who, when he begins to theorise, has doubts as to the truth of the Law of Gravitation, has no doubt, when he throws a penny up into the air, that it will fall on a flat side.

tive reasoning implies a particular constitution of nature. Both mind and nature might, of course, be radically changed by an omnipotent power, but what the consequences of that change might be it is utterly impossible for us to say.

The uniformity of nature, the trustworthiness of our own faculties—these are the ultimate generalisations which lie at the root of all our beliefs, and are the conditions of all our reasonings. It is, of course, always possible to insinuate doubts as to either, but, however curious and entertaining such doubts may be, they have no practical influence even on those who originate them. Even Mr. Jevons himself, we have seen, when not under the dominion of his theory, speaks of some of the results of induction as certain, and we can hardly conceive men of science commonly speaking of the most firmly established generalisations of mechanics, optics, or chemistry, simply as conclusions possessing a high degree of probability.

Still, Mr. Jevons, appearing not in the character of a physicist, but of a logician, tells us that 'the law of gravitation itself is only probably true'.' It would be interesting to learn what is the exact amount of this 'probability,' or, if it be meant that we can only be certain that the force of gravity is acting here and now, it would be an interesting enquiry to ascertain what is

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the exact value of the 'probability' that it is at this moment acting in Manchester as well as in Oxford, or that it will be acting at this time to-morrow as well as to-day.

But, if the conclusions of Induction are thus uncertain, where, according to Mr. Jevons, are we to find certainty? 'Certainty belongs only to the deductive process and to the teachings of direct intuitions.' Does it then belong to the conclusions of deduction? Apparently not, for, at the very beginning of the work, we are told that 'in its ultimate origin or foundation, all knowledge is inductive,' and Mr. Jevons is, of course, too practised a logician to suppose that the conclusion can be more certain than the premisses. The conclusions of geometry, therefore, partake of the same 'uncertainty' as the results of the physical sciences, and the region of 'certainty' is confined to our direct intuitions and to the rules of syllogism (supposing, that is, a difference to be intended between the 'deductive process' and deductive results). I venture to suggest that this small residuum of 'certainty' would soon yield to solvents as powerful as those which Mr. Jevons has applied to the results of induction (and apparently also of deduction); and that, therefore, its inherent 'uncertainty' is no special characteristic of that method, but one which it shares with all our so-called knowledge.

The fact is that in all reasoning, whether inductive or deductive, we make, and must make, assumptions which may theoretically be questioned, but of the truth of which no man, in practice, entertains the slightest doubt. Thus, in syllogistic reasoning, we assume at every step the trustworthiness of memory; we assume, moreover, the validity of the premisses, which, as Mr. Jevons acknowledges, must ultimately be guaranteed either by induction or direct observation; lastly, we assume the validity of the primary axioms of reasoning, which, according to different theories, are either obtained by induction or assumed to be necessary laws of the In this sense, all reasoning and all human mind. science is hypothetical, and the assumption of the Uniformity of Nature does not render inductive reasoning hypothetical in any special sense of the term. For, if the Laws of the Uniformity of Nature and of Universal Causation admit of exceptions or are liable to ultimate frustration, so, for aught we know, may the axioms of syllogistic reasoning or the inductions by which we have established the trustworthiness of our faculties. And, if the conceptions of uniformity and causation be purely relative to man, so, for aught we know, may be the so - called laws of thought themselves 10. Induction

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According to the view of the nature and ultimate origin of human knowledge, accepted both by Mr. Jevons and myself, it is, in fact, no paradox but a mere truism to say that the fundamental axioms of reasoning are themselves only particular uniformities of

would only be hypothetical in a special sense, if we had any reasonable ground for doubting the truth of the hypotheses 12 on which it rests.

But as, 'in its ultimate origin or foundation, all knowledge' (including, of course, that of the laws which govern the syllogistic process itself) 'is inductive,' Professor Jevons must either employ the word 'certain' in a variety of senses, or he must be prepared with the philosophers of the New Academy to maintain the uncertainty of all knowledge whatsoever.

Such, as it appears to me, are the inconsistencies and paradoxes into which a very able writer has been led by a tendency to over-refinement, and, still more perhaps, by a desire to apply the ideas and formulæ of mathematics to the explanation of logical problems.

I must further express my dissidence from Mr. Jevons' statement that all inductive inference is preceded by nature, arrived at by the same evidence and depending for their justification on the same grounds as those ultimate generalisations

on causation to which we give the special names of the Law of Universal Causation and the Law of the Uniformity of Nature.

In each hardly say that I am not here using the word 'hypothesis' in the sense of an unverified assumption. Reasoning, both inductive and deductive, is found on analysis to depend, in the last resort, on certain assumptions or hypotheses, but then the truth of these assumptions or hypotheses is guaranteed by the whole experience of the human race, past and present, and beyond this guarantee I conceive that there is no other attainable. In other words, all truth is relative to our faculties of knowing, and this condition it is in vain for us to attempt to transcend.

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hypotheses 18, from his theory that Induction is simply the Inverse Method of Deduction, and, above all, from what appears to me to be the exceedingly misleading parallel drawn between Nature and a ballot-box. 'Events,' says Mr. Jevons, 'come out like balls from the vast ballot-box of Nature 13.' Now the balls were placed in the ballot-box by human hands; the number and character of them may have been due merely to caprice or chance; moreover, they are all isolated entities having no connexion with each other. Would it be possible to find a stronger contrast to the works of nature? If natural phenomena did indeed admit only of the same kind of study as the drawing of balls from a ballot-box, Mr. Jevons' conception of Induction would undoubtedly be the true one, and I should agree with him that 'no finite number of particular verifications of a supposed law will render that law certain.' But, just because we believe that the operations of Nature are conducted with an uniformity for which we seek in vain amongst the contrivances of men, do we regard ourselves as capable, in many cases, of predicting the one class of events with certainty, while the other affords only matter for more or less probable conjecture.

Intimately connected with Mr. Jevons' depreciation of the value of the inductive inference is his statement that

¹² See chap. i. pp. 11-13, of this work. ¹³ Vol. i. p. 275.

Induction is simply the inverse method of Deduction. If Induction simply consists in framing hypotheses, deducing consequences from the hypotheses, and then comparing these consequences with individual facts for the purpose of verifying them by specific experience 14, I grant that the procedure must, in most cases, be very untrustworthy. In my first Appended Note to my Section on Hypothesis, I have examined this account of Induction, which is virtually identical with that of Dr. Whewell. In opposition to it, I maintain the following theses, which are explained and defended in the course of my work: 1. That our inductions are not always preceded by hypotheses (and it might be added that, even where they are, the hypothesis itself must rest originally on some basis of fact, that is to say, on some induction or other, however imperfect; for a hypothesis must always be suggested by something of which we have had experience); 2. That the mere verification of our hypotheses by specific experience is not sufficient to constitute a valid induction, unless the instances conform with the requirements of one of the inductive methods, or (as in the case of the fundamental laws of inductive reasoning) be coextensive with the whole experience of mankind. Induction, I maintain, may or may not employ hypothesis, but what is essential to it is the inference from the particular

to the general, from the known to the unknown, and the nature of this inference it is impossible to represent adequately by reference to the forms of deduction ¹⁶.

'without a considerable amount of circumlocation,' as the essential difference between inductive and deductive reasoning consists, not so much in the form of the argument, as in the nature of the assumptions made: scientific induction postulating, in addition to the assumptions made in deductive reasoning, the laws of Universal Causation and of Uniformity of Nature, in its strictest sense (see p. 9, note 7); and Inductio per Enumerationem Simplicem, the latter law in its vaguer sense. I think it may be useful to the student here to transcribe (with some subsequent modifications) a note which appeared in the last (9th) edition of my Deductive Logic (pp. 73, 74, note 3).

'If we state explicitly all the assumptions made in the inductive process, the conclusion is contained in the premisses, and the form of the reasoning becomes deductive; but it is seldom that we do state our assumptions thus explicitly. The most essential distinction, however, between inductive and deductive reasoning consists not in the form of the inferences, but in the nature of the assumptions on which they rest. Deductive reasoning rests on certain assumptions with regard to language and co-existence (namely, the Law of Contradiction, the Law of Excluded Middle, and the Canons of Syllogism), while inductive reasoning assumes over and besides these laws the truth of the Laws of Universal Causation, of the Uniformity of Nature and, as implied in the latter, of the Conservation of Energy; or, if it be of the unscientific description which is known as Inductio per Enumerationem Simplicem, it merely assumes, instead of them, the vague and wide principle that the unknown resembles, or will resemble, the known. It hardly needs to be added that all reasoning alike assumes the trustworthiness of present consciousness and of memory.

Amongst the assumptions or pre-suppositions of reasoning, I have not included the so-called Law of Identity; as to say that all A is A,

Mr. Jevons' statement that 'induction is really the reverse process of deduction' I am wholly unable to reconcile with the following statements which occur in the very same page 16: 'In its ultimate origin or foundation all knowledge is inductive,' and 'only when we possess such knowledge, in the form of general propositions and natural laws, can we usefully apply the reverse process of deduction to ascertain the exact information required at any moment.' When we compare these statements, the circle seems complete. A precedes B, and B precedes A. A depends for its validity on B, and B depends for its validity on A. No wonder that human reasoning affords us no 'certain' results.

In offering these criticisms on some fundamental points of difference between Mr. Jevons and myself, I am far from denying the utility of many portions of his work, especially the chapters on the Methods of Measurement and on Hypothesis.

In the present Edition of this work, I have occasionally availed myself of the 'Inductive Logic' of

or a thing is the same as itself, appears to me to be an utterly unmeaning proposition. Mr. Mill (Examination of Hamilton, ch. 21), in attempting to give a meaning to this maxim, really transforms it into a perfectly distinct proposition, namely, that Language may express the same idea in different forms of words.'

¹⁰ Vol. i. p. 14.

Mr. Bain, a work which, though it does not, in my opinion, supersede Mr. Mill's Logic, supplies on some points a valuable complement to it.

In this, as in the last Edition, I have to acknowledge the kindness of Professor Park of Belfast, whose corrections and suggestions have enabled me to make both my works more accurate and serviceable than they would otherwise have been.

LINCOLN COLLEGE. Feb. 24, 1876.

, In the third Edition some new matter was introduced, bearing mainly on the following subjects: Uniformities of Coexistence, the Historical Method, the distinction between Inductio per Enumerationem Simplicem and the Method of Agreement, the constant alternation in practice of the inductive and deductive processes, and the Argument from Universal Consent. In the fourth Edition the principal alterations were the introduction of new foot-notes on the definition of Induction and on the Plurality of Causes, and some additional remarks on the nature of the Method of Residues and on Empirical Laws.

In the fifth Edition, the alterations are more numerous than in either of the two preceding editions. Through the kindness of my friend, Mr. George Griffith of Harrow, I have been enabled to state some of the scientific examples in a more precise form than in the preceding editions, notably those on Double-Weighing (p. 47), on the 'Red Flames' seen during a total eclipse of the Sun (pp. 50-1), and on Spectrum Analysis as applied to the constitution of the Sun and other heavenly bodies (pp. 165-7). The principal alterations or additions in the logical matter are on pp. 204-5 (the Historical Method), p. 206 (the Comparative Method), pp. 227-8 (the Fallacy of 'Exaggerated Comparison'), and the addition of an important foot-note (note 15, p. xix) to the 'Preface to the Third Edition,' on the peculiar nature of Inductive Reasoning and on the assumptions made in it. The following foot-notes are either new or contain additional matter: n. 4, p. 6; n. 11, p. 13; n. 22, p. 23; n. 41, pp. 107-8; n. 5, p. 129; n. 27, p. 166; n. 44, p. 191; n. 54, p. 205; n. 55, pp. 206-7; n. 63, p. 214; n. 24, pp. 281-2; n. 26, p. 282; n. 29, p. 283; n. 80, p. 343.

C. C. C. Dec. 1, 1888.

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Έκ προγινωσκομένων δὲ πᾶσα διδασκαλία, δοπερ καὶ ἐν τοῖς ἀναλυτικοῖς λέγομεν ἡ μὲν γὰρ δι' ἐπαγωγῆς, ἡ δὲ συλλογισμῷ. Ἡ μὲν δὴ ἐπαγωγὴ ἀρχή ἐστι καὶ τοῦ καθόλου, ὁ δὲ συλλογισμὸς ἐκ τῶν καθόλου. Εἰσὶν ἄρα ἀρχαὶ ἐξ ὧν ὁ συλλογισμὸς, ὧν οὐκ ἔστι συλλογισμός ἐπαγωγὴ ἄρα.

Aristotle's Nicomachean Ethics, vi. 3 (3).

Quamvis ad scientiam quamlibet via unica pateat, quâ nempe a notioribus ad minus nota et a manifestis ad obscuriorum notitiam progredimur, atque universalia nobis præcipuè nota sint (ab universalibus enim ad particularia ratiocinando oritur scientia), ipsa tamen universalium in intellectu comprehensio a singularium in sensibus nostris perceptione exmigit.

Preface to Harvey's Treatise De Generatione Animalium.

ELEMENTS

OF

INDUCTIVE LOGIC.

*** The notes appended to the Chapters (as distinguished from the foot-notes) are designed to inform the student of any divergences from the ordinary mode of treatment, or to afford him information on disputed questions which it appeared inconvenient to notice in the text. They may be omitted on the first reading.

CHAPTER I.

On the Nature of Inductive Inference.

TWO bodies of unequal weight (say a guinea and a feather) are placed at the same height under the exhausted receiver of an air-pump. When released, they are observed to reach the bottom of the vessel at the same instant of time, or, in other words, to fall in equal From this fact, it is inferred that a repetition of the experiment either with these two bodies or with any other bodies would be attended with the same result, and that, if it were not for the resistance of the atmosphere and other impeding circumstances, all bodies, whatever their weight, would fall through equal vertical spaces in equal times. Now, that these two bodies in this particular experiment fall to the bottom of the receiver in equal times is merely a fact of observation, but that they would do so if we repeated the experiment, or that the next two bodies we selected, or any bodies, or all bodies, would do so, is an inference, and is an inference of that particular character which is called an Inductive Inference or an Induction 1.

What assumptions underlie this inference, and on what grounds does it rest?

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¹ The student must throughout bear in mind the ambiguous use of the words Induction, Inference, &c., as signifying both the result and the process by which the result is arrived at. See Deductive Logic, Preface, and Part III. ch. i. note 1.

My object in placing the two bodies under the receiver was obviously to answer a question which I had previously addressed to myself: viz. whether, when subject to the action of gravity2 only, they would fall in equal or in unequal times. By exhausting the air in the receiver, I am able to isolate the phenomenon, and thus, by removing all circumstances affecting the bodies, except the action of gravity, to watch the effect of this cause operating alone. But in trying this experiment, in isolating the phenomenon, and asking what will be the effect of the action of gravity operating alone, I am evidently assuming that the effect, whatever it may be, will be entirely due to the cause or causes which are then and there in action; in other words, I am assuming that nothing can happen without a cause, that no change can take place without being preceded or attended by circumstances which, if we were fully acquainted with them, would fully account for that change. This assumption (which may be called the Law of Universal Causation) is universally admitted by mankind, or at least by the reflecting portion of mankind, though the grounds on which it is admitted have been variously stated; some justifying it by an appeal to the continuous and uncontradicted experience not only of the individual himself

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When I employ the expression 'action of gravity' or 'force of gravity,' I must not be understood as adopting any particular theory on the nature of the phenomenon which we call 'gravitation.' I use these terms simply because they are short and recognised phrases for expressing the fact that all terrestrial bodies, when left entirely free, fall in the direction of the earth's centre.

but of the human race, others by an appeal to the necessities of thought.

Thus far, however, we have only ascertained that the fact of these two particular bodies, in this particular instance, falling to the ground in equal times is due to the action of gravity, unimpeded by any other circumstances. But why should I infer that they, if the experiment were repeated, or any other two bodies, if exposed to the same circumstances, would behave in the same way? It is not enough to feel assured that nothing can happen without a cause, and that the only cause operating in this particular instance is the action of gravity; I must also feel assured that the same cause will a invariably be followed by the same effect, or, to speak more accurately, that the same cause or combination of causes, will, if unimpeded by the action of any other cause or combination of causes, be invariably followed by the same effect or combination of effects, or, to state the same proposition in somewhat different language, that, whenever the same antecedents, and none others, are introduced, the same consequents will invariably follow. This assumption (or law) is, like the former, universally admitted by mankind, or the reflecting portion of mankind, though the grounds on which it is admitted have been variously stated, some, as in the case of the former law, referring it to experience, others to certain necessities of thought arising

² The expression 'will' is used for the sake of brevity. The argument, however, is not simply from the present to the future, but from cases within the range of our experience to all cases, past, present, or future, without that range. See p. 32, note 31.

from the original constitution of the human mind. This law may be called the Law of the Uniformity of Nature 1.

The argument, then, in the case which we have taken as our instance, may be represented as follows:—

- I observe that these two bodies (though of unequal weight) reach the bottom of the receiver at the same moment.
- This fact must be due to some cause or combination of causes (Law of Universal Causation).
- The only cause operating in this instance is the action of gravity.
- .. The fact that these two bodies reach the bottom of the receiver at the same moment is due to the action of gravity, operating alone.
 - But, whenever the same cause or combination of causes is in operation, and that only, the same effect will invariably follow (Law of Uniformity of Nature).
- It is, perhaps, necessary thus early to warn the student that the converse of the Law of the Uniformity of Nature does not hold true. Though the same cause, that is, the same antecedent or combination of antecedents, is never followed by different effects, the same effect, or, more strictly speaking (see pp. 127, 8), the same portion of an effect, may be due to different causes. We can, thus, always argue from the cause to the effect, but we cannot always argue from the effect to the cause.

The Law of the Uniformity of Nature implies, I conceive, the truth of the law of the Persistence or Conservation of Energy (namely, that no cause, or part of a cause, will ever be ineffective, or, in other words, that no energy is ever lost), and hence I have not thought it necessary to introduce any express mention of this latter law in the text.

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... Whenever these two bodies, or any other two or more bodies (even though of unequal weight), are subject to the action of gravity only, they will reach the bottom of the receiver at the same moment, or, in other words, will fall in equal times.

The induction just examined has been arrived at by a process of elimination, and takes for granted the conception of causation. It is representative of the inductions with which science is mainly concerned, and of which I shall have, for the most part, to treat in the present work. But there are other inductions of a simpler character, the validity of which is assured not by any artificial process of elimination, but merely by a series of uncontradicted experiences. This kind of induction is usually distinguished by logicians as Inductio per Enumerationem Simplicem. It is often (as will hereafter be pointed out in the 4th chapter) exceedingly untrustworthy, but, when the area of experience is very wide, the evidence which it affords may approach to, and even amount to, certainty. Often moreover, and especially in the case of our widest generalisations, it is our only resource.

Amongst inductions of this kind must be included, as I conceive, the Laws of Uniformity of Nature and Universal Causation themselves, as well as the axioms of mathematics and certain facts of co-existence which have not yet been resolved into, or possibly do not admit of being resolved into, facts of causation. As examples of the last class I may specify the co-existence throughout matter of the properties of inertia and gravity, and the

co-inherence of attributes in the various kinds of animals, plants, and minerals, as, for instance, fusibility at a certain point together with a certain specific gravity in gold, or the combination of rationality with a peculiar physical form in man. Though co-existing facts of this nature may possibly be due to some causal connexion, and might, if we had a perfect knowledge of all natural processes, be explained in that manner, they are, as yet, known to us only as facts of co-existence, and established only by an inductio per enumerationem simplicem, or uncontradicted experience.

Mr. Bain be established by induction, those of Co-existence, Causation, and Equality. Uniformities of Co-existence and Equality can be established only by Inductio per Enumerationem Simplicem, while those of Causation, though, in the actual state of our knowledge, they often rest only on this evidence, ought always to be established by the more refined methods to be described in the sequel of this book. To the above classification I ought to add the Laws of Uniformity of Nature and Universal Causation, both of which, as already remarked, I conceive to be established by uncontradicted experience, or, in other words, by an Inductio per enumerationem simplicem coextensive with all human knowledge. These fundamental laws, thus verified by a constant experience,

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³ Logic, Bk. III. ch. ii.

⁶ On the nature of the evidence on which these laws rest, see the third appended note at the end of this chapter.

are assumed in all scientific inductions concerning Causation, whereas, in mere inductions per Enumerationem Simplicem, all that is assumed is the much vaguer and less precise belief that, under similar circumstances, the unknown resembles, or will resemble, the known, a belief which experience shows to be subject to many modifications.

As the inductions of Causation are those with which science is mainly concerned, and to which alone the more refined rules of Inductive Logic are applicable, I shall in the following work limit myself almost entirely to their consideration. The inductions of Co-existence, with which I shall, to some extent, be concerned in the section on Classification, I shall regard as subservient to these *.

From what has been said above, as well as in distinguishing the various kinds of inference in the Manual of Deductive Logic, it will be seen that Induction may be defined as the legitimate inference of the unknown from the known, that is, of propositions applicable to cases hitherto unobserved and unexamined from propositions which are known to be true of the cases observed and examined. Thus, from the proposition that a guinea

⁷ This belief is what is frequently understood by the Law of the Uniformity of Nature, but I have thought it desirable to confine that expression to the more precise statement with regard to the uniform action of causes.

I shall briefly recur to the subject of Inductions of Co-existence in the fourth chapter, under the head of *Inductio per Enumerationem Symplicem*.

and a feather, if placed under the exhausted receiver of an air-pump, will fall through equal vertical spaces in equal times, may be inferred inductively the proposition that a shilling, a penny, and a straw will, if exposed to the same circumstances, also fall in equal times. But, as we can only draw this inference on grounds which are equally applicable to all bodies whatsoever, when exposed to the same circumstances, and as we might make the same assertion of any two or more bodies, and consequently of all bodies, it will be seen that Induction is not only an inference of the unknown from the known; but, in virtue of that fact, of the general from the particular. In every inductive argument, in fact, it is implied that wherever or whenever the same circumstances are repeated, the same effects will follow. Induction may, therefore, also be defined as the legitimate inference of the ✓ general from the particular, or (in order to include those) cases where general propositions are themselves employed as the starting-point of an inductive argument, of which numerous instances will occur as we proceed) of the more general from the less general .

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^{*} This is a better and more accurate definition than that given at the beginning of the paragraph, because, if we adopt the theory that all our fundamental beliefs are derived from experience, there is no kind of inference which does not involve the assumption that we may argue from the known to the unknown, and from the past to the present and the future. In the case of some of these beliefs, however, as the so-called 'laws of thought,' and the belief in the trustworthiness of our present consciousness and of memory, the assumption has been made so often and so constantly that we have almost ceased to be conscious of making it.

In trying the experiment which furnished our instance at the beginning of the chapter, we were attempting to find an answer to the question, 'Do bodies, when subject to the action of gravity only, fall through equal vertical spaces in equal or in unequal times?' The experiment may be regarded as an attempt to decide between two rival theories (or hypotheses, as they are usually called), one being that bodies fall quicker in proportion to their weights, the other that the weight of the body, when the resistance of the atmosphere is removed, does not affect the time of falling. The experiment is decisive in favour of the latter hypothesis, which is thus entitled to rank as a valid induction. Our inductions are often, as in this case, the result of an attempt to decide between rival hypotheses, or a reply to the question whether some particular hypothesis be true or not, the hypothesis or hypotheses suggesting the particular experiment to be tried. Sometimes, however, we have no assistance of this kind, and we try experiments simply 'to see what will come of them.' Thus, if a chemist discovers a new element, he will proceed to try a variety of experiments in order to determine the proportions in which it will combine with other elements, as well as to discover the various properties of such combinations. Supposing the experiments to have been properly conducted, the inductions at which he arrives will be perfectly valid, though he may have formed no previous theories as to the results of his researches. Occasionally, too, an induction will not be the result of any definite course of investigation, but will be obtruded on our notice, as in the following instance, adduced by Sir John Herschel, to show that 'after much labour in vain, and groping in the dark, accident or casual observation will present a case which strikes us at once with a full insight into a subject.' 'The laws of crystallography were obscure, and its causes still more so, till Haüy fortunately dropped a beautiful crystal of calcareous spar on a stone pavement, and broke it. In piecing together the fragments, he observed their facets not to correspond with those of the crystal in its entire state, but to belong to another form; and following out the hint thus casually obtruded on his notice, he discovered the beautiful laws of the cleavage, and the primitive forms of minerals 10.'

Thus, we perceive that our inductions are sometimes preceded by hypotheses, at other times not. In most cases, probably, we have formed some supposition (or hypothesis) as to the character of a phenomenon before we enter upon, or, at least, before we complete, its investigation. Such suppositions (or hypotheses) are often of the utmost service in directing the course which our experiments and observations shall take. Frequently, also, it is impossible to perform any experiment, or to institute any series of observations, which shall be decisive of the question before us. In this case, unless we altogether suspend our judgment, we must rest content with an unproved theory, and it becomes of prime importance to determine to what conditions such a

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¹⁶ Herschel's Discourse on the Study of Natural Philosophy, § 191.

theory 11, supposition, or hypothesis must conform in order to entitle it to rank as a probable or possible solution of our difficulties. A subsequent section will be specially devoted to these questions, but meanwhile it seemed desirable at once to direct the attention of the student to the distinction between hypothesis and induction. He must bear in mind that, though the formation of hypotheses is frequently an important step in the inductive process, a hypothesis must be carefully distinguished from a valid induction. Without at present attempting any formal definition of a hypothesis, it may be distinguished from an induction (that is, a valid, complete, or perfect induction) as a mere supposition or assumption from an ascertained truth.

** The word 'cause' is commonly used in a very vague and indefinite sense. Of the various antecedents whose presence or absence is essential to the event, it is usual to single out one as the Cause, and either to overlook the others, or to speak of them as 'conditions.' Strictly speaking, however, the Cause consists in the presence of all those antecedents, the withdrawal of any of which, and in the absence of all those antecedents, the introduction of any of which, might frustrate the event. Thus, to take the homely instance of lighting a fire.

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In The word 'theory' is, unfortunately, employed in two meanings:

(I) as = hypothesis, as when we speak of the undulatory theory, the Darwinian theory, or two or more 'rival theories'; (2) as an ascertained truth, or body of truths, as when we speak of the 'lunar theory,' or the 'theory of equations.'

The application of the lighted match is what would ordinarily be called the cause of the combustion. there are other conditions equally necessary, as, for instance, amongst the positive conditions, the presence of fuel and of atmospheric air, and, amongst the negative conditions, the absence of such a quantity of moisture as would prevent the fuel from igniting. In assigning the cause of a phenomenon, it is seldom that the negative conditions are mentioned. It is generally understood that we assign a cause, subject to the qualification 'no counteracting cause intervening.' Amongst the positive conditions, we usually select that which, being last introduced, completes the assemblage of conditions, and stands in closest proximity to the effect. Thus, in our example, the combustion is said to be due to the application of the match, and, when a man, who has previously been in a bad state of health, is attacked by a fever, we speak of the fever as the cause of his death. These, however, as observed by Mr. Mill, are by no means invariable rules. 'It must not be supposed that in the employment of the term this or any other rule is always adhered to. Nothing can better show the absence of any scientific ground for the distinction between the cause of a phenomenon and its conditions, than the capricious manner in which we select from among the conditions that which we choose to denominate the cause. However numerous the conditions may be, there is hardly any of them which may not, according to the purpose of our immediate discourse, obtain that nominal pre-eminence.' Thus, if a plot of dry heath is ignited by a spark from a railwayengine, we may, in common parlance, attribute the fire either to the spark, or to the dryness of the heath, or to the ill-construction of the engine; the first of these assigned causes being the proximate event, the second one of the other positive conditions, the last a negative condition. What, when employing popular language, we dignify with the name of Cause is that condition which happens to be most prominent in our minds at It is, perhaps, superfluous to add that, when the time. aiming at scientific accuracy, we ought to enumerate all the conditions, or, at least, all the positive conditions, on which a phenomenon depends, unless we have a right to presume that there is no likelihood of their being overlooked by those whom we address 12.

In the science of Medicine, the cause which completes the assemblage of conditions is often distinguished as the exciting cause, the other causes being called pre-disposing. Thus, the peculiarities of constitution, age, sex, occupation, &c., which render a person more than ordinarily liable to any particular disorder, would be called the pre-disposing causes; the contagion (by which the body is brought into contact with some specific poison), a sudden chill, bodily fatigue, mental depression, or any circumstance, on the supervention of which the disease is immediately consequent, would be called

¹² The subject of this paragraph is treated with great ability in Mr. Mill's Logic, Bk. III. ch. v. § 3.

the exciting cause ¹⁵. The pre-disposing causes of Asiatic Cholera, for instance, are enumerated in Dr. Guy's edition of Dr. Hooper's 'Vade Mecum,' as 'debility; impaired health; intemperance; impure air; low and damp situations; the summer and autumn seasons: the exciting causes as contagion; a peculiar poison diffused through the atmosphere.' The importance of attending to this distinction in historical and political investigations is forcibly stated and illustrated by Sir G. C. Lewis, in his Methods of Observation and Reasoning in Politics, vol. i. ch. ix. p. 333, &c.

Note 1¹⁴.—Mr. Mill (Logic, Book II. ch. iii.) maintains that, in an act of induction we usually, though not invariably, argue directly from one particular case to another. Dr. Whewell, on the other hand, holds that all inductive inference is from the particular to the general. (Philosophy of Discovery, ch. xxii. § 1-14.) Though I have adopted Dr. Whewell's language (which is that ordinarily employed), I cannot recognise the importance of the difference which he believes to exist between himself and Mr. Mill. To say that what I find to be true of this case will be true of the next which resembles it in certain assignable respects, whatever that case may be, or that what I found to be true of that case must be true of this, because this resembles that in certain as-

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¹⁵ See Dr. Watson's Lectures on Physic, Lecture VI.

¹⁴ The student, unless he have some previous acquaintance with the subjects discussed in them, is recommended to omit these notes on the first reading.

signable respects, is virtually to say that it is true of any and every case which presents these points of resemblance. What is true of each or any case, taken indifferently, must be true of all. 'The burnt child dreads the fire.' Why? Because it once suffered pain, from burning its finger. Now, it appears to me indifferent whether we represent the child as having in its mind the proposition 'That object causes pain,' or the proposition 'That object will cause me pain now, if I approach too near to it.' But, as the former (the general) inference seems to be virtually implied in the latter (the particular), and, as Mr. Mill acknowledges, the particular inference can, on reflexion, only be justified by granting the truth of the general one, I prefer adhering to the common, and, as I think, the more intelligible account of induction. Mr. Mill himself, in one place, speaks of Induction as 'generalisation from experience,' and, in another, as 'the inference of a more general from less general propositions 15.7

Though agreeing with Dr. Whewell in his main position, I must express my entire dissent from the distinction which, throughout this discussion, he attempts to draw between our reasonings in the ordinary affairs

¹⁵ Mr. Jevons (*Principles of Science*, vol. i. pp. 261, 262) seems to have slightly misapprehended my meaning in this note. While I believe that we do, as a matter of fact, often argue from particular to particular, I entirely agree with Mr. Jevons (*Principles of Science*, vol. ii. p. 243) in holding that 'what is inferred of a particular case might be inferred of all similar cases,' or, in other words, that the *logical justification* of such inferences is to be found in the general statement.

of life, and Induction as employed in scientific research. However various may be the conditions of their application, I cannot but regard the mental processes as identical, on whatever classes of objects they may be exercised. We may meet with insurmountable difficulties in the attempt to apply Induction to some obscure question of Physiology, and we may employ it with ease and success a hundred times a day in compassing pleasure or avoiding pain, but I believe the mental process to be essentially the same in both cases.

Note 2.—Since the time of Hume, the nature of our conception of Cause has formed one of the chief topics of philosophical controversy. Previously to his time, it appears to have been taken for granted by the great majority of modern philosophers of all schools ¹⁴ (if we except those who, like Malebranche, believed God to be the only efficient cause in the universe, and so-called acts of causation to be only the occasions of the Divine interference ¹⁷), that the idea of causation necessarily implies the idea of power or necessary connexion;

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Dugald Stewart (in his *Philosophy of the Human Mind*, Notes C and MM) has certainly succeeded in showing that Hume's views on the nature of Cause were anticipated by casual remarks of several other writers; but it still remains true that Hume was the first philosopher who definitely attacked the prevalent philosophical theory.

¹⁷ Still, even according to these philosophers, every act of causation implies an act of power; only the power is exerted not by the so-called cause, but by the Deity himself. It will be noticed that I speak only of *modern* philosophers. Into the difficult question of the notions of causation entertained by ancient writers I do not enter.

necessary connection, that is to say, between the cause and effect, or power in the cause to produce the effect. Even Locke, who effected a revolution in modern philosophy, left this idea of Power unassailed, though he attempted to account for its formation. 'The mind,' says he 18, being every day informed, by the senses, of the alteration of those simple ideas it observes in things without; and taking notice how one comes to an end, and ceases to be, and another begins to exist, which was not before; reflecting also on what passes within itself, and observing a constant change of its ideas, sometimes by the impression of outward objects on the senses, and sometimes by the determination of its own choice; and concluding from what it has so constantly observed to have been, that the like changes will for the future be made, in the same things, by like agents, and by the like ways, considers in one thing the possibility of having any of its simple ideas changed, and in another the possibility of making that change; and so comes by that idea which we call Power. Thus we say, fire has a power to melt gold, i.e. to destroy the consistency of its insensible parts, and consequently its hardness, and make it fluid; and gold has a power to be melted: that the sun has a power to blanch wax, and wax a power to be blanched by the sun, whereby the yellowness is destroyed, and whiteness made to exist in its room. In which, and the like cases, the power we consider is in reference to the change of perceivable ideas. For we

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¹⁸ Locke's Essay, vol. ii. ch. xxi. § 1.

cannot observe any alteration to be made in, or operation upon anything, but by the observable change of its sensible ideas; nor conceive any alteration to be made, but by conceiving a change of some of its ideas.' He then proceeds to include our idea of Power amongst our Simple Ideas.

Hume contested the validity of this idea by an appeal to experience. Whence do we obtain this notion of necessary connexion between two events? Do we observe any such connexion in the events which take place in the external world, or in the relation between volition and the motion of the organs of the body, or in the act of the will by which it summons up, dwells on, or dismisses ideas? 'We have sought in vain for an idea of power or necessary connexion, in all the sources from which we could suppose it to be derived. It appears that, in single instances of the operation of bodies, we never can, by our utmost scrutiny, discover anything but one event following another; without being able to comprehend any force or power, by which the cause operates, or any connexion between it and its supposed effect. The same difficulty occurs in contemplating the operations of mind on body, where we observe the motion of the latter to follow upon the volition of the former, but are not able to observe or conceive the tie, which binds together the motion and volition, or the energy by which the mind produces this effect. The authority of the will over its own faculties and ideas is not a whit more comprehensible: so that, upon the

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whole, there appears not, throughout all nature, any one instance of connexion, which is conceivable by us. All events seem entirely loose and separate. One event follows another; but we never can observe any tie between them. They seem conjoined, but never connected. And as we can have no idea of anything, which never appeared to our outward sense or inward sentiment, the necessary conclusion seems to be, that we have no idea of connexion or power at all, and that these words are absolutely without any meaning, when employed either in philosophical reasonings, or common life 10." Hume then deny the fact of causation, namely, that, when we have been accustomed to observe one event invariably followed by another, we may confidently expect, other circumstances remaining the same, that the one will continue to be followed by the other in the future, and that, if we perceive a change in any phenomenon, we may be confident that some other event has preceded that change? Certainly not. There is, in Hume's writings, absolutely no foundation for the virulence with which he is attacked by Reid 20. What he called in

¹⁹ Hume's Essays. Essay on the Idea of Necessary Causation.

The following may serve as a specimen of Reid's diatribes against Hume. 'Of all the paradoxes this author has advanced, there is not one more shocking to the human understanding than this, That things may begin to exist without a cause. This would put an end to all speculation, as well as to all the business of life. The employment of speculative men, since the beginning of the world, has been to investigate the causes of things. What pity is it, they never thought of putting the previous question, Whether things have a cause or not? This question has at last been started; and

question was not the invariableness of the fact of causation, but the grounds of the prevalent notions attached to the word Cause. Whether his speculations on this subject be well or ill-founded, he certainly did not deny the correctness of the principles on which men act in ordinary life or which guide them in scientific research.

There is another objection to the statements contained in Hume's Essay which is better founded than the foregoing. If the term 'cause' be convertible with the term 'invariable antecedent,' it has been justly objected by Reid 21 that we might speak of day as the cause of night, and of night as the cause of day. That there are expressions in the Essay, in which the cause seems to be absolutely identified with the invariable antecedent or the sum of the invariable antecedents, cannot be denied. Such is the following: 'Suitably to this experience, what is there so ridiculous as not to be maintained by some philosopher?'--- Active Powers, Essay I. ch. iv. Sir W. Hamilton and Dr. Mansel take a far juster view of Hume's position. Even Sir W. Hamilton, however, in commenting on Reid's statement, says, 'This' (namely, That things may begin to exist without a cause) 'is not Hume's assertion; but that, on the psychological doctrine generally admitted, we have no valid assurance that they may not.' The latter is, certainly, not Hume's assertion. It is true that he bases the notion of causation on experience, but then he regards experience as the sole source of all our knowledge, other than that of mathematics. Sir William Hamilton's note requires only to be compared with the following passage from the Essay: 'But when one particular species of event has always, in all instances, been conjoined with another, we make no longer any scruple of foretelling one upon the appearance of the other, and of employing that reasoning which can alone assure us of any matter of fact or existence."

^{*} Active Powers, Essay IV. ch. iii.

therefore, we may define a cause to be an object, followed by another, and when all the objects, similar to the first, are followed by objects similar to the second.' But then the sentence proceeds: 'Or, in other words, where, if the first object had not been, the second never had existed.' Now this alternative definition is not open to Reid's objection 99, though it is open to the objection of ignoring the fact that the same event may be due to distinct causes, as pointed out in p. 6, n. 428. When modified to meet this objection, it would run thus: 'Cause [or causes] and Effect are two [or more] events, or sets of events, which are so related, that, if the first [or one of the first] had not been, the second had never existed.' Or, perhaps, it might be more simply stated thus: 'An Effect is so related to its Cause or its alternative Causes, that if the latter or one of the latter had not been, the former had never existed 24.1

The alternative definition, however, introduces a new idea, not contained in the first definition, that of dependence of the effect upon the cause, which it is not easy to distinguish from the idea of necessary connexion. Hence, Hume appears unconsciously to recur to the very position which he is attacking. It seems to me that the relation of cause and effect, or the dependence of effect on cause, is an idea sui generis, and cannot be resolved into the mere idea of time, or antecedence and consequence. The introduction of the word 'power,' however, or even of the word 'necessary,' into the statement of the relation, occasions needless obscurity and difficulty.

I am indebted to Professor Park of Belfast for drawing my attention to this objection, which had escaped my notice in the First Edition. It was originally pointed out by Dr. Thomas Brown, in his Enquiry into the Relation of Cause and Effect, Note A.

²⁴ This definition is, it must be confessed, somewhat deficient in

Both Dr. Thomas Brown and Mr. Mill attempt to meet Reid's objection.

Brown holds that the cause is that invariable antecedent which *immediately* precedes the effect; thus the position of the sun at a given moment, that which we call sun-rise, is the cause of day.

Mill attempts to meet the same objection by having recourse to the idea of 'unconditionalness.' The cause of a phenomenon is 'the antecedent or concurrence of antecedents on which it is invariably and unconditionally consequent,' i.e. which not only invariably precedes it, but which is followed by the effect without the occurrence of any other condition. Now night cannot be called the cause of day, because it might go on for ever without being followed by day, unless the condition of the sun rising were fulfilled. See Mill's Logic, Bk. III. ch. v. § 5.

simplicity. But I venture to suggest that it will bear closer examination than that of Mr. Mill, who defines 'cause' as the 'unconditional invariable antecedent.' Whether by the term 'unconditional' he means 'not depending on any previous condition,' or 'not combined with any concurrent condition,' it may be objected that there is no such phenomenon in nature. If, as seems clear from the context, the term be used in the latter sense, we shall not only be excluded from saying that night is the cause of day, but also that solar light is the cause of day, for there are other conditions, both positive and negative, essential to the production of what we call day by the solar rays. In fact, according to the terms of this definition, we could never, as we are constantly doing, single out any one prominent phenomenon, and call it the cause of an event, without enumerating all the other conditions, positive and negative, which are essential to its operation.

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The objection to Brown's account is that we fre quently speak without hesitation of A as the cause of B, though we are by no means certain that it is, strictly speaking, the *immediate* antecedent of B, nothing else whatever intervening; in fact, it is questionable whether in any case we can ascertain to a certainty that nothing else intervenes between two events. Similarly, it may be objected to Mill's account that we frequently speak without hesitation of A as being the cause of B, though we are by no means certain that there are not other antecedent conditions, positive and negative, which must be satisfied before A can be followed by B; and, indeed, as in the former case, it may be questioned whether we can ever be certain that there are no other conditions besides those which we have selected 25.

The first author of eminence who adopted Hume's view of the nature of Cause was Dr. Thomas Brown; singularly enough, however, so far from assuming with Hume that its origin was to be found in experience, he regarded it as instinctive. The notion of 'Power' he supposed was simply a gratuitous hypothesis, needlessly interpolated between the antecedent, which we call the Cause, and the consequent, which we call the Effect. 'We are eager to supply, by a little guess-work of fancy, the parts unobserved, and suppose deficiencies in our observation where there may truly have been none; till at length, by this habitual process, every phenomenon

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It is curious that Mill, in attempting to answer Reid, takes no notice of Brown's answer.

becomes, to our imagination, the sign of something intermediate as its cause, the discovery of which is to be an explanation of the phenomenon. The mere succession of one event to another appears, to us, very difficult to be conceived, because it wants that intervening something which we have learned to consider as a cause: but there seems to be no longer any mystery, if we can only suppose something intervening between them, and can thus succeed in doubling the difficulty, which we flatter ourselves with having removed; since, by the insertion of another link, we must now have two sequences of events instead of one simple sequence. Hume's position is also accepted by James Mill in his Analysis of the Phenomena of the Human Mind, and by John Stuart Mill in his System of Logic.

Hume's antagonists have generally (with Kant) combated his arguments by denying the assumption on which they are based, namely, that the *origin* of our conception of Cause is to be sought in experience. Hume, it will be recollected, challenges those who maintain the hypothesis of 'power' or 'necessary connexion' to show how we can have become acquainted with it. Does it come from our experience of the external world, or from our experience of the control of our will over our own acts or our own thoughts? The answer of the Kantian School would be that it does not come from experience at all, that it is one of those fundamental conceptions which are native to the

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⁹⁶ Brown's Lectures on the Philosophy of the Human Mind, Lecture IX. Cp. Lecture II.

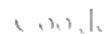
human mind, not given by experience but evoked by it. Others, like Reid and Stewart, to whom we may add M. Maine de Biran, surrender the notion of power as applied to causation in the external world, while they maintain it as applied to our own actions, which are the results of will. We are conscious, they say, of power in ourselves, though we perceive only succession in the external world. Dr. Mansel, following Cousin, adopts a third view, and maintains that the notion of 'Power' is given only in the control of the mind over its own operations. 'The intuition of Power is not immediately given in the action of matter upon matter; nor yet can it be given in the action of matter upon mind, nor in that of mind upon matter; for to this day we are utterly ignorant how matter and mind operate upon each other. We know not how the material refractions of the eye are connected with the mental sensation of seeing, or how the determination of the will operates in bringing about the motion of the muscles. We can investigate severally the phenomena of matter and of mind, as we can examine severally the constitution of the earth, and the architecture of the beavens: we seek the boundary line of their junction, as the child chases the horizon, only to discover that it flies as we pursue it. There is thus no alternative, but either to abandon the inquiry after an immediate intuition of power, or to seek for it in mind as determining its own modifications; -- a course open to those who admit an immediate consciousness of self, and to them only. My first and only presentation of power or causality

is thus to be found in my consciousness of myself as willing 27.

The relation subsisting between an act of will and the motion of the limbs, or between a physical antecedent and its consequent, he regards as beyond our knowledge. 'Our clearest notion of efficiency is that of a relation between two objects, similar to that which exists between ourselves and our volitions. But what relation can exist between the heat of fire and the melting of wax, similar to that between a conscious mind and its self-determinations? Or, if there is nothing precisely similar, can there be anything in any degree analogous? We cannot say that there is, or, if there is, how far the analogy extends, and how and where it fails. We can form no positive conception of a power of this kind: we can only say, that it is something different from the only power of which we are intuitively conscious. But, on the other hand, we are not warranted in denying the existence of anything of the kind; for denial is as much an act of positive thought as affirmation, and a negative idea furnishes no data for one or the other 25.2

It would, however, be beside my purpose to enter into a detailed account of the history of this controversy. In consequence, however, of its historical importance, it seemed essential to take some notice of it, and to point out that, whatever theory may be adopted as to the nature of Cause, and however great our inability to conceive how one event is followed by another, there is, at least, sufficient definiteness in the conception to entitle it to be accepted

^{*} Ibid. p. 140.



r Prolegomena Logica, pp. 138, 139.

as the basis of scientific reasoning. Whether we acknowledge that one event has invariably the power of producing another, or whether we content ourselves with asserting that it is invariably followed by that other, it is, in either case, the element of invariableness which makes the connexion or conjunction, whichever we may call it, a fitting object of scientific research. But remove the element of invariableness, and suppose, if it be supposable, that the same antecedent or set of antecedents is sometimes followed by one consequent, and sometimes by another, and sometimes by none at all; in that case science would be impossible.

The student who wishes to obtain further information on this controversy (a controversy, however, which possesses a historical rather than a practical or scientific interest) is referred to Hume's Essay on the Idea of Necessary Connexion; Dugald Stewart's Dissertation, Part II. sect. 8; Mill's Logic, Book III. ch. v; Sir W. Hamilton's Lectures on Metaphysics, Lectures XXXIX, XL; Mansel's Prolegomena Logica, ch. v; Mill on Hamilton, ch. xvi; Lewes' History of Philosophy, Articles on Hume and Kant. I refer only to books likely to be within the student's reach. In quoting or referring to Hume, I have employed only his Essays. Many writers persist in making references to his Treatise of Human Nature, a work written at the early age of twenty-seven and afterwards repudiated by the author as containing an immature expression of his opinions 30. In the Advertisement

²⁹ This work is undoubtedly of the highest philosophical interest,

to his Essays, he desires that 'the following Pieces may alone be regarded as containing the author's philosophical sentiments and principles.'

Note 3.—That a cause is ; that every event has a cause; that the same cause is always attended with the same effect; are obviously three distinct propositions, and still there are few writers who, in their treatment of the question of Causation, have not more or less confounded them. The first proposition (if completed) would be the Definition of Cause, the predicate, of course, depending on the view adopted with reference to the question discussed in the previous note. The second is a statement of the Law of Universal Causation, the third of the Law of the Uniformity of Nature.

It will be observed that in the text of this chapter I have said of each of these laws that it 'is universally admitted by mankind, or, at least, by the reflecting portion of mankind.' The latter clause must be regarded as emphatic, and suggests, I think, a sufficient answer to those authors who call in question their universal reception. Mr. Lewes, speaking of the Law of Universal Causation, says, 'All believe irresistibly in particular acts of causation. Few believe in universal causation;

but when we are concerned in determining the matured philosophical opinions of Hume it cannot be regarded as authoritative. It is curious to find a recent editor of Hume's Essays expressly defending the practice on which I have snimadverted in the text. See Mr. Grose's edition of Hume's Essays, vol. i. p. 39.

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and those few not till after considerable reflexion *0.' He then proceeds to adduce the case of a student of chemistry, who could not be convinced of the truth of the Law, but 'looked upon the argument as an unwarrantable assumption.' Now I venture to suggest that this incapacity was due to the terms of the proposition not being made sufficiently intelligible to him. I question whether any man of average powers of understanding could be found who would maintain the contradictory of either of these Laws; who would assert, that is to say, that an event might happen without anything to account for it, or that a repetition of exactly the same circumstances might be followed by a different effect. That a considerable amount of intelligence is necessary in order to understand the general terms in which the propositions are stated, is undeniable, but, when once understood, I presume that the propositions cannot fail to be acquiesced in. Like all other propositions, however, of wide import, they may be both understood and acquiesced in, without being fully realised. It is the full and constant realisation of these Laws, at all times and under all circumstances, which mainly distinguishes the man of scientific from the man of unscientific habits of thought. The unscientific man either does not think of enquiring into the causes of the phenomena around him, or notes with little precision the circumstances which he is investigating. The scientific man, on the other hand, insists on invariably referring the phenomena in which

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Lewes' History of Philosophy, Article on Kant.

he is interested to their several causes, and is satisfied with nothing but the most rigorous enquiry into the relation between these causes and their effects.

But, it may be asked, if the Laws of Universal Causation and of the Uniformity of Nature are, on reflexion, thus universally received, by what mental process do men assure themselves of their truth? Of the origin of these, as of kindred beliefs, two different explanations are offered by rival schools of psychologists. According to one school, the human mind is so constituted that it cannot but accept them; they are fundamental beliefs which exist in the mind prior to all experience, though it is experience which occasions us to realise our possession of them. We have never *learnt* them; we have simply discovered that we possess them. Thus Reid, speaking of our conviction that the future will resemble the past⁸¹ (what we now call the Law of Uniformity of Nature), says, 'The wise Author of our nature hath

of the Uniformity of Nature. 'It has been well pointed out,' says Mr. Mill, 'that Time, in its modifications of past, present, and future, has no concern either with the belief itself, or with the grounds of it. We believe that fire will burn to-morrow, because it burned to-day and yesterday; but we believe, on precisely the same grounds, that it burned before we were born, and that it burns this very day in Cochin-China. It is not from the past to the future, as past and future, that we infer, but from the known to the unknown; from facts observed to facts unobserved; from what we have perceived, or been directly conscious of, to what has not come within our experience. In this last predicament is the whole region of the future; but also the vastly greater portion of the present and of the past. —Mill's Lagic, Bk. III. ch. iii.

implanted in human minds an original principle by which we believe and expect the continuance of the course of nature, and the continuance of those connexions which we have observed in time past. It is by this general principle of our nature, that, when two things have been found connected in time past, the appearance of the one produces the belief of the other⁸².' And Dr. Whewell, speaking of the Law of Universal Causation, says, 'We assert that "Every event must have a cause:" and this proposition we know to be true, not only probably, and generally, and as far as we can see; but we cannot suppose it to be false in any single instance. We are as certain of it as of the truths of arithmetic or geometry. We cannot doubt that it must apply to all events past and future, in every part of the universe, just as truly as to those occurrences which we have ourselves observed. What causes produce what effects; -- what is the cause of any particular event; what will be the effect of any peculiar process;—these are points on which experience may enlighten us. Observation and experience may be requisite, to enable us to judge respecting such matters. But that every event has some cause, Experience cannot prove any more than she can disprove. She can add nothing to the evidence of the truth, however often she may exemplify it. This doctrine, then, cannot have been acquired by her teaching 33.

PReid's Inquiry into the Human Mind on the Principles of Common Sense, ch. vi. § 24.

³⁵ Whewell's History of Scientific Ideas, Bk. III. ch. ii. § 1.

The opposite school of psychologists (of which Mr. Mill and Professor Bain may be taken as the modern representatives) maintains that there is nothing in these and kindred beliefs which compels us to distinguish them generically from other truths, but that, like all other truths, they are the result of Experience. From our earliest years, we have been so constantly accustomed to observe one change preceded by another change, and the same antecedents followed by the same consequents, as well as to find our own experience in these respects corroborated by that of others, that, on reflexion, we all acquiesce, and cannot but acquiesce, in the statements which generalise these facts. This, it is held, is a sufficient explanation of that universality and necessity, which, by the advocates of the intuitional theory, described in the last paragraph, are supposed to distinguish the 'fundamental beliefs of the human mind' or 'the principles of common sense,' as they are called by these authors, from all other truths. The beliefs have acquired the character of universality and necessity, not because they have sprung from any other source than our ordinary beliefs, but because of the constancy and variety of the experience from which they are gained. 'In fact, our whole lives,' says James Mill, 'are but a series of changes, that is, of antecedents and consequents. The conjunction, therefore, is incessant; and, of course, the union of the ideas perfectly inseparable. We can no more have the idea of an event without having the ideas of its antecedents and its consequents, than we can have

the idea and not have it at the same time 4.' But here occurs a difficulty. If the Laws of Universal Causation and of the Uniformity of Nature are inferred from particular facts of causation, are generalisations from experience, or, in other words, inductions, how is it that they are made the grounds of all other inductions? Is not this to argue in a circle? The answer to this difficulty is that the Laws in question are the result of an uniform and constant experience, co-extensive not with the life of the single individual who employs them, but with the entire history of the human race; that, consequently, when we adduce them as the grounds on which our other inductions rest, we are performing the perfectly legitimate process of resolving narrower into wider cases of experience. The argument, in short, is this: the inference from this narrow field of observation (the particular induction which we happen to be making) must be allowed to be true, unless we are prepared to deny one or other of the much wider generalisations which constitute the Laws of Universal Causation and of the Uniformity of Nature. To recur to the instance adopted in the text, the proposition that bodies, subject to the action of gravity only, fall through equal vertical spaces in equal times, can be called in question only on

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James Mill's Analysis of the Phenomena of the Human Mind, ch. xi. The position maintained by James Mill is that these beliefs owe their universality to the fact of their being inseparably associated with all our other cognitions. This is only another mode of stating the theory which derives them from experience,

peril of doubting one or other of the fundamental laws; thus, the doubt which might attach to it is shifted to two other propositions which no one would think of questioning. Or, to state the same position in a slightly different form, this particular instance is shown to be a member of an infinitely long series, the other members of which have been examined and approved; as, therefore, it differs in no essential respect from them, it claims to be admitted also. There is, indeed, throughout this argument one assumption; as the rival theory assumed the trustworthiness of what it styled our 'fundamental beliefs,' so this assumes the validity of experience. But, unless we make one or other of these assumptions, we must be prepared to maintain that knowledge is altogether impossible 55.

There is a third theory of the origin of universal beliefs which combines, with certain modifications, both the others. It would admit that all beliefs alike are ultimately derived from experience, and still it would freely adopt the language that there are some beliefs which are 'native to the human mind.' The word 'experience,' as ordinarily employed by psychologists,

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^{**} It should be noticed that Dr. Mansel, while agreeing in the main, as he usually does, with the intuitional school, in respect to the origin of our belief in the Law of Universal Causation, refers to experience the origin of our belief in the Uniformity of Nature. 'The belief in the uniformity of nature is not a necessary truth, however constantly guaranteed by our actual experience.' Mansel's Metaphysics, Chapter on Necessary Truths. Cp. Prolegomena Logica, ch. v. Dr. Mansel's treatment of these questions is, in many respects, peculiar to himself.

includes not only the experience of the individual, but the recorded experience of mankind. On the theory, however, of which I am now speaking, it has a still more extended meaning; it includes experience, or, to speak more strictly, a peculiar aptitude for forming certain experiences, transmitted by hereditary descent from generation to generation. While some ideas occur only to particular individuals at particular times, there are others which, from the frequency and constancy with which they are obtruded upon the minds of men at all times and under all circumstances, become, after an accumulated experience of many generations, connatural, as it were, to the human mind. We assume them, often unconsciously, in our special perceptions, and when the propositions, which embody them, are propounded to us, we find it impossible, on reflexion, to doubt their truth. It is by personal experience of external objects and their relations that each man recognises them, but the tendency to recognise them is transmitted, like the physical or mental peculiarities of race, from preceding generations, and is anterior to any special experience whatever on the part of the individual. This theory, to which much of modern speculation appears to be converging, is advocated with great ability in the works of Mr. Herbert Spencer 86.

The student who wishes for further information on the questions discussed in this Note is referred to Dugald Stewart's *Philosophy of the Human Mind*, Part II. ch. v.

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^{*} See especially his work on the Principles of Psychology.

§ 287 ('Of that Permanence or Stability in the order of Nature which is presupposed in our Reasonings concerning Contingent Truths'); Reid's Intellectual Powers, Essay VI. ch. vi; Reid's Active Powers, Essay I. ch. iv; Hamilton's Supplementary Dissertations to Reid's Works, Note A, § 3, Note Q; Hamilton's Lectures on Metaphysics, Lectures XXXIX, XL; James Mill's Analysis of the Phenomena of the Human Mind, ch. xi; Mill's Logic, Book III. ch. iii-v, xxi; Mansel's Prolegomena Logica, ch. v; Mansel's Metaphysics, Section on Necessary Truths; Mill on Hamilton, ch. xvi; Lewes' History of Philosophy, Article on Kant; Bain's Moral and Mental Science, Book II. ch. vi, with Appendix B; Herbert Spencer's Principles of Psychology. The student, in employing these references, must be careful to distinguish between what relates to the Law of Universal Causation (sometimes called the Principle of Causality) and the Law of the Uniformity of Nature. The two Laws, as already noticed, are not always distinguished with sufficient care.

²⁷ In Sir W. Hamilton's edition of Stewart's Works, the corresponding reference is Part II. Subdivision I. ch. ii. section 4, subsection 2.

CHAPTER II.

Of Processes subsidiary to Induction.

OF the various mental processes subsidiary to Induction proper, it will be sufficient for our purpose to discuss Observation and Experiment, Classification (including Nomenclature and Terminology), and Hypothesis.

§ 1. Of Observation and Experiment.

These words are now so familiar, that they hardly require any explanation. To observe is to watch with attention phenomena as they occur, to experiment (or, to adopt more ordinary language, to perform an experiment) is, not only to observe, but also to place the phenomena under peculiarly favourable circumstances, as a preliminary to observation. Thus, every experiment implies an observation, but it also implies something more. In an experiment, I arrange or create the circumstances under which I wish to make my observation. Thus, if two bodies are falling to the ground, and I attend to the phenomenon, I am said to observe it, but, if I place the bodies under the exhausted receiver of an air-pump, or cause them to be dropped under any special circumstances whatever, I may be said not only to make an observation, but also to perform an experiment. Bacon

has not inaptly compared experiment with the torture of witnesses. Mr. Mill distinguishes between the two processes, by saying that in observation we find our instance in nature, in experiment we make it, by an artificial arrangement of circumstances. 'When, as in astronomy, we endeavour to ascertain causes by simply watching their effects, we observe; when, as in our laboratories, we interfere arbitrarily with the causes or circumstances of a phenomenon, we are said to experiment.'

As Observation often involves little or no conscious effort, while Experiment always implies an artificial arrangement of circumstances, it might be expected that the general employment of the former for scientific purposes would long precede that of the latter. And this supposition is confirmed by the History of Science. Though it is false to affirm that Experiment was never employed by the Greeks⁵, its general neglect was certainly one cause of the little progress made by them in the physical sciences.

In the attempt to ascertain the effect of a given cause, there can be no question of the general superiority of

^{1 &#}x27;Quemadmodum enim in civilibus ingenium cujusque, et occultus animi affectuumque sensus, melius elicitur, cum quis in perturbatione ponitur, quam alias: simili modo, et occulta naturæ magis se produnt per vexationes artium, quam cum cursu suo meant.' Nov. Org., Bk. I. Aph. xcviii.

² Thomson and Tait's Natural Philosophy, vol. i. § 369.

For a refutation of this popular misconception, see Mr. Lewes' work on Aristotle, ch. vi. Mr. Lewes, however, seems to me not sufficiently to recognise the slight extent to which Experiment was employed in ancient as compared with modern times.

Experiment over Observation. To be able to vary the circumstances as we choose, to produce the phenomenon under investigation in the precise degree which is most convenient to us, and as frequently as we wish, to combine it with other phenomena or to isolate it altogether, are such obvious advantages that it is not necessary to insist upon them. Without the aid of artificial experiment, it would have been impossible, for instance, to ascertain the laws of falling bodies. To disprove the old theory that bodies fall in times inversely proportional to their weights, it was necessary to try the experiment; to be able to affirm with certainty that all bodies, if moving in a non-resisting medium, would fall to the earth through equal vertical spaces in equal times, it was essential to possess the means of removing altogether the resisting medium by some such contrivance as that of the air-In some of the sciences, such as Chemistry, the Sciences of Heat, Light, and Electricity, it is next to impossible, at least in their inductive stage, to advance a single step without the aid of Experiment. . No amount of mere Observation would ever have enabled us to detect the chemical elements of which various bodies are composed, or to ascertain the effects of these elements in their pure state. Even when Observation alone reveals to us a fact of nature, Experiment is often necessary in order to give precision to our knowledge. That the metals are fusible, and that some are fusible at a lower temperature than others, is a fact which we can conceive to have been obtruded upon man's observation,

but the precise temperature at which each metal begins to change the solid for the liquid condition could be learned only by artificial experiment.

But, though, in ascertaining the effect of a given cause, Experiment is a far more potent instrument than Observation, the latter process is also available, and is • frequently of the greatest service. Thus, the Science of Medicine equally avails itself, for this purpose, both of observations and experiments. The scientific physician will not only try the effects of different medicaments, different modes of diet, and the like, but he will also watch the effects on the organic system of various occupations, habits, and pursuits. In some cases even, as in all astronomical and many physiological phenomena, the only means open to us of ascertaining the effect of a given cause is Observation. If we wish to ascertain the various phenomena attendant on a shower of meteors or a total eclipse of the sun, we must wait till the shower of meteors occurs or the total eclipse takes place. we wish to learn the effects of the lesion of a particular part of the nervous system, we must generally wait till an instance offers itself; there are many experiments too dangerous and too costly to be made, at least in the case of man.

While, however, both Observation and Experiment are available in ascertaining the effects of a given cause, in the reverse process of ascertaining the cause of a given effect, Observation alone is open to us. 'We can take a cause,' says Mr. Mill, 'and try what it will

produce; but we cannot take an effect, and try' [that is, experimentally] 'what it will be produced by. We can only watch till we see it produced, or are enabled to produce it by accident.' In those cases, consequently, in which effects alone are patent to us, and the causes are concealed from our view, we are compelled, unless we are able to reverse the problem in the manner noticed in the next paragraph, to have recourse to Observation. A new disease makes its appearance: the mode of its action, and the conditions favourable or unfavourable to its diffusion, can only be learned by a careful observation and comparison of cases.

It should, however, be noticed that the problem of finding the cause of a given effect is, in practice, as, for instance, in many cases of chemical analysis, often reversed, and that, by setting in action a variety of causes, we try to discover whether any one of them will produce the effect in question. Experiment is thus substituted for Observation.

It will readily be seen that those Sciences which depend wholly or mainly on Observation are, as inductive sciences, at a great disadvantage compared with those in which it is possible largely to employ Experiment. Where we wish to ascertain the effect of a given cause, and we cannot make the instances for ourselves, the want of appropriate and definite instances will often completely baffle us. And, though the cause of a given effect can only be learned by Observation, this is generally an enquiry of extreme difficulty, requiring to be

supplemented by experiment, or the actual production of the given effect by the supposed cause, before we can be certain that it has been conducted with the required accuracy. Thus, mere observation of the electrical phenomena which we witness in the heavens could never have given us the Science of Electricity. The experiments which we may conduct in an hour are often worth a century spent in observations.

In the Science of Astronomy this defect is more than compensated by the extreme simplicity of the phenomena, the heavenly bodies being regarded by us, not in themselves, but only in their mutual relations. Hence, we are, at a comparatively early stage, enabled to apply the Deductive Method, and to solve the problems of Astronomy by mathematical calculations. But in the very complex Science of Physiology this resource is not open to us, and hence the backwardness of those departments of physiological science in which direct experiment is not available. Any animal or vegetable organism is so complex, the data are so numerous, and bear to each other so many different relations, that, hitherto, it has been found impracticable to subject physiology, at least in any detail, to a deductive treatment. In social and political speculations, the want of experiment is, to some extent, supplied by statistics. social or political experiment is generally as impracticable as an experiment in physiology, and the danger with which it is attended is often incomparably greater. But the number of observations open to us in these

enquiries (as, for instance, in respect to crime, education, trade, taxation, &c.) is often very large, and, by carefully comparing and systematising them, we may frequently detect some relation between two circumstances which enables us, with great probability, to infer that one has something to do with the production of the other. I am here, however, trenching on the province of those chapters which treat more peculiarly of inductive inference.

The following Rules may be laid down for the right conduct of Observations and Experiments:—

Rule I. They must be precise. It is often of the utmost importance to notice the exact time at which an event occurs, the length of its duration, the position of an object in space, its relation to surrounding objects, and the like. We are all acquainted with the prime importance of precision of detail in legal evidence; it is no less indispensable in scientific research. For the purpose of enabling us to attain this object, various instruments and methods have been invented. As instances of these devices may be given, amongst instruments, the telescope, the microscope, the thermometer, the barometer, measures of various kinds, the balance, the dial, the clock, the watch, the chronometer, the vernier, the goniometer, the galvanometer, the thermo-electric pile; amongst methods, the decimal system of notation, fractions both vulgar and decimal, the divisions of time, the various contrivances for the measurement of space, the method of double-weighing, the method of least

squares, the personal equation in astronomical observations. To these instances might be added numerous others, but these will be sufficient to show the great aid derived by what may be called the natural methods of observation from artificial contrivances. The Thermometer and the Method of Double-Weighing furnish such striking exemplifications of the assistance thus afforded, that, though they are probably familiar to most of my readers, it may be desirable to explain them, one as an example of an instrument, the other of a method.

The Thermometer (it is not necessary here to describe the different kinds of thermometers) is a contrivance for determining the degree of temperature, irrespective of the mode in which it affects individual organisms. As our sensibility varies considerably under different circumstances, so that what at one time affects us with the sensation of hot will at another affect us with that of cold, the sense of touch cannot be depended upon for giving us accurate measurements of temperature. But the fact that, while the pressure remains unaltered, an augmentation of temperature, with certain rare exceptions (to be noticed hereafter), expands the bodies subject to its influence furnishes us with such a means of measurement. We take a substance which notably exemplifies the power of heat in expansion, such as mercury, alcohol, or, where it is necessary to ensure great precision, atmospheric air carefully prepared, and, by confining it within a tube, and marking off a scale of measurements along the side, we are enabled, by noting the degree of expansion of the substance in the tube, to estimate, at least approximately, the degree of temperature in the atmosphere or any other body, the conditions of which we are investigating.

The method of Double-Weighing is peculiarly simple and ingenious. It is a contrivance for remedying any possible inequality in the effective arms of the beam of the Balance. The body to be weighed is placed at one end of a balance, and is exactly balanced by another body placed at the other end; the first body is then removed, and its place supplied by a standard weight or weights, till these exactly balance the second body; we are thus, on the principle that things which are equal to the same thing are equal to one another, assured of the precise equivalence in weight of the body to be weighed and the standard weight or weights, provided, of course, that we can depend on the instrument giving the same results in successive weighings.

It frequently happens, however, that a single observation may greatly mislead us. I may be in a district at one time, and find the air very temperate and agreeable; the next time I come, it may be peculiarly hot, or chill, or moist. I may see a man, at the first shot, hit his mark; but, at the subsequent shots, he may fire very wide of it. Hence the importance, whenever there is any liability to error, of taking an average of observations. If a sufficient number of observations be taken, there is every probability that an error in one direction will be compensated by an error in the other, and that an average, derived from all the observations, will approximate much more nearly to the truth than any single observation is likely to do. Thus, if I wish to ascertain the true character of the climate at any particular place, the observations I consult must extend over a considerable number of years; if I wish to estimate truly the skill of the marksman, I must watch, not a single shot, but many successive ones. The average, it is true, is liable to error, but any single observation is much more so. There is hardly any department of science, depending upon observation, in which, if it be our object to obtain precision, this method is not indispensable 4.

Rule II. But, though it is necessary to be precise in our observations and experiments, it is also important, in order to avoid distraction and waste of time, to attend only to the material circumstances of the case we are investigating. A physician, for instance, in prescribing for his patient, would not now think it necessary to take an observation of the planets, nor would a chemist, in gathering herbs for his decoctions, think it of any consequence to notice the phase of the moon. A caution should, however, be added. Before neglecting any circumstance in our observations, it is of the utmost im-

^{*} The student who may wish for further information in connexion with Rule I. is referred to Dr. Whewell's Novum Organon Renovatum, Bk. III. ch. il., and Herschel's Discourse on the Study of Natural Philosophy, § 387-9. On the importance of taking an average of observations, see Herschel's Discourse, § 226-30.

portance to have ascertained beyond doubt that it is not material to the subject of our enquiries. To neglect this caution would be a violation of the first Rule.

Rule III. The circumstances under which an observation or experiment is made should, except in the very simplest cases, be varied as much as possible. A physician, in studying the character of a disease, wi'l note its effects on persons of different ages, constitutions, habits of life, and the like. An astronomical observer will not be content with a single observation of a newlydiscovered comet, but will note the phenomena which attend it at various stages in its passage through the heavens. A chemist will combine a newly-discovered element with the various other elements, and will try upon it the effect of heat, pressure, &c. It is, of course, implied that some discretion will be employed in the application of this Rule, and that the variation of circumstances will not be carried beyond the point at which there is some probability of its adding to our knowledge.

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The neophyte in science requires to be reminded that observations which might at first be supposed to be immaterial are often afterwards found to be amongst the circumstances most material to the enquiry. 'Could anything' (says Dr. Rolleston, in his Address before the Medical Association in 1868) 'have seemed at first sight to be more impertinent, more otiosely curious and trifling, than to enquire during an epidemic of cholera what was the nature of the subsoil in the area it was ravaging, to what depth it was porous, and at what level the water was, and had been previously, standing in it? Yet, as I think, Von Pettenkofer has at last fought out and won his battle on these points.'

Rule IV. The phenomenon under investigation should if possible be isolated from all other phenomena, or, at least, from all those which are likely to interfere with our study of it. In studying the effects of the action of gravity upon bodies, it was necessary to exhaust the atmosphere and to withdraw the support, and, by thus isolating the phenomenon, to enable us to perceive how bodies behave when subject to the action of gravity only. A physician, in trying the effects of a new drug, will, at first at least, administer it alone, and not in combination with other drugs which might augment or counteract its influence on the system.

A beautiful instance of the isolation of a phenomenon is afforded whenever there occurs a total eclipse of the sun. As, on these occasions, the moon, by a curious coincidence, exactly covers, or rather more than covers, the sun's surface, and thus intercepts all light from it, we are able to see certain rose-coloured protuberances, projecting, as it were, from the dark edge of the moon, but, in fact, proceeding from the sun. The real nature of these 'red flames' was long a matter of dispute, but it seems now to be conclusively settled that they are portions of an atmosphere of incandescent hydrogen in which the sun is enveloped, and which often shoots out

[•] By observing the third of these rules we usually prepare our instances for the application of what will hereafter be explained as the Method of Agreement, and by observing the fourth for the application of what will hereafter be explained as the Method of Difference.

in these flames to distances estimated, on one or two occasions, at no less than 300,000 miles. They can now be seen, whenever the sun is shining, by means of the spectroscope; but had it not been for the isolation of the phenomenon thus produced by the intervention of the moon, astronomers would have till quite recently been ignorant of its existence. Here, to use a bold metaphor, we might say that Nature herself performs an experiment for us.

When it is impossible entirely to isolate a phenomenon, it is sometimes possible so far to diminish the action of the concomitant circumstances as to be able accurately or approximately to calculate what would be the effect, if they were altogether absent. Thus, we can never altogether remove the influence of friction on a moving body, but we can so far diminish it as to be able to say what the effect would be were no such influence at work. We cannot altogether eliminate the influence of extraneous circumstances on a patient subject to medical régime, but, by due care, we may minimise the excitement, fatigue, ennui, or other unfavourable conditions which might interfere with our treatment.

The circumstances under which we perform our experiments being more in our own power than those under which we conduct our observations, it is obvious that the foregoing rules, and especially the third and fourth, can be more easily observed in experiments than in observations.

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⁷ See Young on the Sun, p. 202.

§ 2. On Classification, Nomenclature, and Terminology.

(1) OF CLASSIFICATION.

A classification, in the widest sense of the term, is a division, or a series of divisions and subdivisions. The process of classifying our own thoughts or feelings, or the actions of ourselves or others, or the external objects which surround us, is one of the most constant occupations of the mind. Thus, we are perpetually dividing outward objects into those which are useful or those which are useless or noxious to us; those which are useful into such as are within and such as are beyond our power to attain; those which are useful and which it is within our power to attain into such as are to be sought at once, and those the effort to appropriate which may be more advantageously postponed, -each of these divisions admitting of almost infinite subdivision. In fact, as has frequently been remarked, every attribution of a general name implies an act of division or classification. When we speak of a horse, we are dividing all objects into those which are horses and those which are not. When we speak of a bay horse, we are superadding to this division the subdivision of horses into bay horses and those of any other colour.

But the process of Classification of which I am about to treat, though the same in kind with that which we employ in the affairs of ordinary life, is of a much more complex and systematic character. The great difference is that, whereas in the affairs of ordinary life we generally

^a See Deductive Logic, Part II. ch. viii.

classify objects with reference to some one principle, that principle varying according to the particular purpose we happen to have in view (thus we classify horses according to their colour, their breed, their strength, &c., each classification being suggested by some distinct purpose), a scientific classification must take account of all the points of difference which are in any way likely to facilitate the scientific investigation of the group. The purport of the science being defined, the classification must be based, not on one or two characters, selected arbitrarily, but on the entire assemblage of characters which the science investigates. Thus, if Botany be defined as the science which investigates the organisation (including under that term the form, structure, and functions) of plants, a botanical classification, in order to be strictly scientific, must not omit to take into account any part of that organisation. But it is evident that such a requirement would produce endless confusion, unless we could discover some mode of subordinating the characters, so as to make the more important points of difference the basis of the higher divisions in the series. Hence we see already that a scientific classification must be guided by at least two principles, a review of all the characters or distinguishing marks, so far as they are known and so far as they fall within the scope of the science, and a subordination of these characters one to another. To these principles others will subsequently be added.

Before proceeding to the attempt to ascertain induc-

tively facts of co-existence or causation amongst a vast mass of phenomena, it is often highly important, if not essential, to arrange these phenomena in groups, as well as to determine the order in which these groups themselves shall be arranged. Hence the importance of laying down correct rules for Classification in a System of Inductive Logic. It is exclusively as subsidiary to Induction that I shall here consider the subject of Classification*.

A scientific Classification, regarded as subsidiary to Induction employed for scientific purposes, may be defined as A Series of Divisions, so arranged as best to facilitate the complete and separate study of the several groups which are the result of the divisions, as well as of

* It will probably occur to the student that the materials for Classification can themselves only be obtained by Induction. And this is true. All Classification implies the prior employment of an Inductio per Enumerationem Simplicem, by which we establish the fact of the co-inherence of certain attributes. But these 'inductions of co-existence' (see pp. 7-9), which precede our classifications, are altogether of a different order from the 'inductions of causation' which it is the ultimate aim of science to establish. and to which I regard Classification as mainly subordinate. I say 'mainly subordinate,' for, of course, there is no doubt that, when, by means of certain 'inductions of co-existence,' we have constituted a class, we are in a more favourable position than before for detecting additional facts of co-existence among the associated phenomena.

When, from a wide experience, I find that the attributes a, b, e, d, e invariably co-exist in the same objects, I generally constitute these objects into a class, and designate them by a class-name. The name thus serves to recall the fact of the co-inherence of the attributes, and I am far more likely, than if I had never made the classification, to discover the co-existence with the other five of some sixth attribute, say f, or to be able to trace some causal connexion between, say, a and b, or a, b, and c.

the entire subject under investigation. 'The general problem of classification,' says Mr. Mill', 'in reference to these [namely, scientific] purposes may be stated as follows: To provide that things shall be thought of in such groups, and those groups in such an order, as will best conduce to the remembrance and to the ascertainment of their laws.'

The sciences of Botany and Zoology are rightly regarded as furnishing the best examples of Scientific Classification. The excellence of the classifications which they present may be referred to two reasons. The first is the extraordinary multiplicity of the different kinds of animals and plants which are found on the surface of the globe: this fact has, from the earliest times, exercised man's ingenuity in the attempt to name them and reduce them to order. The second reason may be found in the imperfection of these sciences in their present condition: the difficulty of discovering laws of succession, or, in other words, relations of cause and effect, in the animal and vegetable kingdoms has naturally led scientific enquirers to concentrate their attention on the far easier task of describing and arranging the objects themselves. Mineralogy, though its classifications are less systematic and complete, is also, in the present state of the science, mainly occupied in attempting the work of classification.

The best means, perhaps, of making the student acquainted with the nature of scientific classification is to compare the method of natural classification (which aims

[&]quot; Mill's Logic, Bk. IV. ch. vii. § 1.

at being strictly scientific) with that of artificial classification (which, so far as it is artificial, is not scientific), giving illustrations from the sciences of Botany and Zoology. An examination of the natural system will enable us to lay down certain rules for scientific classification, and I shall conclude with such remarks as may seem necessary in order to preserve the student from erroneous impressions.

A natural system of Classification aims at classifying objects according to the whole of their resemblances and differences, so far as these are recognised by the science in whose service the classification is made. But amongst these resemblances and differences some are found to be invariably attended by a number of others, and consequently these, as the more important, are selected as the characters by which to discriminate the higher divisions of the series, the less important characters being, throughout the whole series, subordinated to the more important. This successive subordination of characters and the consequent coincidence of the groups formed by our classifications with what appear to be the great divisions of nature are the peculiarities which mainly distinguish a natural system. An artificial system, on the other hand, is one which selects arbitrarily some point of difference amongst the objects to be classified, and then, so far as possible, makes this or similar points the basis of its classifications. No system, however, as we shall see presently, is purely artificial. Though of little use, except as a preliminary effort, for the purposes of science, an artificial system possesses one great advantage. As it bases its divisions, where possible, on some one property, and that generally something which at once strikes the eye (one of the earliest of the modern attempts to classify plants took for its basis the form of the corolla), it is peculiarly easy of application, and can be much more readily learnt than a natural system. It thus often serves the purposes of a key, by which we may easily discover the place of a group in a natural system. I now proceed to offer illustrations.

In Botany, the most celebrated artificial system is that known as the Linnæan, though Linnæus also did much towards the establishment of a natural system. In this system, which was a great advance on preceding artificial systems, the main basis of classification is the number of stamens and pistils which are to be found in the flowering plant. This character is, however, to some extent modified by other considerations, such as the relative lengths of the stamens, the shape of the fruit, &c.; so far as these modifications are admitted, the Linnæan system approaches to a natural system. The annexed Tables (extracted from Balfour's Manual of Botany 11) will give the student some idea of the manner in which the Classes (higher divisions) and the Orders (divisions intermediate between the Classes and Genera) are constituted according to the Linnæan system. It should be premised that the stamens are the male organs, and the pistils the female organs of a plant.

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¹¹ §§ 716, 717.

TABULAR VIEW OF THE CLASSES OF THE LINNZEAN SYSTEM

- A. Flowers present, or evident Stamens and Pistils (Phanerogamia).

 I. Stamens and Pistil in every flower.
 - 1. Stamens free.
 - a. Stamens of equal length, or not differing in certain proportions;

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|--|----------|---------------|--|--|--|--|
| in number I | Class I. | Monandria. | | | | |
| 3 3 | 11. | Diandria. | | | | |
| — 3 | III. | Triandria. | | | | |
| - 4 | IV. | Tetrandria. | | | | |
| — <u>5</u> | v. | Pentandria. | | | | |
| 6 | VI. | Hexandria. | | | | |
| – 7 | VII. | Heptandria. | | | | |
| - 8 | | Octandria. | | | | |
| - 9 | IX. | Enneandria. | | | | |
| — IO | X. | Decandria. | | | | |
| | XI. | Dodecandria. | | | | |
| - 20) inserted on Calyx- | XII. | Icosandria. | | | | |
| or more on Receptacle | | Polyandria. | | | | |
| Stamens of different lengths; | | - | | | | |
| two long and two short | XIV. | Didynamia. | | | | |
| four long and two short | XV. | Tetradynamia. | | | | |
| 2. Stamens united; | | | | | | |
| by Filaments in one bundle | XVI. | Monadelphia. | | | | |
| ——in two bundles | XVII. | Diadelphia. | | | | |
| in more than two bundles | XVIII. | Polyadelphia. | | | | |
| by Anthers (Compound flowers) | XIX. | Syngenesia. | | | | |
| with Pistil on a Column | XX. | Gynandria. | | | | |
| II. Stamens and Pistil in different flowers; | | | | | | |
| on the same Plant | XXI. | Monœcia. | | | | |
| on different Plants | XXII. | Diœcia. | | | | |
| III. Stamens and Pistil in the same or in different flowers on the same or on different Plants | XXIII. | Polygamia. | | | | |
| B. Flowers absent, or Stamens and Pistils and evident | XXIV. | Cryptogamia. | | | | |
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The Classes are sub-divided into Orders, as will be seen from the next Table, on a less uniform plan than that on which they were themselves constituted.

TABULAR VIEW OF THE ORDERS OF THE LINNAEAN SYSTEM.

| Class I. \ | Monogynia ¹² I Free Style. |
|------------|---|
| II. | Digynia 2 Free Styles. |
| TIT: | Trigynia 3 |
| IV. | Tetragynia 4 — |
| V. | Pentagynia 5 — |
| VL | Hexagynia 6 |
| VII. | ≻Heptagynia |
| VIII.] | Octogynia 8 |
| 1X. | Enneagynia |
| X. | Decagynia 10 — |
| XI | Dodecagynia 12-19 |
| XII. | Polygynia 20 and upwards. |
| XIIL | |
| VIII | Gymnospermia Fruit formed by four Achsenia. Angrospermia Fruit, a two-celled Capsule with |
| XIV. | Angiospermia Fruit, a two-celled Capsule with |
| | many seeds. |
| XV. | Siliculosa Fruit, a Silicula. Siliquosa Fruit, a Siliqua. |
| | _ |
| XVI. | Triandria, Decandria, &c. (number of Stamens), as in |
| XVII. | Classes |
| XVIII. | |
| | Polygamia Æqualis Florets all hermaphrodite. |
| | — Superflua Florets of the disk hermaphro- |
| _ | dite, those of the ray pistilli- ferous and fertile. |
| | Frustranea Florets of the disk hermaphro- |
| XIX. | dite, those of the ray neuter. |
| • | Necessaria Florets of the disk stammiferous, |
| | those of the ray pistilliferous. |
| | Segregata Each floret baving a separate |
| | involucre. |
| | Monogamia |

¹² It must not be supposed that all the Orders, Monogynia, &c., exist in each of the first thirteen Classes. When an Order is absent, the next Order which is present takes its place in the numerical arrangement. Thus, if the Order Trigynia be absent, and the next Order which is present be Tetragynia, as in Class IV, this latter will rank as the third Order.

| XX. XXI. XXII. | Monandria, Diandria, &c. | (number of Stamens), as in the Classes. | | |
|----------------------|--------------------------|--|--|--|
| XXIII. | Monœcia | Hermsphrodite, staminiferous and pistilliferous flowers on the same plant. on two plants. on three plants. Ferns. Mosses. Liverworts. Lichens. Sea-weeds. Mushrooms. | | |
| | Dicecia | on two plants. on three plants. | | |
| XXIV | Kilices | Ferns. Mosses. | | |
| | Lichenes | . Liverworts. . Lichens. | | |
| | Fungi | Mushrooms. | | |

'Even as an artificial method,' says Professor Balfour15, 'this system has many imperfections. If plants are not in full flower, with all the stamens and styles perfect, it is impossible to determine their class and order. In many instances, the different flowers on the same plant vary as regards the number of the stamens. Again, if carried out rigidly, it would separate in many instances the species of the same genus; but, as Linnæus did not wish to break up his genera, which were founded on natural affinities, he adopted an artifice by which he kept all the species of a genus together. Thus, if in a genus nearly all the species had both stamens and pistils in every flower, while one or two were monœcious or dicecious, he put the name of the latter in italics, in the classes and orders to which they belonged according to his method, and referred the student to the proper genus for the description.'

The species of the Linnauan system coincide with those of the natural system. The same is mostly the case with

¹¹ Balfour's Manual of Betany, § 718.

system is, therefore, far from being purely artificial. In fact, when we come to the lower groups of vegetables (genera and species), we are compelled to discriminate them one from another by a multiplicity of characters, so that a purely artificial system of botany would be impossible.

The framers of natural systems of botany, instead of selecting some one character, such as the number of stamens and pistils, as the basis of the higher divisions, attempt to discover a number of characters, any one of which, if employed as the instrument of division, would give the same results as any of the others. This coincidence of divisions founded on various characters is a proof that we have reached some real distinction in nature. The main division of plants into cellular and vascular, or acotyledonous and cotyledonous, and the sub-division of vascular or cotyledonous plants into monocotyledonous and dicotyledonous, furnish remarkable instances of such a coincidence, and may consequently be regarded as corresponding with grand divisions in nature itself.

'In taking a survey of the Vegetable Kingdom, some plants are found to be composed of cells only, and are called *Cellular*; while others consist of cells and vessels, especially spiral vessels, and are denominated *Vascular*. If the embryo is examined, it is found in some cases to have cotyledons or seed-lobes, in other cases to want them; and thus some plants are *cotyledonous*, others

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acotyledonous; the former being divisible into monocotyle-donous, having one cotyledon, and dicotyledonous, having two [or more] cotyledons. The radicle, or young root of acotyledons, is heterorhizal, that of monocotyledons is endorhizal, that of dicotyledons, exorhizal. When the stems are taken into consideration, it is seen that marked differences occur here also, acotyledons being acrogenous, monocotyledons endogenous, and dicotyledons exogenous. The venation of leaves, parallel, reticulated, or forked, establishes the same great natural divisions; and similar results are obtained from a consideration of the flowers, monocotyledons and dicotyledons being phanerogamous and acotyledons cryptogamous.'

'Thus, the following grand natural divisions are arrived at:-

- 1. Cellular...Acotyledonous. Heterorhizal. Acrogenous. Cryptogramous.
- 2. Vascular. | Monocotyledonous. Endorhizal. Endogenous. | Phanero-Dicotyledonous. Exorhizal. Exogenous. | gamous. |

Having established these Primary Divisions of the vegetable kingdom, the botanist, guiding himself as far as possible by the same principles as those on which the primary divisions were formed, proceeds to divide and sub-divide till at last he arrives at species, which are usually defined to be collections of individuals so nearly resembling each other that they may be supposed to be descended from a common stock. Thus, the Class 'Dicotyledones or Exogenæ' is sub-divided into four

¹⁴ Balfour's Manual of Batany, §§ 723, 724.

sub-classes, one of which is the 'Thalamifloræ,' characterised as having 'calyx and corolla present, petals distinct and inserted into the thalamus or receptacle, stamens hypogynous.' This sub-class is divided into a number of orders (sixty in Professor Balfour's Manual), one of which is Hypericaceæ, the Tutsan or St. John's-wort family, thus described:—

* 'Sepals 4-5, separate or united, persistent, usually with glandular dots, unequal; sestivation imbricated. Petals 4-5, oblique, often with black dots, sestivation contorted. Stamens bypogynous, indefinite in number; generally polyadelphous, very rarely 10, and monadelphous or distinct; filaments filiform: anthers bilocular, with longitudinal dehiscence; carpels 2 5, united round a central or basal placenta; styles the same number as the carpels, usually separate; stigmas capitate or simple. Fruit either fleshy or capsular, multilocular, and multivalvular, rarely unilocular. Seeds usually indefinite in number, minute, anatropal, usually exalbuminous; embyro usually straight.—Herbaceous plants, shrubs, or trees, with exstipulate entire leaves, which are usually opposite and dotted. Flowers often yellow.'

In this order there are fifteen known genera, one of which is the Hypericum, which is thus described in Irvine's *Handbook of British Plants*:—

'Hypericum, St. John's-wort. Herbaceous plants or shrubs, with opposite simple, entire leaves, which are usually furnished with pellucid dots (reservoirs of essential oil). Sepals five, free or united at the base, ovate, slightly unequal, permanent. Petals as many as the sepals, obtuse, spreading. Stamens indefinite, combined at the base into three or five sets, with small roundish anthers. Ovary with three-five cells or carpels and as many styles, with simple stigmas. Fruit capsular, rarely baccate, three-five-celled, with numerous seeds.'

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This genus is divided into sub-genera or sections, one of which is thus described:—

'Stems herbaceous. Stamens in three parcels (triadelphous). Styles three. Capsule three-celled, three-valved.'

The sub-genus or section is again divided into subsections, one of which is characterised as having 'stems round, sepals with ciliary glands.' This sub-section contains amongst its species the well-known Hypericum Pulchrum, 'Elegant St. John's-wort,' thus described:—

'Stems erect, bent at the base, round, glabrous, simple or branching. Leaves ovate, clasping, corriaceous, smooth, with numerous translucent dots. Flowers in opposite panicled cymes. Sepals obsvate, roundish, with a point, ciliated, with nearly sessile glands. Petals oblong, ribbed, with black sessile glands 18.

The first peculiarity which strikes us in these descriptions is the large number of characters which is employed in constituting even the higher divisions of the series. Instead of describing merely the number and distribution of the stamens, as in the Linnæan system, we have, even in the description of the Order, a reference to almost every part of the plant. We next notice the much greater definiteness which the characters assume, as we descend lower in the series. Thus, to take the sepals as an instance, the description of the sub-class simply informs us of the presence of a calyx, while each successive division (except the sub-genus) gives us more and more definite information as to the number, position, form, &c. of the sepals which constitute the calyx.

¹⁶ See Irvine's Handbook of British Plants, under Order CIII.

Again, we observe that, in the lower divisions, the stem, leaves, sepals, and petals are the characters which are brought into greatest prominence, whereas the stamens and the various parts of the pistil (the carpels, styles, and stigmas), which are employed in the higher divisions, disappear from the lower, as no longer affording grounds of difference. Now the stamens and pistil, inasmuch as any peculiarity in them is generally accompanied by a larger number of peculiarities in other parts of the plant, are usually of far more importance than the corolla (petals) and calyx (sepals), and therefore it is reasonable to suppose that the grounds of difference furnished by them would be likely to be exhausted in the higher divisions. At the same time we see that, in the instance we have taken, the sepals and petals furnish grounds of difference at a very early stage of the classification, and consequently that even the less important characters are often used concurrently with others to determine the higher divisions.

In Zoology, the advantage of a natural over an artificial classification is more readily recognised than in Botany, the structure and functions of animals being more familiar and apparent than those of plants. A division of animals, for instance, which adopted the number of limbs as its sole distinguishing character, and thus brought together, as quadrupeds, the ox and the frog, would be so absurd on the face of it, as to be rejected at once. 'No arrangement of animals,' says Dr. Whewell 16, 'which, in

¹⁴ History of the Inductive Sciences, Bk. XVI. ch. vii.

a large number of instances, violated strong and clear natural affinities, would be tolerated because it answered the purpose of enabling us easily to find the name and place of the animal in the artificial system. Every system of Zoological arrangement may be supposed to aspire to be a natural system.' He then proceeds to give an instance of an attempt to constitute an artificial classification in the ichthyological branch of Zoology. 'Bloch, whose ichthyological labours have been mentioned, followed in his great work the method of Linnæus,' (who devoted much of his attention to the classification of animals as well as of plants). 'But towards the end of his life he had prepared a general system, founded upon one single numerical principle—the number of fins; just as the sexual system of Linnæus is founded upon the number of stamina: and he made his sub-divisions according to the position of the ventral and pectoral fins; the same character which Linnæus had employed for his primary division. He could not have done better, says Cuvier, if his object had been to turn into ridicule all artificial methods, and to show to what absurd combinations they may lead.'

'By the natural method,' says M. Milne Edwards 17 (whose remarks on Zoological Classifications and the Primary Divisions and Classes of the Animal Kingdom

¹⁷ See Milne Edwards' Zoologie (in the Cours élémentaire d'histoire naturelle), septième édition, §§ 364, 365. There is an English translation of this work by Dr. R. Knox. I have followed it, except in a few places where it does not accurately represent the original.

are well worthy of the attention of all students of inductive logic), 'the divisions and subdivisions of the animal kingdom are founded on the whole of the characters furnished by each animal, arranged according to their degree of respective importance; thus, in knowing the place which the animal occupies, we also know the more remarkable traits of its organisation, and the manner in which its principal functions are exercised.

'The rules to be observed in arriving at a natural classification of the animal kingdom are of extreme simplicity, but often there is much difficulty in the application. They may be reduced to two, for the object of the zoologist in establishing such a classification is,—

'1st. To arrange animals in natural series, according to the degree of their respective affinities,—that is to say, to distribute them in such a manner that those species which most nearly resemble each other may occupy the nearest places, while the distance of two species from each other may, in some sort, be the measure of their non-resemblance.

'2nd. To divide and subdivide this series according to the principle of subordination of characters,—that is to say, by reason of the importance of the differences which these animals present amongst them.'

The Primary Divisions of the animal kingdom, according to the natural system, are four, there being four types of structure and of nervous organisation, to which animal life conforms.

. These four principal forms may be understood by a

reference to four well-known animals-the dog, the crayfish or lobster, the snail, the asterias or sea-star.

'In order that the zoological classification might be a faithful representation of the more or less important modifications introduced into the structure of animals, it was necessary to distribute these beings into four principal groups or divisions; and this is, in fact, what Cuvier did.

'The animal kingdom is divided into vertebrate animals, articulated or annulated animals, molluscs, and zoophytes.

'The fundamental differences distinguishing these four primary divisions depend chiefly on the mode of arrangement of the different parts of the body and on the conformation of the nervous system. It is easy to understand the importance of these two dominant characters: to feel and to move is the especial character of animal life, and these two functions belong to the nervous system. It might readily, then, be anticipated that the mode of conformation of this system would exert a powerful influence over the nature of animals, and would furnish characters of primary importance in classification.

'The general disposition or mode of reunion of the different parts of the body exercises an equally important influence, as modifying the localisation of the functions and the division of the physiological result 18.1

Vertebrate animals are thus described:-

'The vertebrate animals resemble man in the more important points of their structure; almost all the parts of their bodies are

²⁰ Milne Edwards, §§ 372, 373.

in pairs, and disposed symmetrically on the two sides of a medial longitudinal plane; their nervous system is highly developed, and is composed of nerves and ganglions, and of a brain and spinal marrow. To these characteristics we may add that the principal muscles are attached to an internal skeleton, composed of separate pieces, connected together, and disposed so as to protect the more important organs, and to form the passive instruments of locomotion; that the more important part of this skeleton forms a sheath for the brain and spinal marrow, and results from the reunion of annular portions, called vertebrae; that the apparatus for the circulation is very complete, and that the heart offers at least two distinct reservoirs; that the blood is red; that the limbs are almost always four in number, and never more; finally, that there exist distinct organs lodged in the head for sight, hearing, smell, and taste 19.2

The Primary Division (embranchement) 'Vertebrate Animals' is sub-divided into the five classes, Mammals, Birds, Reptiles, Batrachia, Fishes, of which Mammals are thus described:—

'Organs of lactation. Hot blood. Circulation complete, and heart with four cavities. Pulmonary respiration simple. Lobes of the cerebellum reunited by an annular protuberance. Lower jaw articulated directly with the cranium. The body generally covered with hairs. Viviparous.'

'There exist considerable differences amongst the mammalia, and these modifications of structure serve as the basis for the division of the class into groups of an inferior rank, called *orders*. Most of these groups are so distinct as to admit of no doubt in respect of their limits: they constitute, in fact, natural divisions; but in others the line of demarcation is by no means so distinct.

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¹⁸ Milne Edwards, § 374.

Thus a mammal may have points of resemblance so close to two groups as to render it almost indifferent to which it be referred. To some naturalists, differences appear important which are disregarded by others, and hence a want of agreement on the subject of classification has always prevailed.

'The method followed here is nearly the same as that proposed by Cuvier. It rests mainly on the differences mammals show in respect of their extremities and teeth, differences which always imply a crowd of others in habits, structure, and even intelligence.

'Keeping in view the *ensemble* of these characters, the class mammalia may be divided into two groups,—the *monodelphic* and *didelphic*.

'The monodelphic or monodelphian are the more numerous, and are distinguished chiefly by their mode of development. At birth they are already provided with all their organs, and before birth they derive their nourishment from the mother by means of a placenta. Their brain is more perfect than the didelphian, by the presence of a corpus callosum uniting the two cerebral hemispheres. Finally, the walls of the abdomen have no osseous supports attached to the margins of the pelvis, as we find in the second great class of mammals. The mammals thus organised have been subdivided into two groups,—namely, ordinary mammals and pisciform mammals.

'The ordinary mammals are organised principally to live on solid ground; the skin is provided with hairs. These animals are further subdivided into ten orders: the bimana, quadrumana, cheiroptera, insectivora, rodentia, edentata, carnivora, amphibia, pachydermata, and ruminantia. The first eight of these orders have flexible fingers and toes, with nails covering only the dorsal aspect of the toe or finger, and comparatively small; hence they have been called unguiculata; the last two, -namely the pachydermata and ruminantia, have the extremity of the finger and toe entirely enclosed in a boof; they are thus called ungulata.

'The order bimana includes only man: in him alone the arms are destined for prehension, the limbs for progression and support in the erect attitude. Thus, his natural position on the soil is unmistakeably vertical. The teeth are of three kinds, and have their edges on the same plane; they are frugivorous: finally, the brain is more perfect, more highly developed, than in any other animal.'

Here the Order is co-extensive with the Species, but usually the Order is divided into Genera, and each Genus into Species. Thus, the Order 'Carnivora' is divided into the Genera 'cat,' 'hyæna,' 'dog,' 'bear,' &c. Again, the Genus 'dog' comprises the dog properly so called, the wolf, and the fox. The Genus 'cat' comprises not only the cat properly so called, but the tiger, lion, panther, &c.

It may be as well to add an account of the characters which distinguish respectively the Order 'Carnivora,' the

²⁶ Milne Edwards, §§ 409-412.

Genus 'Felis,' and the Species 'Leo,' in order to serve as an example or illustration of the manner in which these several degrees in the scale of Classification are usually described:—

'The order of carnivora is composed of ordinary unguiculated mammals; the form of their dentition is complete, but they have no opposing thumb. According to the mode of life of these animals, their intestinal canal is short; their jaws and their muscles strong, in order to seize and devour their prey; their head from this circumstance seems large. The jaws are short, thus favouring their strength, and the form of the temporal-maxillary articulation proves that the teeth are made for tearing and cutting, not for grinding or masticating. The canine teeth are large, long, and very powerful; the incisors, six in number in each jaw, small; the molars, sometimes adapted merely for cutting, in others surmounted with rounded tubercles, presenting no conical points, arranged as in the insectivors. One of these molar teeth is usually much longer and more cutting than the others, and has therefore been called the carnivorous molar tooth; behind these (on each side) are one or two molars, almost flat, and between the carnivorous molar and the canine a variable number of false molars. The food of the animal, whether exclusively composed of flesh or mixed with other matters, may be judged of by the varying proportions of these cutting or tuberculated molars.

'Animals of this order have generally the toes armed with claws adapted to hold and to tear their prey; usually also they have no collar-bones.'

The following are the characteristics of the genus 'Felis,' and of the species 'Leo':—

'Their jaws are short, and are acted on by muscles of extraordinary strength; their retractile nails, concealed between the toes in a state of repose by means of elastic ligaments, are never blunted. Their toes are five in number on the anterior limbs, and four on those behind. Their hearing is exceedingly fine, and the best developed of all their senses. They see well by day and night, but they are not far-sighted; in some the pupil is elongated vertically, in others it is round. They make great use of the organ of smell; they consult it before eating, and often when anything disturbs them. Their tongue is covered with horny and very rough points. Their coat is in general soft and fine, and the surface of the body very sensible to the touch; their whiskers especially seem to be instruments of great sensibility. Though of prodigious vigour, they generally do not attack animals openly, but employ cunning and artifice. They never push their prey to flight, but, watching by the margins of rivers and pools in covert, they spring at once on their victim.

'At the head of this genus stands the lion, measuring frequently twelve feet in length, or over six feet to the setting on of the tail; about three feet in height, and characterised by the square head, the tuft of hair terminating the tail, and in the male by the mane which flows from the head and neck."

The process by which the Zoologist constitutes the Primary Divisions of animal life, and then descends from these to the Species, is distinguished by the same peculiarities as those which we remarked in reviewing the natural classifications of the Botanist. In one step or other of the classification almost every known characteristic of a species will be found. As we descend the series, the characters gain in definiteness and, as a rule, lose in importance. Moreover, even in the higher divisions of the series, numerous characters are used, and those not always of great apparent importance. Thus, that 'the body is generally covered with hairs' is one of the characters of Mammalia.

The student will now be in a position to understand

²² Milne Edwards, § 414.

the rules which may be laid down for the right conduct of a Natural Classification.

I. Not only the lower, but the higher groups of the series should be so constituted as to differ from one another by a multitude of characters. It is only when, as is the case in the primary divisions of Botany and Zoology, we arrive at the same divisions from a variety of different considerations, that we can feel assured that our groups really correspond with distinctions in Nature. It is this coincidence, in the higher groups of the series, of divisions formed on different principles, that distinguishes a Natural from an Artificial Classification.

II. The more important characters should be selected for the purpose of determining the higher groups. is called the principle of the subordination of characters. But how are we to determine the relative importance of characters? 'We must consider as the most important attributes,' says Mr. Mill 22, 'those which contribute most, either by themselves or by their effects, to render the things like one another, and unlike other things; which give to the class composed of them the most marked individuality; which fill, as it were, the largest space in their existence, and would most impress the attention of a spectator who knew all their properties but was not specially interested in any.' This account is perfectly true, but it seems to be hardly sufficiently definite. The following criteria may be proposed for the purpose of discriminating between the more and the less important

²² Mill's Logic, Bk. IV. ch. vii. § 2.

properties of natural objects. (1) A character which is found to furnish an invariable index to the possession of certain other characters is of more importance than a character which furnishes no such index. Thus, the internal structure of an animal is of more importance than its size, and the mode of fructification of a plant than the colour of its flowers. (2) Amongst such characters, a character is regarded as of more or less importance, according as it accompanies a greater or smaller number of other differences. Thus, in the classification of animals, the characters from which the classes unguiculata and ungulata are so called are of more importance than the form of the teeth, which is used in distinguishing the orders. For the same reason, the mode of growth of flowering plants (which leads to the distinction of endogenous and exogenous plants) is of far more importance, as a character, than the number of stamens or pistils. Hence, in constituting the higher divisions of a series we must look for those characters which are accompanied by the largest number of differences.

III. The classification should be gradual, proceeding by a series of divisions and subdivisions. When the group to be classified consists of an enormous number of species, as in the case of animals and plants, the necessity of observing this rule is obvious. To descend at once from the Primary Divisions to, say, Genera and Species, would render the Classification comparatively worthless. The object of a classification being to bring together those groups which resemble each other and to

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separate those groups which differ from each other, we must take account of degrees of resemblance and difference, so that, as a rule, the number of gradations will increase with the number of groups to be classified. Both in Botany and Zoology, the grand divisions which seem now to be universally recognised are Primary Divisions, or Sub-Kingdoms (embranchements), Classes, Orders, Genera, and Species. Between these various other divisions are interpolated, according to the seeming requirements of each particular system, and often according to the views of each individual author. Moreover, below Species are often reckoned Varieties, and even Varieties are sometimes subdivided, this being especially the case when animals have become domesticated or plants cultivated. Taking as an instance the Anthyllis Vulneraria (Common Lady's Finger), the divisions and subdivisions of a natural classification may be illustrated thus *:-

| I. PRIMARY DIVISION | | | | | | Cotyledones. |
|---------------------|----|---|---|---|---|-----------------------|
| II. CLASS . | | | | | | Dicotyledones. |
| Subclass | | | | | | Calycifloræ. |
| III. ORDER . | | | | , | | Leguminosæ. |
| Suborder | | | | | | Papilionacen. |
| Tribe . | | | , | | | Loteæ. |
| Subtribe | | | | | - | Genisteæ. |
| IV. GENUS . | | | | | | Anthyllis. |
| Subgenus or Section | | | , | | | Vulneraria. |
| V. SPECIES | | | , | | | Vulneraria. |
| Variety | | | | | | Dillenii. |
| Race . | | | | | | Floribus eoccineis. |
| Variation | ٠. | • | | • | | Foliis hirsutissimis. |

Balfour's Manual of Botany, § 725.

³⁴ It is not uncommon in the classificatory sciences, as in this

In very extensive groups, other divisions may be interpolated; thus a subgenus or section is often divided into a subsection. On the other hand, many of these divisions often disappear; if a genus consist of only a small number of species, and there be no very striking points of difference amongst them, we may descend at once, without any intermediate divisions, from the Genus to its various Species. Sometimes, even, an order may contain only a single genus, or a genus a single species, in which case the two may be regarded as coextensive. In the case of Man, we saw that we descend at once from the Order to the varieties, the Order Bimana being coextensive with the genus and species Homo, so that here three even of the grand divisions are coincident.

IV. The groups should be so arranged, that those which have the closest affinities may be brought nearest to each other, while the distance of one group from another may be taken as a measure of their dissimilarity. The observation of this rule would result in what Mr. Mill calls 'the arrangement of the natural groups into a natural series.' For the purposes of subsequent induction, it is plain that it is of the utmost importance not widely to dissever groups which present many phenomena in common, or which we even suspect may do so. The object aimed at by this rule is, to a great extent, attained by the observation of the Subordination

instance, to assign the same name to a higher and lower division, the lower division exhibiting in a marked manner the characters possessed in common by the various members of the higher division. of Characters (Rule 2), according to which, the higher the place of the division in the series, the more important is the collection of characters which serves to constitute it. If Rule 2 were duly observed, it would be impossible for any two widely dissimilar groups to be brought into juxtaposition in the lower divisions of the series. Thus, the ox and the frog, the primrose and the mushroom, would in any natural system be at considerable distances from each other. But it is not sufficient to observe the rule of the Subordination of Characters. The arrangement of the cognate groups in each division should be such that at the head of the series may come those groups which are most like the groups of the preceding division, while at the bottom of the series may come those groups which are most like the groups of the subsequent division. Thus, suppose that we have Orders A, B, C, of which B resembles A more than C does, and that A is subdivided into the genera a' a'' a''' b'b''c; B into the genera m'm''nop'p''; C into the genera x' x" y', y", y"", z (of which the genera represented by the earlier letters of the alphabet are more akin to each other than those represented by the later, and conversely): in our arrangement we ought to place c in juxtaposition with m' m'', and p' p'' in juxtaposition with x' x'', the remaining groups being arranged, as above, on the same principle. If such an arrangement could be effected, it is plain that those groups which presented in the greatest intensity the principal phenomena of the class of objects under investigation would

come first in the series, and that those which presented them in the least intensity would come last. In Zoology, for instance, those groups would come first which presented in the greatest intensity the principal phenomena of animal life, and in Botany those which presented in the greatest intensity the principal phenomena of veget-It is, of course, seldom, in the arrangement of able life. natural objects, that we are able to draw up an exact table of precedence amongst the groups of any division, but we are often able to say that this or that group or collection of groups (a or a' a" a"') should rank first in the series, or that it should rank before some other group or collection of groups. Thus, no zoologist would hesitate to assign to man (the Order Bimana) the highest place in any classification of Mammalia, while he would place next the Order Quadrumana, and in this Order he would select apes, and, amongst apes, the anthropoid apes, to be brought into closest juxtaposition with man.

This rule is obviously of most difficult application. It points out an ideal to be aimed at, but one which is never likely to be perfectly realised. So many are the properties to be taken into consideration in every natural object, that it is often impossible to say that this object is, on the whole, more like another than that. The groups of the higher divisions may often, those of the lower may sometimes, be tabulated in some order of precedence; but there remains a large number of cases to which the rule is inapplicable, or to which, at least, it has not yet been successfully applied. This is especially

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the case in Botany, where, though, in respect of complexity of structure and perfection of organism, Vascular plants may be ranked above Cellular, and Dicotyledons above Monocotyledons, there are many cases among the subdivisions, especially of Monocotyledons and Dicotyledons, where no order of precedence can as yet be satisfactorily established. But, even if the rule were of universal application, and if we were perfectly acquainted with all the properties of bodies and their relative value, it would not follow that we could establish what Dr. Whewell, in his opposition to this doctrine of Classification by Series, calls 'a mere linear progression in nature.' There might still be many Orders, Genera, or Species, which, to use a familiar expression, we should be obliged to bracket. 'It would surely be possible,' says Mr. Mill 25, 'to arrange all places (for example) in the order of their distance from the North Pole, though there would be not merely a plurality, but a whole circle of places at every single gradation in the scale.'

Remark r. A natural classification is supposed to be complete, when it has descended as low as species,—a species being regarded as a group consisting of individuals, all of which have descended from a common stock. Or, if the process be reversed, and the classification be an ascending instead of a descending one, species are regarded as the starting point of the naturalist, and it is supposed that the problem before him is to group them

²⁶ Bk. IV. ch. viil. § 1. Note.

under higher divisions. But a species may, as we have seen, be divided into varieties, sub-varieties, &c. Now, in what consists the difference between the relation of a variety to a species and the relation of a species to a genus? To this question a very large section of naturalists now maintain that no satisfactory answer can be given. If it be said that varieties of the same species may be developed in the course of time, but that species themselves must be regarded as distinct, it may be asked on what grounds this supposition rests. Different varieties of the same species are certainly more like each other than different species of the same genus, just as species of the same genus have more resemblance than genera of the same order, or members of any lower division than members of any higher division; but, given a larger amount of time, is there more difficulty in supposing a common stock for the different species of a genus than for the different varieties of a species? This is the question originated with so much ability by Mr. Darwin in his work on the Origin of Species. His own solution of the question is well known. 'It will be seen,' he says 26, 'that I look at the term species, as one arbitrarily given for the sake of convenience to a set of individuals closely resembling each other, and that it does not essentially differ from the term variety, which is given to less distinct and more fluctuating forms. The term variety, again, in comparison with mere individual differences, is also applied arbitrarily, and for mere

³ Darwin's Origin of Species, ch. 11.

convenience' sake.' It does not fall within my province to discuss the question of the 'Origin of Species,' but it is desirable that the student should be aware that the practice of naturalists in stopping at species, as if they were the 'infimæ species' of the old logicians below which divisions need not proceed, is far from being universally accepted.

Remark 2. As our knowledge of the external world becomes enlarged, the number of natural groups, recognised by the classificatory sciences, is being continually increased. Botanists and zoologists (especially the former) are constantly discovering or recognising new varieties, frequently new species, and occasionally, even, new general and orders. 'The known species of plants,' says Dr. Whewell 57, 'were ro,000 at the time of Linnæus, and are now [A.D. 1858] probably 60,000.' The increase in the number of recognised varieties, sub-varieties, &c., is even still more rapid. One common effect of these constant discoveries and recognitions is to bridge over what previously appeared to be gaps in nature, thus illustrating the fact that there are but few breaks in natural phenomena, that there pervades nature a Law of Continuity, according to which a group seldom occurs to which some other group may not be found very closely allied. So complete, sometimes, is this continuity, that it becomes very difficult to distinguish the groups by any fixed characters. Two species (say) are discriminated, and then a third group is found which partakes of the character of each of the

[&]quot; History of Scientific Ideas, Bk. VIII. ch. ii. § 6.

others. This is constituted a new species, and then a fourth group is found intermediate between this and the first, and so on. 'It has been shown,' says Dr. Carpenter, as quoted by Sir W. Grove 20, 'that a very wide range of variation exists among Orbitolites, not merely as regards external form, but also as to plan of development; and not merely as to the shape and aspect of the entire organism, but also with respect to the size and configuration of its component parts. It would have been easy, by selecting only the most divergent types from amongst the whole series of specimens which I have examined, to prefer an apparently substantial claim on behalf of these to be accounted as so many distinct species. But after having classified the specimens which could be arranged around these types, a large proportion would yet have remained, either presenting characters intermediate between those of two or more of them, or actually combining those characters in different parts of their fabric; thus showing that no lines of demarcation can be drawn across any part of the series that shall definitely separate it into any number of groups, each characterised by features entirely peculiar to itself.' We certainly find in nature a persistency of type, which is the result of the laws of hereditary transmission; if there were no such persistency, the attempt to group natural objects would be fruitless and absurd. But, at the same time, when we have succeeded in establishing groups,

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Essay on Continuity, printed at the end of the Fifth Edition of The Correlation of Physical Forces, pp. 326, 327.

we constantly find that there are individual members diverging more or less from the ordinary type, and forming intermediate links between proximate classes. To adopt and alter a metaphor employed by Dr. Whewell, natural classes may be regarded as the forests of neighbouring hills, the hills being seldom separated by well-defined valleys, and the valleys being frequently interspersed with straggling trees or clumps.

Remark 3. It sometimes happens that one of the characters by which classes or groups are distinguished, one from another, is to be found, not invariably, but only usually or occasionally in the members of the group. Thus, in the description of the Order Rosaceæ, we find that 'the seeds are erect or inverted, usually exalbuminous. Flowers sometimes unisexual.' Such indefinite descriptions would be entirely out of place in an artificial classification, but in a natural classification, where the entire assemblage of the characters must be taken into consideration, a character, though not found invariably, or even though found but seldom, may still be valuable in distinguishing a group.

Remark 4. The most important characters are not always those by which a group is most easily recognised. For the purpose of recognition, some external and prominent character or set of characters is generally best adapted. Thus, if we wished to determine whether a plant were monocotyledonous or dicotyledonous, our easiest course would be to examine the stem; if the stem were endogenous, we should know that the plant

was a monocotyledon, if exogenous, that the plant was a dicotyledon. A single character is often sufficient to determine the place of a plant or animal in a series, because we already know that the possession of this character is a sign of the possession of the various other characters which are enumerated in the description of the natural class. The method of determining, by means of one or a few characters, the place of a natural object in a classification, is often called Diagnosis or Characteristick. 'The Characteristick,' says Dr. Whewell 29, 'is an Artificial Key to a Natural System. As being Artificial, it takes as few characters as possible; as being Natural, its characters are not selected by any general or prescribed rule, but follow the natural affinities. 'The genera Lamium and Galeopsis (Dead Nettle and Hemp Nettle) are each formed into a separate group in virtue of their general resemblances and differences, and not because the former has one tooth on each side of the lower lip, and the latter a notch in its upper lip, though they are distinguished by these marks,'

Note.—Dr. Whewell maintains that natural classes are determined, not by definition, that is, by an enumeration of characters, but by type, that is, by resemblance, more or less complete, to some one member of the class, round which the others are grouped. Thus, according to this theory, the Class Mammalia would be determined, not

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²⁹ History of Scientific Ideas, Bk. VIII. ch. ii. § 7.

by an enumeration of characters, but by resemblance, more or less complete, to some typical specimen, say Dog; the genus Dog would be determined not by an enumeration of the characters which are common to the dog, wolf, and fox (the species comprised in the genus), but by approximation to the type-species dog: similarly, the Order Rosaceæ would be determined not by an enumeration of characters, common to a large number of genera, but by the resemblance, more or less complete, of these genera to the type-genus Rosa. Dr. Whewell's view will be understood from the following extract:—

'In a Natural Group the class is steadily fixed, though not precisely limited; it is given, though not circumscribed; it is determined, not by a boundary line without, but by a central point within; not by what it strictly excludes, but by what it eminently includes; by an example, not by a precept; in short, instead of Definition we have a Type for our director.

'A Type is an example of any class, for instance, a species of a genus, which is considered as eminently possessing the characters of the class. All the species which have a greater affinity with this Type-species than with any others, form the genus, and are ranged about it, deviating from it in various directions and different degrees. Thus a genus may consist of several species, which approach very near the type, and of which the claim to a place with it is obvious; while there may be other species which straggle further from this central

knot, and which yet are clearly more connected with it than with any other. And even if there should be some species of which the place is dubious, and which appear to be equally bound by two generic types, it is easily seen that this would not destroy the reality of the generic groups, any more than the scattered trees of the intervening plain prevent our speaking intelligibly of the distinct forests of two separate hills.

'The Type-species of every genus, the Type-genus of every family, is, then, one which possesses all the characters and properties of the genus in a marked and prominent manner. The Type of the Rose family has alternate stipulate leaves, wants the albumen, has the ovules not erect, has the stigmata simple, and besides these features, which distinguish it from the exceptions or varieties of its class, it has the features which make it prominent in its class. It is one of those which possess clearly several leading attributes; and thus, though we cannot say of any one genus that it must be the Type of the family, or of any one species that it must be the Type of the genus, we are still not wholly to seek: the Type must be connected by many affinities with most of the others of its group; it must be near the centre of the crowd, and not one of the stragglers to.'

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^{**} History of Scientific Ideas, Bk. VIII. ch. ii. § 3. art. 10. Mr. Mill (Logic, Bk. IV. ch. vii. §§ 3, 4) examines Dr. Whewell's views at considerable length. He appears to me, in this examination, to insist too emphatically on what he calls 'distinctions of kind,' and to assert, without sufficient warrant, that 'the species of Plants are not only real kinds, but are probably, all of them, real lowest kinds,

There is much force in what Dr. Whewell here says, but his main position appears to me to be incorrect. May not the various steps in the process of Classification be described as follows? We, first, observe a general resemblance amongst a variety of groups. Prompted by the observation of this resemblance, we determine to constitute the groups into a distinct class. But it is not sufficient simply to enumerate the groups which the class contains; it is incumbent upon us to state the principle on which the classification is made. statement consists in an enumeration of those characters which are common to all the members of the newly-constituted class, and which, at the same time, distinguish them from the members of other classes, with the addition, in some cases, of certain characters which belong to most, or even to a few only, of the members of the Thus, the class is determined (or 'given,' to use Dr. Whewell's expression) by an enumeration of characters. But, when the class is once familiar to us, the repetition of the class-name suggests, not the characters, but some typical specimen of the class, some one group which stands out prominently as possessing the characters by which the class was determined; and it is by reference to this central specimen, as it were, that we fix the position of the other groups and adjudicate on the claims of

Infimæ Species, which if we were to subdivide into sub-classes, the subdivision would necessarily be founded on definite distinctions, not pointing (apart from what may be known of their causes or effects) to any difference beyond themselves.'

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any newly-discovered group to take its place by the side of the others. Thus, the type-species, type-genus, or typical order, may be of the greatest service as a convenient embodiment of the characters, but the characters must be enumerated, and the class determined, before we can select our typical example.

(2) OF NOMENCLATURE.

Nomenclature is intimately connected with Classification. The groups, whether natural or artificial, into which objects are distributed, could neither be recollected by ourselves nor communicated to others, unless they were fixed by the imposition of names. A Nomenclature is a collection of such names, applied to the members of the various divisions and subdivisions which constitute a classification. The number of natural groups, however, is so enormously large, that it would be next to impossible to devise, and, if possible to devise, it would be impossible to remember, distinct names for each group. Thus, the known species of plants, for instance, amount to upwards of 60,000, and, if we took into account varieties, sub-varieties, &c., the number of groups would be represented by many multiples of this sum. Some artifice, therefore, is necessary by which a comparatively small number of names may be made to distinguish a large number of groups. Botany and Chemistry furnish admirable examples of the employment of such an artifice, and some knowledge of the principles which guide the imposition of names in those

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two sciences (a knowledge which may be easily acquired) would probably be of more service to the student than anything which he might learn from a body of rules for Nomenclature in general.

In Botany, the higher groups (including genera) have distinct names. Thus, we have Dicotyledones, Rosaceæ, Rosa, &c. But, when we arrive at the species, these are known by the generic name with the addition of some distinctive attribute. Thus, the genus Geranium is represented in the British Isles by thirteen species, called respectively Geranium phæum, G. nodosum, G. sylvaticum, G. pratense, G. sanguineum, G. pyrenaicum, G. pusillum, G. dissectum, G. columbinum, G. rotundifolium, G. molle, G. lucidum, G. robertianum. The specific names are selected from various considerations; sometimes in honour of an individual (as Equisetum Mackaii, Rosa Wilsoni), sometimes from the country or the district in which the plant abounds, sometimes from the soil which is most favourable to it, sometimes from some peculiarity in the plant itself. So arbitrary and fanciful sometimes are these names, that Linnæus (as we are told by Dr. Whewell31) 'gave the name of Bauhinia to a plant with leaves in pairs, because the Bauhins were a pair of brothers, that of Banisteria to a climbing plant, in honour of Banister, who travelled among mountains.' It is plain that a name which describes some peculiarity in the plant itself is of most service to the learner; but any name, easily remembered, serves

¹¹ History of Scientific Ideas, Bk. VIII. ch. il. § 6.

the main purpose of a nomenclature, which is to distinguish one group from another. Varieties, sub-varieties, &c., are distinguished from each other on the same principle as species. Thus, as we have seen, of the species Anthyllis Vulneraria there is a variety Dillenii, and of the variety Anthyllis Vulneraria. Dillenii there is a 'race' Floribus coccineis, and of the race there is a 'variation' Foliis hirsutissimis. The nomenclature of Zoology is now generally constructed on the same principle as that of Botany. In some systems of Mineralogy, three names are employed, namely, those of the Order, Genus, and Species, as, for instance, Rhombohedral Calc Haloide.

The nomenclature of Chemistry, or, at least, of Inorganic Chemistry, which, in some respects, furnishes an interesting example of a scientific nomenclature, is constructed on the principle of making the prefixes and affixes of the words employed significant of the nature of the substances for which they stand. Thus, we have the affixes ide, ic, ous, ate, ite, &c., and the prefixes mono, di, tri, sesqui, &c., each having a special significance, though, unfortunately, not always an unambiguous one.

It would transcend the limits of this work to give an account, sufficiently clear and precise, of the Nomen-clature of Inorganic Chemistry (which, moreover, is at present in a transitional state), but the student, who is anxious to gain some idea of the principles on which it is constructed, can refer to Watts' Dictionary of Chemistry, vol. iv. art. Nomenclature.

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(3) OF TERMINOLOGY.

A Nomenclature of a Science is, as we have seen, a collection of names of groups. A Terminology is a collection of the names (or terms) which distinguish either the properties or the parts of the individual objects which the science recognises. Thus, when we speak of the genus 'Rosa,' we are employing the nomenclature of Botany; but, when we say that the individuals of the genus 'Rosa' have 'their corolla imbricated before flowering, their styles with lateral insertion, their carpels numerous,' &c., we are employing not the nomenclature, but the terminology, of the science. In botany we have an almost perfect example of a complete and judiciously constructed terminology.

'The formation of an exact and extensive descriptive language for botany,' says Dr. Whewell so, 'has been executed with a degree of skill and felicity, which, before it was attained, could hardly have been dreamt of as attainable. Every part of a plant has been named; and the form of every part, even the most minute, has had a large assemblage of descriptive terms appropriated to it, by means of which the botanist can convey and receive knowledge of form and structure, as exactly as if each minute part were presented to him vastly magnified. This acquisition was part of the Linnæan Reform. "Tournefort," says Decandolle, "appears to have been the first who really perceived the utility of fixing the sense of terms

³³ History of Scientific Ideas, Bk. VIII. ch. ii. § 2.

in such a way as always to employ the same word in the same sense, and always to express the same idea by the same word; but it was Linnæus who really created and fixed this botanical language, and this is his fairest claim to glory, for by this fixation of language he has shed clearness and precision over all parts of the science."

'It is not necessary here to give any detailed account of the terms of botany. The fundamental ones have been gradually introduced, as the parts of plants were more carefully and minutely examined. Thus the flower was successively distinguished into the calyx, the corolla, the stamens, and the pistils: the sections of the corolla were termed petals by Columna; those of the calyx were called sepals by Necker. Sometimes terms of greater generality were devised; as perianth to include the calyx and corolla, whether one or both of these were present; pericarp for the part inclosing the grain, of whatever kind it be, fruit, nut, pod, &c. And it may easily be imagined that descriptive terms may, by definition and combination, become very numerous and distinct. Thus leaves may be called pinnatifid, pinnatipartite, pinnatisect, pinnatilobate, palmatifid, palmatipartite, &c., and each of these words designates different combinations of the modes and extent of the divisions of the leaf with the divisions of its outline. In some cases arbitrary numerical relations are introduced into the definition: thus a leaf is called bilobate when it is divided into two parts by a notch; but, if the notch go to the middle of its length, it is bifid; if it go near the base of the leaf, it is bipartite; if to the base, it is bisect,

Thus, too, a pod of a cruciferous plant is a siliqua if it be four times as long as it is broad, but if it be shorter than this it is a silicula. Such terms being established, the form of the very complex leaf or frond of a fern is exactly conveyed by the following phrase: "fronds rigid pinnate, pinnæ recurved subunilateral pinnatifid, the segments linear undivided or bifid spinuloso-serrate."

A Terminology, I have said, comprises the terms appropriated to express, not only the parts of objects, but also their properties. Thus, in the foregoing example, the words 'sepals,' 'petals,' &c., express parts of the plant, the words 'pinnatifid,' 'bilobate,' &c., which are applied to the shape of the leaves, express characters or properties. A complete terminology must be so constructed as to express every shade of difference in all those properties which are recognised in a scientific treatment of the object. Thus, if colour be regarded as of importance in the description of a plant, mineral, &c., it is essential that there shall be some appropriate term by which to describe every shade of colour. But there are few terms which, from their mere signification, can call up any precise idea in the mind. Hence it is necessary to fix by convention the precise meaning of every technical term employed in science. Again, to appropriate the words of Dr. Whewell, 'The meaning of technical terms can be fixed in the first instance only by convention, and can be made intelligible only by presenting to the senses that which the terms are to signify. The knowledge of a colour by its name

can only be taught through the eye. No description can convey to a hearer what we mean by apple-green or French grey. It might, perhaps, be supposed that, in the first example, the term apple, referring to so familiar an object, sufficiently suggests the colour intended. But it may easily be seen that this is not true; for apples are of many different hues of green, and it is only by a conventional selection that we can appropriate the term to one special shade. When this appropriation is once made, the term refers to the sensation, and not to the parts of this term; for these enter into the compound merely as a help to the memory, whether the suggestion be a natural connexion as in "apple-green," or a casual one as in "French grey." In order to derive due advantage from technical terms of this kind, they must be associated immediately with the perception to which they belong; and not connected with it through the vague usages of common language. The memory must retain the sensation; and the technical word must be understood as directly as the most familiar word, and more distinctly. When we find such terms as tin-white or pinchbeck-brown, the metallic colour so denoted ought to start up in our memory without delay or search." When we have fixed, by convention, the meaning of a term, it must invariably be employed in this sense, and in no other. The least vagueness or inconsistency in the use of terms may interpose a fatal obstacle in the way, not only of the learners, but

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²⁴ History of Scientific Ideas, Bk. VIII. ch. ii. § 2.

even of the promoters of a science. The progress of the Mechanical Sciences and of what are commonly called Physics was long retarded by the vague and unintelligent use of such words as 'heavy,' 'light,' 'hot,' 'cold,' 'moist,' 'dry,' &c. Even still such words as 'force,' 'fluid,' attraction,' 'ether,' &c., are often employed without sufficient precision.

A Terminology, as remarked by Dr. Whewell³⁴, is indispensably requisite in giving fixity to a Nomenclature. Thus, in Botany, 'the recognition of the kinds of plants must depend upon the exact comparison of their resemblances and differences; and, to become a part of permanent science, this comparison must be recorded in words.'

Dr. Whewell devotes the last Book of his Novum Organon Renovatum to a series of aphorisms on the 'Language of Science,' including both Nomenclature and Terminology. These aphorisms afford one of the best examples of Dr. Whewell's style and mode of treatment, and will well repay the attention of the student who is desirous of acquainting himself further with the methods of the Classificatory Sciences. Mr. Mill has some chapters (Logic, Bk. IV. ch. iii-vi) on 'Naming' and the 'Requisites of a Philosophical Language,' and, in addition to the passage already referred to, Dr. Whewell treats these subjects in his History of Scientific Ideas, Bk. I. ch. ii; Bk. VIII. ch. ii. §§ 2 and 6; Bk. VIII.

³⁴ Novum Organon Renovatum, Bk. IV. Aphorism ii.

ch. iii. art. 5. In Mr. Bain's *Inductive Logic*, there is a special chapter (Bk. IV. ch. iii) on Classification, and another (Bk. V. ch. vi) on the Sciences of Classification.

§ 3. On Hypothesis.

When the mind has before it a number of observed facts, it is almost irresistibly driven to frame for itself some theory as to the mode of their co-existence or succession. It is from this irresistible impulse to refer to some law the various phenomena around us that all science as well as all scientific error has sprung. In some cases, as we have seen in the first chapter **, a single observation or experiment may at once establish a true theory or valid induction, independently of any previous suppositions on our part. But, in all the more intricate branches of enquiry, true theories have usually been preceded by a number of false ones, and it has not unfrequently occurred that the false theories have been mainly instrumental in conducting to the true. Thus, the elliptical theory of planetary motion was preceded by the circular theory, with its various modifications, and the undulatory theory of light by the emission theory. Rather than rest satisfied with a number of disconnected facts, men have often imagined the most absurd relations between phenomena, such as that a comet was the harbinger of war, or that the future could be foretold by These theories, assumptions, or suppositions, when employed provisionally in scientific enquiry and

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³⁵ See pp. 11, 12.

falling short of ascertained truths, are called hypotheses, and have already been alluded to in the first chapter. The word 'hypothesis,' as commonly employed, is exclusive of propositions which rest upon absolute proof, whether inductive or deductive, and is generally used in contradistinction to them. Thus, we speak of a science being only in a hypothetical stage, or of a hypothesis being converted into an induction or being brought deductively under some general law already ascertained to be true. On the other hand, we should hardly dignify with the name of 'hypothesis' a supposition which, at least in the eyes of its framer, did not possess some amount of plausibility. A hypothesis se may be described as a supposition made without evidence or without sufficient evidence, in order that we may deduce from it conclusions agreeing with actual facts. If these conclusions are correctly deduced, and really agree with the facts, a presumption arises that the hypothesis is true. Moreover, if the hypothesis relates to the cause, or mode of production of a phenomenon, it will serve, if admitted, to explain such facts as are found capable of being deduced from it. And this explanation is the purpose of many, if not most, hypotheses. Explanation, in the scientific sense, means the reduction of a series of facts which occur uniformly but are not connected by any known law of causation into a series which is so connected, or the reduction of complex laws of causation

^{**} The following sentences, to the end of the paragraph, are slightly altered from Mr. Mill's Logic, Bk. III. ch. xiv. § 4.

into simpler laws. If no such laws of causation are known to exist, we may *suppose* or *imagine* a law that would fulfil the requirement; and this *supposed* law would be a hypothesis.

A hypothesis may be serviceable in many ways. In the first place, it may afford a solution, more or less probable, of a problem which is incapable of any definite solution, or which, at least, has not yet been definitely solved. Thus, many of the advocates of the Darwinian hypothesis maintain that it is the most probable solution of an insoluble problem. Secondly, what was at first started as a hypothesis may ultimately be established by positive proof, as has been the case with the elliptical theory of planetary motion, and, as many suppose, with the undulatory theory of light. Thirdly, even though a hypothesis may ultimately be discovered to be false, it may be of great service in pointing the way to a truer theory. Thus, as already remarked, the circular theory of planetary motion, and the supplementary theory of epicycles and eccentrics, undoubtedly contributed to the formation of the hypothesis which was eventually proved to be true. Kepler himself tried no less than nineteen different hypotheses, before he hit upon the right one, and his ultimate success was doubtless in no slight degree due to his unsuccessful efforts. There is hardly any branch of science in which it might not be affirmed that, without a number of false guesses, true theories could never have been attained. Lastly, a hypothesis, whether true or false, if it be applicable to all the

known facts, serves as a means of binding those facts together, of colligating them, to use a technical phrase, and thus, by presenting them under one point of view, plainly marks off the phenomena to be explained. A theory, like the Phlogistic theory in Chemistry, or the theory of epicycles and eccentrics (which, by being sufficiently extended, might have been made to include all the phenomena of planetary motion), may thus have been of the greatest service in the history of science, simply by keeping before the minds of investigators the precise phenomena which demanded an explanation.

The formation of hypotheses is obviously the work of the imaginative faculty, a faculty of hardly less importance in science than in art. To lay down rules for the exercise of this faculty has hitherto been found futile. The object of Inductive Logic is rather to restrain the exuberant, than to excite the sluggish, imagination. The latter office is best fulfilled by recounting the great achievements of science, and thus arousing the ambition and kindling the enthusiasm of her votaries. The former (which is no less necessary) may be promoted by determining the conditions to which a hypothesis must conform, in order that it may rank as a provisional explanation of facts, and before it is entitled to demand the honours of a rigorous inductive examination. These conditions may be reduced to three:—

I. The hypothesis must not be known or suspected to be untrue, that is to say, it must not be inconsistent with facts already ascertained or the inferences to which they lead. It would be absurd, for instance, in the present state of knowledge, to propose design or compact as the cause of the divergences which are found in the various dialects of a language, or to suppose the heavenly bodies to move in perfect circles. So simple a rule as this may appear to be superfluous, but it seems necessary to include it in the conditions to which a hypothesis must conform, as, otherwise, a perverted ingenuity might succeed in framing numberless hypotheses which violated none of the preliminary conditions.

II. The hypothesis must be of such a character as to admit of verification or disproof, or at least of being rendered more or less probable, by subsequent investigations ²⁶. Unless this restriction were placed on the formation of hypotheses, there would be no limit to the wildness of conjecture in which theorists might indulge.

The explanation of this rule, contained in the latter clause of the sentence, has been suggested by Mr. Jevons' chapter on the Use of Hypothesis, a chapter which may be read with advantage by the student. His second condition of a legitimate hypothesis, which corresponds with my first, is expressed thus: 'That it do not conflict with any laws of nature, or of mind, which we hold as true.' Principles of Science, vol. ii, p. 139.

case where a supposition is already supported by a certain amount of probable evidence, but where it is not likely to be rendered more or less probable by further investigation. But such a supposition, though it would be an imperfect induction or deduction, could hardly be called a hypothesis, a term which seems always to imply something provisional, something which, on further enquiry, may be either confirmed or weakened, rendered more or less probable than it now is.

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It might, for instance, be maintained that falling bodies are dragged to the earth by the action of invisible spirits, and, wild as such a theory would be, there is nothing positively to disprove it. Granted that, like many other products of imagination, such a theory might possibly be true, it would still fall without the scope of science. The aim of science is proof, present or prospective, and consequently what neither admits of proof, nor, so far as we can foresee, is ever likely to admit of it, or even of approximation to it, is no fitting object of scientific enquiry. As affording a caution against the unrestrained exercise of the imagination in scientific speculation, it may be useful to adduce a few instances of suppositions or hypotheses, which were probably considered as perfectly satisfactory by those who proposed them or amongst whom they were prevalent, which would now be regarded by all competent authorities as absurd, and which still do not admit of being distinctly disproved.

It was once very generally held that the position of the planets with reference to the earth at any particular moment determines not only the course of human events at that time, but the subsequent life of each person born under the 'conjuncture.' Such an absurd theory is now probably held by no single person of sound understanding; but, so complicated is the web both of society and of individual life, and so easy would it be to explain 'apparent exceptions' by having recourse to 'counteracting causes,' that, if any ingenious person were to maintain and defend this theory, it would probably

be impossible to disprove it. Palmistry affords another instance of the same kind. The interlacing of the lines on the palms of the hands is said to indicate a man's 'fortunes.' Such a notion is too absurd to be discussed; but, if maintained, how could it be disproved? It might always be said that the general theory of palmistry was true, though there might be some error in the particular rules by which the 'fortune' in question was foretold.

The early history of Geology is full of hypotheses of this kind. The following examples of theories, which no scientific man would now entertain, but which hardly admit of disproof, are extracted from Lyell's *Principles of Geology* 10:—

'Andrea Mattioli, an eminent botanist, the illustrator of Dioscorides, embraced the notion of Agricola, a skilful German miner, that a certain "materia pinguis," or "fatty

The superstitions connected with dreams afford a similar instance: 'The ancients were convinced that dreams were usually supernatural. If the dream was verified, this was plainly a prophecy. If the event was the exact opposite of what the dream foreshadowed, the latter was still supernatural, for it was a recognised principle that dreams should sometimes be interpreted by contraries. If the dream bore no relation to subsequent events unless it were transformed into a fantastic allegory, it was still supernatural, for allegory was one of the most ordinary forms of revelation. If no ingenuity of interpretation could find a prophetic meaning in a dream, its supernatural character was even then not necessarily destroyed, for Homer said there was a special portal through which deceptive visions passed into the mind, and the Fathers declared that it was one of the occupations of the dæmons to perplex and bewilder us with unmeaning dreams.'-Lecky's History of European Morals, vol. i. p. 385.

[&]quot; Lyell's Principles of Geology, ch. iii.

matter," set into fermentation by heat, gave birth to fossil organic shapes. Yet Mattioli had come to the conclusion, from his own observations, that porous bodies, such as bones and shells, might be converted into stone, as being permeable to what he termed the "lapidifying juice." In like manner, Falloppio of Padua conceived that petrified shells were generated by fermentation in the spots where they are found, or that they had in some cases acquired their form from "the tumultuous movements of terrestrial exhalations." Although celebrated as a professor of anatomy, he taught that certain tusks of elephants, dug up in his time in Apulia, were mere earthy concretions; and, consistently with these principles, he even went so far as to consider it probable that the vases of Monte Testaceo at Rome were natural impressions stamped in the soil. In the same spirit, Mercati, who published, in 1574, faithful figures of the fossil shells preserved by Pope Sixtus V. in the Museum of the Vatican, expressed an opinion that they were mere stones, which had assumed their peculiar configuration from the influence of the heavenly bodies: and Olivi of Cremona, who described the fossil remains of a rich museum at Verona, was satisfied with considering them as mere "sports of nature." Some of the fanciful notions of those times were deemed less unreasonable, as being somewhat in harmony with the Aristotelian theory of spontaneous generation, then taught in all the schools. For men who had been taught, in early youth, that a large proportion of living animals and plants was formed from the fortuitous concourse of atoms, or had sprung from the corruption of organic matter, might easily persuade themselves, that organic shapes, often imperfectly preserved in the interior of solid rocks, owed their existence to causes equally obscure and mysterious.'

'As to the nature of petrified shells, Quirini conceived that, as earthy particles united in the sea to form the shells of mollusca, the same crystallizing process might be effected on the land; and that, in the latter case, the germs of the

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animals might have been disseminated through the substance of the rocks, and afterwards developed by virtue of humidity. Visionary as was this doctrine, it gained many proselytes even amongst the more sober reasoners of Italy and Germany; for it conceded that the position of fossil bodies could not be accounted for by the diluvial theory.'

It has been maintained by theologians, more ardent than discreet, that all fossils were the creations of the Devil, whose object was either to mimic the Almighty or to tempt mankind to disbelieve the Mosaic account of the creation. Such theories admit of no refutation; every argument, grounded on the resemblance of fossil remains to living organisms, shows only more distinctly, to those who have once embraced the idea, the success of the alleged agent as a mimic or as an impostor.

Other instances of hypotheses which violate this rule are afforded by the Vortices of Descartes and the Crystalline Spheres of the ancient astronomers, both of which were imagined for the purpose of accounting for the phenomena of planetary motion. Both of these hypotheses have been subsequently disproved by the free passage of comets through the spaces supposed to be occupied, according to the one theory, by the Vortices, according to the other, by the solid Crystalline Spheres. But at the time they were first started, there was no reasonable ground for supposing that, if untrue, they could be disproved, and, what is more important, there was no possibility of proving them or even rendering them more probable; they were simply freaks of imagination, incapable of proof and, to all appearance, of disproof.

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Another theory more absurd even than that of the solid crystalline spheres, but which has not, like that, been positively disproved, is the curious hypothesis by which Lodovico delle Colombe endeavoured to reconcile the Aristotelian doctrine that the moon was a perfect body with the recent discoveries of Galileo, who, by the aid of his telescope, had found that its surface was full of hollows, and was consequently charged by his enemies with taking a fiendish delight in distorting the fairest works of nature; the apparently hollow parts, suggested Lodovico, were filled with a pure transparent crystal, and so both the astronomer and the Stagirite were right.

It will be observed that I regard hypotheses as admissible, even though they are not likely ever to be positively proved or disproved, provided that the accumulation of further evidence is likely to render them more or less probable. Between such theories and the theories just exemplified, which are neither supported nor likely to be supported by any evidence whatever, there is the widest difference, and, while the one have no place in Science, the other, I conceive, have a legitimate claim to further consideration. The ideal of Science, it is true, is proof; but, while it can never recognise mere freaks of fancy, it is often compelled to rest content with probabilities. Instances of hypotheses such as I have in view are the Darwinian hypothesis and the Meteoric theory of the repair of Solar Heat, to be noticed presently.

III. The hypothesis must be applicable to the descrip-

tion or explanation of all the observed phenomena, and, if it assign a cause, must assign a cause fully adequate to have produced them. A hypothesis, which does not satisfy this requirement, may be at once rejected. Thus, when the circular theory of planetary motion was found inapplicable to describe several of the phenomena, it was rightly abandoned, and the theory of epicycles and eccentrics, which, though erroneous, was fully adequate to explain all the known phenomena, was substituted for it. One of the most familiar instances of an inadequate hypothesis is the theory started by Voltaire, there is little doubt in irony, that the marine shells found on the tops of mountains are Eastern species, dropped from the hats of pilgrims, as they returned from the Holy Land. Such a theory would obviously be inadequate to account (1) for the numbers of the shells, (2) for the fact that they are found imbedded in the rocks, (3) for their existence far away from the tracks of pilgrims, to say nothing of the fact that many of these shells bear no resemblance to recent Eastern species, while none resemble them exactly. The contrast between an adequate and an inadequate hypothesis is well illustrated by two of the rival hypotheses by which it is attempted to account for the generation and the maintenance of solar heat. These are respectively the Meteoric Theory and the Theory of Chemical Combustion. In speaking of the former theory, Professor Tyndall says 41:-

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⁴¹ Heat a Mode of Motion, 3rd ed. §§ 689-693. Sir William Thomson, however, from various considerations, arrived at the con-

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'I have already alluded to another theory, which, however bold it may at first sight appear, deserves our serious attention—the Meteoric Theory of the Sun. Kepler's celebrated statement, that "there are more comets in the heavens than fish in the ocean," implies that a small portion only of the total number of comets belonging to our system are seen from the earth. But besides comets, and planets, and moons, a numerous class of bodies belong to our system which, from their smallness, might be regarded as cosmical atoms. Like the planets and the comets, these smaller asteroids obey the law of gravity, and revolve in elliptic orbits round the sun. It is they which, when they come within the earth's atmosphere, and are fired by friction, appear to us as meteors and falling stars.

'On a bright night, twenty minutes rarely pass at any part of the earth's surface, without the appearance of at least one meteor. Twice a year (on the 12th of August and 14th of November) they appear in enormous numbers. During nine hours in Boston, when they were described as falling as thick as snowflakes, 240,000 meteors were observed. The number falling in a year might, perhaps, be estimated at hundreds or thousands of millions, and even these would constitute but a small portion of the total crowd of asteroids that circulate round the sun. From the phenomena of light and heat, and by direct observation on Encke's comet' (the inference from which 'observation,' however, it may be remarked, is very doubtful), 'we learn that the universe is filled by a resisting

clusion that 'the sun's expenditure [of heat], though originated, is not maintained by mechanical impact; the low rate of cooling and the consequent constancy of the emission being considered by him as due, in great part, to the high specific heat of the matter of the sun.' See Tyndall's Heat, &c., § 701. Other physicists (see Young on the Sun, pp. 270-7) conjecture that the heat of the sun is partly due to its gradual contraction and the increase of temperature thus generated.

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medium, through the friction of which all the masses of our system are drawn gradually towards the sun. And though the larger planets show, in historic times, no diminution of their periods of revolution, it may be otherwise with the smaller bodies. In the time required for the mean distance of the earth to alter a single yard, a small asteroid may have approached thousands of miles nearer to the sun.

'Following up these reflexions, we should be led to the conclusion that, while an immeasurable stream of ponderable meteoric matter moves unceasingly towards the sun, it must augment in density as it approaches its centre of convergence. And here the conjecture naturally rises, whether that vast nebulous mass, the Zodiacal Light, which embraces the sun, may not be a crowd of meteors. It is at least proved that this luminous phenomenon arises from matter which circulates in obedience to planetary laws; hence, the entire mass of the sodiacal light must be constantly approaching, and incessantly raining its substance down upon the sun.

It is easy to calculate both the maximum and the minimum velocity, imparted by the sun's attraction to an asteroid circulating round him. The maximum is generated when the body approaches the sun from an infinite distance; the entire pull of the sun being then exerted upon it. The minimum is that velocity which would barely enable the body to revolve round the sun close to his surface. The final velocity of the former, just before striking the sun, would be 390 miles a second, that of the latter 276 miles a second. The asteroid, on striking the sun, with the former velocity, would develope more than 9000 times the heat generated by the combustion of an equal asteroid of solid coal; while the shock, in the latter case, would generate heat equal to that of the combustion of upwards of 4000 such asteroids. It matters not, therefore, whether the substances falling into the sun be combustible or not; their being combustible would not add sensibly to the tremendous heat produced by their mechanical collision.

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'Here, then, we have an agency competent to restore his lost energy to the sun, and to maintain a temperature at his surface which transcends all terrestrial combustion. In the fall of asteroids we find the means of producing the solar light and heat. It may be contended that this showering down of matter necessitates the growth of the sun: it does so; but the quantity necessary to maintain the observed calorific emission for 4000 years, would defeat the scrutiny of our best instruments. If the earth struck the sun, it would utterly vanish from perception; but the heat developed by its shock would cover the expenditure of a century.'

Of the other theory, Professor Tyndall says 42:-

'Sir William Thomson adduces the following forcible considerations to show the inadequacy of chemical combination to produce the sun's heat. "Let us consider," he says, "how much chemical action would be required to produce the same effects. . . . Taking the former estimate, 2781 thermal units "centigrade (each 1390 foot pounds) or 3,869,000 foot pounds, which is equivalent to 7000 horse-power, as the rate per second of emission of energy from every square foot of the sun's surface, we find that more than 0.42 of a pound of coal per second, 1500 lbs. per hour, would be required to produce heat at the same rate. Now if all the fires of the whole Baltic fleet (this was written in 1854) were heaped up and kept in full combustion over one or two square yards of surface, and if the surface of a globe all round had every square yard so occupied, where could

⁴ Heat a Mode of Motion, \$ 700.

The thermal unit is the quantity of heat necessary to raise the temperature of a pound of water one degree. If the degree be centigrade, this is equivalent to the heat generated by a pound weight falling from a height of 1390 feet against the earth. The term foot-found expresses the energy requisite to lift one pound to the height of a foot.

a sufficient supply of air come from to sustain the combustion? Yet such is the condition we must suppose the sun to be in, according to the hypothesis now under consideration. . . . If the products of combustion were gaseous, they would, in rising, check the necessary supplies of fresh air; if they were solid and liquid (as they might be if the fuel were metallic), they would interfere with the supply of elements from below. In either or in both ways, the fire would be choked, and I think it may be safely affirmed that no such fire could keep alight for more than a few minutes, by any conceivable adaptation of air and fuel. If the sun be a burning mass it must be more analogous to burning gunpowder than to a fire burning in air; and it is quite conceivable that a solid mass, containing within itself all the elements required for combustion, provided the products of combustion are permanently gaseous, could burn off at its surface all round, and actually emit heat as copiously as the sun. Thus, an enormous globe of gun-cotton might, if at first cold, and once set on fire round its surface, get to a permanent rate of burning, in which any internal part would become heated sufficiently to ignite, only when nearly approached by the burning surface. It is highly probable indeed that such a body might for a time be as large as the sun and give out luminous heat as copiously, to be freely radiated into space, without suffering more absorption from its atmosphere of transparent gaseous products than the light of the sun actually does experience from the dense atmosphere through which it passes. Let us therefore consider at what rate such a body, giving out heat so copiously, would burn away; the heat of combustion could probably not be so much as 4000 thermal units per pound of matter burned, the greatest thermal equivalent of chemical action yet ascertained falling considerably short of this. But 2781 thermal units (as found above) are emitted per second from each square foot of the sun; hence there would be a loss of about 0.7

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of a bound of matter per square foot per second . . . or a layer half a foot thick in a minute, or 55 miles thick in a year. At the same rate continued, a mass as large as the sun is at present would burn away in 8000 years. If the sun has been burning at that rate in past time he must have been of double diameter, of quadruple heating power, and of eightfold mess only 8000 years ago. We may therefore quite safely conclude that the sun does not get its heat by chemical action . . . and we must therefore look to the meteoric theory for fuel."

A hypothesis which fulfils these three conditions is a legitimate hypothesis, though it must conform to still more rigorous requirements before it can be accepted as a complete Induction, or even be regarded as possessing any great amount of probability. Thus, the Meteoric Theory, though it is not yet proved, and perhaps never may be proved, to be the true explanation of the phenomenon of solar heat, is perfectly tenable as a hypothesis. For, to take the conditions in the reverse order to that in which they have been enumerated above, the impact of a large number of meteors on a body of considerable density, such as the sun probably is, would be competent or adequate to produce the given effect; the theory in question is likely, if not to be proved or disproved, at least to be rendered more or less probable by the progress of astronomical science; lastly, we do not know, nor have we any reason to suppose, that the hypothesis is an untrue explanation of the facts. But, though legitimate as a hypothesis, before we could accept the Meteoric Theory as a Valid or Complete Induction,

that is to say, an ascertained truth, we should require to know not only that there is a large number of meteors circulating round the sun, that these meteors have a tendency to fall into the central body, and that, if they were falling or had fallen in sufficient quantities, they would be competent or would have been complent to produce the present amount of solar heat, but also that they do, as a matter of fact, fall in sufficient quantities to account for the phenomenon, or, at least, that *** **thing** else** but the showering down of asteroids and meteors could** account for it.

It was by availing himself of the latter mode of proof that Newton demonstrated the existence in the sun of a central force attracting the planets towards it. Assuming Kepler's hypothesis (then sufficiently verified by observation to be universally accepted as a true statement of the facts), that equal areas are described by the radii vectores of the planets in equal times, Newton showed that this fact could be due to only one cause, namely, the deflexion of the planets from their rectilinear course by a force acting in the direction of the sun's centre. The existence of the central force was, at first, started by him as a hypothesis. 'He then proved that,' on the supposition of the existence of such a force, 'the planet will describe, as we know by Kepler's first law that it does describe, equal areas in equal times; and, lastly, he proved that if the force acted in any other direction whatever, the planet would not describe equal areas in equal times. It being thus shown that no other hypothesis would accord with the facts, the assumption was proved; the hypothesis became an inductive truth. Not only did Newton ascertain by this hypothetical process the direction of the deflecting force; he proceeded in exactly the same manner to ascertain the law of variation of the quantity of that force. He assumed that the force varied inversely as the square of the distance; showed that from this assumption the remaining two of Kepler's laws might be deduced; and finally, that any other law of variation would give results inconsistent with those laws, and inconsistent, therefore, with the real motions of the planets, of which Kepler's laws were known to be a correct expression 44.

It will be noticed that the course of demonstration pursued in this instance is the following: (1) we have certain observed facts; (2) these observed facts are generalised in what are called Kepler's Laws; (3) we have the assumption of the central force; (4) it is shown that the central force will account for Kepler's Laws, and therefore, of course, for the particular facts of observation on which those Laws were founded; (5) it is shown (and this, together with the next step, is what properly constitutes the demonstration) that this assumption is the only one which will account for the Laws or the particular facts expressed by them; (6) it is inferred inductively, by means of the Method of Difference (to be hereafter described), that the assumption of the central force, as it will account for, and is the only supposition

[&]quot; Mill's Logic, Bk. III. ch. xiv. § 4.

which will account for, the observed facts, must be accepted as true; (7) Kepler's Laws (which had hitherto been accepted as correct statements of observed facts, though they had not yet been explained by reference to any cause competent to account for them) are now proved deductively from what we have ascertained to be the Valid Induction of the Central Force.

A Hypothesis can only be converted into a Valid Induction 45 by the application of one or other of the Inductive Methods (to be described in the next Chapter), or, if we insist on strict accuracy of proof, of such of them as furnish absolutely certain conclusions.

Note 1.—According to the view here taken, which agrees with that of Mr. Mill, a hypothesis cannot claim to be regarded as an established truth, till it has conformed to the requirements of one or other of the inductive methods, or has been shown to admit of being deduced from some previously established Induction. Thus, when Newton proves the existence of a central force, deflecting the planets from the recti-

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Complete Induction, it must not be forgotten that we have admitted, as legitimate, hypotheses which are never likely to rest on more than probable evidence. These can, of course, receive accessions of proof only by the same means as those by which we establish Imperfect Inductions. It should also be remembered that the truth of a hypothesis may be demonstrated by deductive as well as by inductive methods.

lineal course which they would otherwise describe and making them describe curves round the sun, by showing that no other supposition would account for the fact that their radii vectores describe equal areas in equal times, he is, as Mr. Mill says, employing the Method of Difference. The demonstration 'affords the two instances, A B C, a b c, and B C, b c. A represents central force; A B C, the planets plus a central force; BC, the planets as they would be without a central force. The planets with a central force give a (areas proportional to the times); the planets without a central force give δc (a set of motions) without a, or with something else instead of a. the Method of Difference in all its strictness. It is true, the two instances which the method requires are obtained in this case, not by experiment, but by a prior deduction. But that is of no consequence. It is immaterial what is the nature of the evidence from which we derive the assurance that ABC will produce abc, and BC only bc; it is enough that we have that assurance. In the present case, a process of reasoning furnished Newton with the very instances, which, if the nature of the case had admitted of it, he would have sought by experiment45.'

Dr. Whewell, who does not acknowledge the utility of Mr. Mill's methods, appears to regard the inductive process as consisting simply in the framing of successive hypotheses, the comparison of these hypotheses with the ascertained facts of nature, and the introduction into them of such modifications as that comparison may

⁴⁴ Mill's Logic, Bk. III. ch. ziv. 4 4.

render necessary 47. The first requisite in a hypothesis, according to Dr. Whewell, is that it shall explain all the observed facts. But its probability, he urges, will be considerably enhanced, if, in addition to explaining observed facts, it enables us to predict the future. 'Thus the hypotheses which we accept ought to explain phenomena which we have observed. But they ought to do more than this: our hypotheses ought to foretel phenomena which have not yet been observed; at least all phenomena of the same kind as those which the hypothesis was invented to explain. For our assent to the hypothesis implies that it is held to be true of all particular instances. That these cases belong to past or to future times, that they have or have not already occurred, makes no difference in the applicability of the rule to them. Because the rule prevails, it includes all cases; and will determine them all, if we can only calculate its real consequences. Hence it will predict the results of new combinations, as well as explain the appearances which have occurred in old ones. And that it does this with certainty and correctness, is one mode in which the hypothesis is to be verified as right and useful 48.7

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⁵⁷ A theory of Induction almost identical with that of Dr. Whewell (though, I venture to suggest, not so clearly stated or so carefully guarded) has been recently propounded by Professor Stanley Jevons in his *Principles of Science*. This theory, together with other points of difference between Professor Jevons and myself, I have noticed in the Preface to the third edition, reprinted in the present one.

⁴⁸ Novum Organon Renovatum, Bk. II. ch. v. art. 10.

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Curiously enough, the first hypothesis which Dr. Whewell cites, as having fulfilled both these conditions, is also one which eventually proved to be false. 'For example, the Epicyclical Theory of the heavens was confirmed by its predicting truly eclipses of the sun and moon, configurations of the planets, and other celestial phenomena; and by its leading to the construction of Tables by which the places of the heavenly bodies were given at every moment of time. The truth and accuracy of these predictions were a proof that the hypothesis was valuable, and, at least to a great extent, true; although, as was afterwards found, it involved a false representation of the structure of the heavens.' A theory may thus not only enable us to explain known facts, but even to predict the future, and still be untrue. Notwithstanding, however, the infelicitous character of the example selected, Dr. Whewell attaches the greatest importance to the fulfilment of this condition by a hypothesis. 'Men cannot help believing that the laws laid down by discoverers must be in a great measure identical with the real laws of nature, when the discoverers thus determine effects beforehand in the same manner in which nature herself determines them when the occasion occurs. Those who can do this must, to a considerable extent, have detected nature's secret; -must have fixed upon the conditions to which she attends, and must have seized the rules by which she applies them. Such a coincidence of untried facts with speculative assertions cannot be the work of chance, but implies some large portion of truth

in the principles on which the reasoning is founded. To trace order and law in that which has been observed, may be considered as interpreting what nature has written down for us, and will commonly prove that we understand her alphabet. But to predict what has not been observed, is to attempt ourselves to use the legislative phrases of nature; and when she responds plainly and precisely to that which we thus utter, we cannot but suppose that we have in a great measure made ourselves masters of the meaning and structure of her language. The prediction of results, even of the same kind as those which have been observed, in new cases, is a proof of real success in our inductive processes.'

But what appears to Dr. Whewell to establish the truth of a hypothesis beyond all question is what he calls a Consilience of Inductions. 'We have here spoken of the prediction of facts of the same kind as those from which our rule was collected. But the evidence in favour of our induction is of a much higher and more forcible character when it enables us to explain and determine cases of a kind different from those which were contemplated in the formation of our hypothesis. The instances in which this has occurred, indeed, impress us with a conviction that the truth of our hypothesis is certain. No accident could give rise to such an extraordinary coincidence. No false supposition could, after being adjusted to one class of phenomena, exactly represent a different class, where the agreement was unforeseen and uncontemplated. That rules springing from remote and unconnected quarters

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should thus leap to the same point, can only arise from that being the point where truth resides.

'Accordingly the cases in which inductions from classes of facts altogether different have thus jumped together, belong only to the best established theories which the history of science contains. And, as I shall have occasion to refer to this peculiar feature in their evidence, I will take the liberty of describing it by a particular phrase; and will term it the Consilience of Inductions.

'It is exemplified principally in some of the greatest discoveries. Thus it was found by Newton that the doctrine of the Attraction of the Sun varying according to the Inverse Square of the distance, which explained Kepler's Third Law, of the proportionality of the cubes of the [mean] distances to the squares of the periodic times of the planets, explained also his First and Second Laws, of the elliptical motion of each planet; although no connexion of these laws had been visible before. Again, it appeared that the force of Universal Gravitation, which had been inferred from the Perturbations of the moon and planets by the sun and by each other, also accounted for the fact, apparently altogether dissimilar and remote, of the Precession of the equinoxes. was a most striking and surprising coincidence, which gave to the theory a stamp of truth beyond the power of ingenuity to counterfeit 49.2

It is undeniable that a theory which thus appears to afford an explanation of different classes of facts strikes

^{**} Novum Organon Renovatum, Bk. II. ch. v. art. 11.

the imagination with considerable force, and that its very simplicity furnishes prima facie evidence of its truth. But what is required before a hypothesis can be placed beyond suspicion is formal proof, and that, it appears to me, is furnished by Mr. Mill's 'methods,' and not by Dr. Whewell's requisitions of explanation, prediction, and consilience of inductions. For the questions at issue between Mr. Mill and Dr. Whewell, see Whewell's Novum Organon Renovatum (where his views are stated in their latest and most matured form), Bk. II. ch. v. § 3, and Mill's Logic, Bk. III. ch. xiv. § 6.

Note 2.—In attempting to determine the conditions to which a legitimate hypothesis must conform, I have avoided the employment of the expressions vera causa and adaquata causa. In the first place, a hypothesis may simply attempt to find a general expression for a number of isolated facts without referring them to any cause, as was the case with the various hypotheses respecting the shape of the planetary orbits, and hence to speak as if a hypothesis always assigned a cause is an undue limitation of the meaning of the word. But to the expression vera causa there is a more special exception. Its meaning is ambiguous. Is it the actual cause which produces a phenomenon, or a cause which we know to be actually existent, or a cause analogous to an existent cause? The student will find a criticism of this expression (first employed by Newton) in Dr. Whewell's Philosophy of Discovery, ch. xviii. § 5, &c. The expression cannot

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have been used in the first, which is its most obvious, sense, for, as Dr. Whewell says, 'although it is the philosopher's aim to discover such causes, he would be little aided in his search of truth, by being told that it is truth which he is to seek.' But in the second of the two remaining senses, the requirement, as would now be generally acknowledged, is too stringent, and, if it had been invariably observed, would have prevented us from reaping some of the greatest discoveries in science, while in the last it is so vague as to be of no practical service. It has been attempted to affix other meanings to the phrase; but there can be little doubt that Newton, having in mind the Vortices of Descartes, intended to protest against the introduction of causes of whose existence we have no direct knowledge, and consequently laid down a rule, which the subsequent history of science has shown to be needlessly stringent.

Note 3.—We sometimes find the expression a 'gratuitous' hypothesis.' By this phrase is meant the assumption of an unknown cause, when the phenomenon is capable of being explained by the operation of known causes, or the introduction of an extraneous (though it may be known) cause, when the phenomenon is capable of being accounted for by the causes already known to be in operation. Of the latter case we should have instances, where a man is supposed to have acted at the suggestion of another, though his own motives would supply a sufficient explanation of his conduct, or where

a man is supposed to have been poisoned, though he was already known to have been suffering from a fatal disease. Of the former case we should have instances in the crystalline spheres of the ancient astronomers and in the masses of crystal which were supposed by Lodovico delle Colombe to fill up the cavities of the moon (there being no instances known to us of the existence of crystal in these huge masses, and the phenomena being capable of explanation without making the supposition); in the caloric (which was supposed to be a distinct substance) of the early writers on heat; in the 'electrical fluid' of the early electricians; and in the ἀπόρροιαι of Democritus or the 'intentional species' of the Peripatetics, which, being invented for the purpose of explaining the perception of material objects by the mind, were themselves equally in need of explanation. In all these instances, under whichever of the two cases they may fall, the objection to the hypothesis is that it seems 'not to be needed.'

I have said nothing of 'gratuitous hypotheses' in the text, as a hypothesis, though it may appear to be gratuitous, may still be legitimate, and may even ultimately turn out to be true.

CHAPTER III.

On the Inductive Methods.

INDUCTION has been defined to be a legitimate inference from the known to the unknown. unknown must not be entirely unknown. It must be known to agree in certain circumstances with the known, and it is in virtue of this agreement that the inference is made. Now, how are we to ascertain what are the common circumstances which justify the inductive inference? X and Y may both agree in exhibiting the circumstances a, b, c, but it will not follow because X exhibits the quality m, that therefore this quality will also necessarily be found in Y. Nor even, if twenty, thirty, a hundred, or a thousand cases could be adduced in which the circumstances a, b, c were found to be accompanied by the circumstance m, would it follow necessarily (it might not even follow probably) that the next case in which we detected the circumstances a, b, c would also exhibit the quality m. We might pass through a field containing thousands of blue hyacinths, but this fact would not justify us in expecting that the next time we saw

a hyacinth, it would be a blue one. This form of induction (Inductio per Enumerationem Simplicem) may have no value whatever. In most cases, the condemnation passed on it by Bacon1 is perfectly just: 'Inductio quæ procedit per enumerationem simplicem, res puerilis est, et precario concludit, et periculo exponitur ab instantia contradictoria, et plerumque secundum pauciora quam par est, et ex his tantummodo quæ præsto sunt, pronunciat.' But when we have reason to think that any instances to the contrary, if there were such, would be known to us, the argument may possess considerable value, and when, as in the case of the Laws of Causation and of the Uniformity of Nature, we feel certain, from a wide and uncontradicted experience, that there are no cases to the contrary, no stronger argument (to us individually) can be adduced. It is not often, however, that an Inductio per Enumerationem Simplicem can afford us this certainty 9. Our trustworthy inductions are, in the majority of cases, the result of our detecting some fact of causation among the observed phenomena. We find, for instance, that, amongst the observed phenomena, a, b, c, d of X, a is the cause of c, and, consequently, if we observe the phenomenon a in Y, we infer that, if there are no counteracting circumstances, Y will possess the quality c as well; or, if we

¹ Novum Organum, Lib. I. aph. ev.

^{*} It must be remembered that a complete enumeration of instances, when we know the enumeration to be complete, inasmuch as it leaves no room for an inference from the known to the unknown, does not furnish an inductive but a deductive argument. See Elements of Deductive Logic, Part III. ch. i. appended Note 2.

observe the phenomenon c in Y, we infer that it is not unlikely that a may be present as well. The problem of Induction, therefore, resolves itself (except in the cases in which we may legitimately employ Inductio per Enumerationem Simplicem, or the cases in which we have no other resource) into the problem of detecting facts of Causation. Certain rules for this purpose have been laid down by Mr. Mill, called by him the Experimental Methods, but which I shall describe as the Inductive Methods.

These Methods, it will be noticed as we proceed, are all methods of elimination, or devices by which we are enabled to argue from a comparatively small number of instances with the same certainty as if they were ever so numerous.

Before proceeding to state and explain these Rules or Methods, it may be useful to make some preliminary remarks on the nature of the causal relations which subsist among phenomena.

- (1) The same cause, unless there are counteracting circumstances, that is, other causes which prevent it from acting or which modify its action, is invariably followed by the same effect.
- (2) As already shown (Chapter I. pp. 13-16), several causes may have co-operated in producing any given effect. In this case, it is not unusual to speak of the 'combination of causes' or the 'sum of the causes.'

[&]quot; I say 'not unlikely,' for c might be due to some other cause as well as a, and, therefore, the presence of c does not enable us to infer with certainty the presence of a, as does that of a the presence of c.

- (3) The same effect may be due to several distinct causes, or combinations of causes, being due sometimes to one and sometimes to another, and, hence, though we may always argue from a particular cause to its effect, we cannot always argue from an effect to any particular cause. Thus, ignition may be due, not only to the concentration of the rays of solar heat, but also to friction, electricity, &c. This fact has given occasion to the expression 'Plurality of Causes,' for which a recent writer (Mr. Carveth Read) has proposed to substitute the expression 'Vicariousness of Causes,' in order to distinguish clearly the case of alternative from that of co-operating or concurrent causes, noticed in the last paragraph '.
- 1 It is sometimes doubted whether the same effect is ever really due to different causes, and it may be conceded, I think, that different causes never do produce precisely the same aggregate of effects. Together with certain common effects, they produce certain divergent effects, and it is the presence of these, indeed, that enables us to determine the particular cause which has been at work in the particular instance. There is, however, nothing in this circumstance inconsistent with the occurrence of some one or more effects common to all the causes. Thus, the whole group of effects produced severally by heat, electricity, impact, differs widely, but, at the same time, the motion of a needle may be a common part of the effect in all three instances, and, when we see the needle in motion, we may be unable to say to which of the three causes motion is due. Similar considerations may be applied to the cases of ignition, and death, which are favourite illustrations of the operation of a plurality of causes. Taking A, B, C, D as causes or combinations of causes, and a, b, c, &c. as individual portions of the aggregate effects produced by the causes, we may conceive A as producing a b c d e, B as pro-

- (4) It frequently happens that between the original cause and the ultimate effect there intervene a number of intermediate causes. Thus, suppose we make an experiment by which motion is converted into heat, heat into electricity, and electricity into chemical affinity; we may, roughly speaking, say that motion has been the cause of the chemical affinity, or chemical affinity the effect of the motion, but, speaking strictly, we ought to enumerate the intervening causes.
- (5) Sometimes a number of effects appear to be produced simultaneously by the same cause. Thus, it would appear that there are many cases in which, if one of the agents, motion, heat, light, electricity, magnetism, and chemical affinity, is excited, the rest are developed simul-

ducing d e f g h, C as producing c d e i k l, D as producing e m n o. In this case, e may be regarded as an effect due to any one of the causes A, B, C, D, though the 'attendant circumstances,' as they are often called, are widely different in each instance. If, therefore, we were to state the doctrine of Plurality or 'Vicariousness' of Causes exactly, we should say, not that the same effect may be due to different causes, but that, of the total effects due to different causes, a certain portion is often found to be common to all. For purposes of practice, however, the ordinary mode of statement is sufficiently precise.

It seems hardly necessary to remark that it is no valid objection to the doctrine of Plurality of Causes that we are sometimes able to detect between the alternative causes and the identical effect some set of conditions which is the same in all cases. This discovery only removes the plurality of causation one step further back, and the doctrine can only be consistently denied by those who maintain that at no single point in the series of receding causes can we find the same effect produced, or capable of being produced, by distinct causes.

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taneously. These simultaneous effects, whether we conceive that they are really or only apparently simultaneous, would be called *joint* or common effects of the cause. Similarly the expression 'joint effects' would be employed for the effects produced by the same cause on different bodies, or different portions of the same body. Thus, if a blow bruises my forehead, and at the same time gives me a headache, the bruise and the headache may be called joint effects of the blow. These joint effects may be, as it were, in different degrees of descent from the same cause. Thus, if the headache incapacitates me for work, my incapacity for work and the bruise on my forehead will be joint effects, but in different degrees of descent from the original cause.

Any phenomena which are connected, either as cause and effect, and that either immediately or remotely, or as joint effects, and that either in the same or in different degrees of descent from the same cause, may be spoken of as being causally connected, or as causal relations, or as being related to one another through some fact of causation.

I now proceed to the statement of the Inductive Methods.

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^{*}See Grove's Correlation of Physical Forces, Concluding Remarks. What Sir W. Grove calls 'Force' would now be denominated 'Energy,' and the doctrine of the 'Correlation of Physical Forces' would be subsumed under that of the 'Conservation of Energy.'

METHOD OF AGREEMENT.

CANON 5.

If two or more instances of the phenomenon under investigation have only one other circumstance in common, that circumstance may be regarded, with more or less of probability, as the cause (or effect) of the given phenomenon, or, at least, as connected with it through some fact of causation.

Wherever the phenomenon a is found, we observe that b is found, either invariably or frequently 7, in conjunction with it. This fact leads us to suspect that there is some causal connexion between them. On what grounds, and under what circumstances, are we justified in drawing such an inference? And what is the particular character of the inference which we are justified in drawing? The answer to these questions involves many difficulties, of which I shall now attempt to offer a solution.

When antecedents and consequents are discriminated in this discussion, antecedents will be represented by Roman capitals, A, B, C, &c., and consequents by Greek characters, a, β , γ , &c. When circumstances are not distinguished as antecedents and consequents, I shall employ the small Roman letters, a, b, c, &c.

The statement of the Canons is taken, with some modifications, from Mr. Mill's Logic. The authorities for the various examples, when these are not of a familiar character, are cited at the foot of the page.

⁷ I add 'or frequently,' as it is not necessary that the conjunction shall be invariable. The student need not, however, at present trouble himself with this distinction, which will be fully explained below. See pp. 137-8, 145-7.

Now, suppose that we have A B followed by $\alpha \beta$, and A C by α γ; it might, at first sight, appear that A must be the cause of a, or, if we were attempting to ascertain the effect of a given cause (which, however, is a much rarer application of this method), that a must be the effect of A. And there is much plausibility in this supposition, for, provided that all the other circumstances remain the same, whatever can, in any given instance, be excluded, or, to use the technical term, eliminated without prejudice to a phenomenon, cannot have any influence on it in the way of causation, nor, making the same proviso, can an effect which disappears be due to a cause which continues to operate. Thus, if we were attempting to find the cause of a given effect a, it might be argued that B cannot be its cause, for it is absent in one of the cases where a is present, and similarly of C; but that a must be due to some cause; and, consequently, it is due to A, the only antecedent remaining. Or, if we were attempting to find the effect of a given cause A, it might be argued that β cannot be its effect, for it is absent in one of the cases where A is present, and similarly of γ ; but that, as a has been permanently present, A must be its cause. If it were not for the fact that the same event may be due to a great number of distinct causes (as is exemplified in the familiar cases of motion, death, disease, &c.), this reasoning would be perfectly Now it will be observed that, when B was removed, it was replaced by C. It is, therefore, conceivable that a may have been due to B in the first instance, and

to C in the second, it being, of course, in each case, only a portion of the effect, the remaining portions being respectively \$, \gamma, and A having been throughout inoperative. This consideration, it is plain, vitiates the reasoning, whether we are attempting to discover the effect of a given cause or the cause of a given effect. Thus, suppose that there are two distinct drugs, either of which is potent to remove a given disease, and that, in administering each of them, we mix it with some perfectly inert substance, which is the same in each case; if the principles of the above reasoning were correct, and we were justified in neglecting to take account of what may be called the Plurality of Causes, we should be at liberty to argue (if we were seeking the cause of a given effect) that the restoration of the patients to health was, in each case, due to the inert substance, or (if we were seeking the effect of a given cause) that the inert substance was the cause of their restoration to health.

But, if the Method of Agreement is open to so serious an objection, it may be asked on what grounds is it recognised as an Inductive Method? The answer is that, by the multiplication and variation of instances, the possible error due to the Plurality of Causes may be rendered less and less probable, till, at last, for all practical purposes, it may be regarded as having disappeared. Thus, if to the instances A B, $\alpha\beta$; A C, $\alpha\gamma$; we can add A D, $\alpha\delta$; A E, $\alpha\epsilon$, &c. &c.; it is plain that we may, at each step, be very considerably diminishing the possibility of an error in our reasoning, and, after a

certain number of instances, may be justified in feeling morally certain that we have avoided it. It is not likely that, in a number of instances, each agreeing in some one circumstance (besides the phenomenon which is being investigated) but differing as widely as possible in all other circumstances, the same event should in each case, or in a majority of cases, or in even a great number of cases, be due to different causes. The chance of an inert substance being successively mixed with two potent drugs, and of the effects which are really due to them being erroneously ascribed to it, is, in the present state of medical science, but a very slight one; but the probability is obviously considerably diminished, if instead of two such errors we suppose three, instead of three we suppose four, and so on.

For the sake of simplicity, I have assumed groups of two antecedents and two consequents (AB, aB; AC, ay; &c. &c.), but it is extremely seldom that we find in nature combinations so simple. We have usually a vast mass of antecedents and a vast mass of consequents (or, to state the same proposition in more scientific language, a vast mass of antecedents all, or most of them, contributing to a complex effect), and hence it often becomes a matter of extreme difficulty to discover a collection of instances which, presenting the phenomenon in question, agree in only one other circumstance or even in a small number of other circumstances. The difficulty, therefore, of rigidly satisfying the requirements of the Method must be added to what Mr. Mill calls its

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characteristic imperfection, namely, the uncertainty attaching to its conclusions from the consideration of the Plurality of Causes.

But there is still a third difficulty incident to the Method of Agreement, which however is, in a majority of cases, of a theoretical rather than a practical nature. If we insisted literally on the fulfilment of the condition that the instances presenting the given phenomenon should have only one other circumstance in common, it would be simply impossible to find such instances. All instances will be found to agree in a number of circumstances which are immaterial to the point under investigation. Thus, if we are enquiring into the properties of a group of external objects, they will all agree in the fact that they are subject to the action of gravity, and probably also in the facts that they are surrounded by atmospheric air and exposed to the light of the sun; but, if these facts do not affect the subject of our enquiry, we may pass them over as if they had no existence. When, therefore, we employ the expression 'only one circumstance in common,' we must be understood to mean 'only one material circumstance,' and to exclude all circumstances which a wide experience or previous inductions have shown to be immaterial to the question before us. It need hardly be added that, in forming this judgment as to the material or immaterial character of the circumstances, the greatest caution is often required.

But, suppose we have ascertained (when enquiring into the cause of a given effect) that the instances agree

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in only one antecedent (or rather one material antecedent), namely A, and that we have so multiplied and varied the instances as to have satisfied ourselves that we have excluded the possibility of a Plurality of Causes, are we justified in drawing the inference that A is the cause of a? We are so justified, for a must be due to something which went before it, and, as it has been shown that it is not due to any of the other antecedents, it must be due to A. Similarly, if our object be to enquire into the effect of a given cause A, we are justified, if we discover a consequent a, of which we can assure ourselves that it is not due to any of the other antecedents, in regarding it as the effect of A.

Hitherto, we have supposed the antecedents and consequents to be discriminated. But, suppose that we have a number of phenomena a b c d e, a d e f g, &c., in which we cannot discriminate them, how will the conclusions of the Method of Agreement be affected? There will, as in the former cases, obviously be the difficulties arising from Plurality of Causes and the complexity of the phenomena. Supposing, however, these to be overcome, and two circumstances only, a and b, to have been ascertained to be common to all the instances, what conclusion shall we be justified in drawing with reference to the connexion between a and b? It is only reasonable to suppose that they must be causally connected in some way, else their connexion would be a mere casual coincidence; a supposition which we assume to have been excluded by the number and variety of the instances examined. But they need not necessarily stand to each other in the relation of cause and effect, for they may be common effects (in the same, or in different degrees of descent) of some cause which has itself ceased to operate. In social and physiological phenomena this is frequently the case. A disease will leave effects behind it which will continue to co-exist for years after the disease itself has passed away, and which, though not standing to each other in the relation of cause and effect, are thus causally connected. The social condition of any old country is, to a great extent, an aggregate of such effects, the original cause or causes of which have long ceased to have any existence.

It should be noticed that the Method of Agreement is mainly, though not exclusively, a Method of Observation rather than of Experiment, and that it is applied far more frequently for the purpose of enquiring into the causes of given effects than into the effects of given causes. The reason of this peculiarity is that in trying an experiment, or in enquiring into the effect of a given cause, we are generally able to employ one of the other Methods, which, as will be seen hereafter, are not exposed to the same difficulties as the Method of Agreement.

It should also be noticed that where, after a careful elimination and an examination of a sufficiently large number of instances, we have, instead of two, some three, four, or more circumstances common to all the instances, we may, with much probability, regard them all, unless we know or suspect any of them to be immaterial circumstances, as being causally connected. If the common circumstances be a, b, c, d, this is all that we can infer. But, if they be A, B, C, α , we may infer that the cause of α is certainly either A or B or C, or some two of them acting jointly, or all acting together, while those common antecedents, which do not either constitute or contribute to the cause, probably stand in some causal relation to it, and consequently to its effect α . Similar conclusions may be drawn, if the common circumstances left after elimination be A, α , β , γ . Thus, for instance, α , β , γ might all be joint effects of A, or α might be its immediate effect, and β , γ effects of α , and so on.

It is perhaps not superfluous to remind the student that, in the application of this Method, he should be peculiarly careful not to overlook any instance in which the given phenomenon is unaccompanied by the other circumstance. Such an instance should at once lead him to suspect that some third common circumstance, which may be the true cause (or effect) of the given phenomenon, has escaped his attention, but this, if it be the case, does not necessarily vitiate his conclusion. If the given phenomenon be the consequent, and this other circumstance the antecedent, such an instance may only point to some other and independent cause of the phenomenon in addition to the cause he supposes himself to have ascertained. If, on the other hand, the given phenomenon be the antecedent, and this other circumstance the consequent, such an instance may only point to a counteracting cause which, in this exceptional case, frustrates

the supposed effect. The only condition essential to an application of the Method of Agreement is that the cases on which the inference is founded shall present only two circumstances in common. It is not necessary that these circumstances should invariably be found in conjunction, provided that in the cases where they are found in conjunction no other common circumstance can be detected. I shall recur to this subject below.

In the statement of the Canon, I have thought it desirable to introduce the expression 'with more or less of probability,' in order to show that, under no circumstances, does an inference drawn in accordance with the Method of Agreement attain to absolute and formal certainty, though, as we have seen, it may attain to moral certainty.

As familiar examples of the employment of the Method of Agreement, the following may be adduced:---

After taking a particular kind of food, whatever else I may eat or drink, and however various my general state of health, the temperature of the air, the climate in which I am living, and my divers other surroundings, I am invariably ill; I am justified in regarding the food as the probable cause of my illness, and avoid it accordingly. This example furnishes a good illustration both of the difficulties and of the possible cogency of the Method of Agreement. What made me ill on each of two, three, or four occasions, may have been some viand different from the

⁸ See pp. 145-7.

one in question, but it is very unlikely, if the number of occasions on which the inference is based be considerable, that it has been a different viand on each of them.

I find that a certain plant always grows luxuriantly on a particular kind of soil; if my experience of the other conditions be sufficiently various, I am justified in concluding that the soil probably possesses certain chemical constituents which are peculiarly favourable to the production of the plant.

Trade is observed to be in a languishing condition wherever there exist certain restrictions, such as high duties, difficulties thrown in the way of landing or locomotion, &c.; if it could be ascertained that these countries agreed in no other respect which could influence the condition of trade, except in being subject to these restrictions, it might be inferred with considerable probability that the commercial depression was due to the restrictions as a cause.

In all these cases, it will be seen that the great difficulty consists in ascertaining that the supposed cause is the only circumstance, or the only material circumstance, which, in addition to the phenomenon itself, the various instances possess in common.

I now append a few instances of a less familiar nature:—

The occurrence of Aurora Borealis has, under meteorological conditions of very different character, been invariably found to be accompanied by considerable magnetic disturbances. It is rightly inferred that there is some causal connexion between magnetic disturbance and the occurrence of the Aurora Borealis.

It has been observed uniformly, and under a variety of circumstances, that, wherever an indiscriminate system of almsgiving has prevailed, the population has, sooner or later, become indolent and pauperised. This fact may be noticed especially in the neighbourhood of large monasteries, in parishes where large sums of money are distributed in the shape of 'doles,' in places which are the residence of rich and charitable but injudicious persons, and the like. The reason is not difficult to discover. The unfortunate recipients of the charity are left without the ordinary motives to exertion, and consequently, when the abnormal supply ceases, or becomes too small for the wants of an increased population, being without self-reliance or any special skill, they have no resource but beggary.

After a variety of experiments on substances of the most different kinds, and under the most different circumstances, it has been found that, as a body passes from a lower degree of temperature to a higher, it invariably undergoes a change of volume, though that change may not always be in the same direction, it being, in the great majority of cases, in the direction of expansion, but, occasionally, in that of contraction. Hence it has been inferred that change of volume is an invariable effect of change of temperature (it being understood, of course, that pressure and other circumstances, as, for instance, the chemical condition of the body, remain the same).

It has been supposed by some writers on physics that we may go further than this conclusion, and state that augmentation of temperature is invariably followed by augmentation of volume, and diminution of temperature by diminution of volume, the exceptions of water as well as of bismuth and of the casting-metals generally (which suddenly expand at the moment of solidification) being explained as anomalies due to some interfering cause. We are, however, at present so little acquainted with the intimate constitution of bodies, that it might be rash to state the proposition in this form, and, stated as above, it is open to no exception 10.

* Water follows the general rule, and continues to contract in bulk as its temperature is lowered, till it reaches about 39° Fahrenheit or 4° Centigrade, when it begins to expand, and continues to do so till after its conversion into ice, so that a given weight of water at the temperature (say) of 37°, or when frozen, occupies more space than it occupied at (say) the temperature of 40°. This anomaly is somewhat boldly explained by Sir W. Grove as due to the setting in of the process of crystallization, which he supposes to begin at 39°, and to interfere with the ordinary law of contraction and expansion. (See Grove's Correlation of Physical Forces, fifth ed. p. 58, &cc.)

I adduce this instance as an example of the Method of Agreement rather than of the Method of Concomitant Variations, because the argument, as here stated, rests rather upon the variation of circumstances and the great diversity of bodies in which the law is found to hold good, than upon the relation between the various degrees of expansion or contraction and the various degrees of temperature in the same body. Had the stress been laid upon the latter consideration, the argument would undoubtedly have been an instance of the Method of Concomitant Variations.

It frequently happens, in fact, that two or more Methods are combined in the same proof. In the present instance, as will be seen below, the argument as applied to each particular kind of body The following example, which also illustrates the caution necessary to be observed in framing a general proposition, is extracted from Sir John Herschel's Discourse on the Study of Natural Philosophy 11:—

'A great number of transparent substances, when exposed in a certain particular manner, to a beam of light which has been prepared by undergoing certain reflexions or refractions (and has thereby acquired peculiar properties, and is said to be "polarised"), exhibit very vivid and beautiful colours, disposed in streaks, bands, &c. of great regularity, which seem to arise within the substance, and which from a certain regular succession observed in their appearance, are called "periodical colours." Among the substances which exhibit these periodical colours occur a great variety of transparent solids, but no fluids and no opaque solids. Here, then, there seems to be sufficient community of nature to enable us to use a general term, and to state the proposition as a law, viz. transparent solids exhibit periodical colours by exposure to polarized light. However, this, though true of many, does not apply to all transparent solids, and therefore we cannot state it as a general truth or law of nature in this form; although the reverse proposition, that all solids which exhibit

(mercury, for instance) is an argument based on the Method of Concomitant Variations; but when we proceed to extend the experiment to other bodies, and then argue from the variety of the bodies examined that a body, in passing from one degree of temperature to another, invariably undergoes a change of volume, it appears to me that we are no longer employing the Method of Concomitant Variations but the Method of Agreement. It must be borne in mind that the object of our enquiry is not strictly the effects of heat (for the total effects of heat, inasmuch as we cannot wholly exhaust any body of its heat, must be unknown to us), but the effects of a change of temperature.

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such colours in such circumstances are transparent, would be correct and general. It becomes necessary, then, to make a list of those to which it does apply; and thus a great number of substances of all kinds become grouped together in a class linked by this common property. If we examine the individuals of this group, we find among them the utmost variety of colour, texture, weight, hardness, form, and composition; so that, in these respects, we seem to have fallen upon an assemblage of contraries. But, when we come to examine them closely in all their properties, we find they have all one point of agreement, in the property of double refraction, and therefore we may describe them all truly as doubly refracting substances. We may, therefore, state the fact in the form, "Doubly refracting substances exhibit periodical colours by exposure to polarized light;" and in this form it is found, on further examination, to be true, not only for those particular instances which we had in view when we first propounded it, but in all cases which have since occurred on further enquiry, without a single exception; so that the proposition is general, and entitled to be regarded as a law of nature.

The experiments by which Dr. Wells 19 established his Theory of Dew afford a remarkable example of the Method of Agreement. By employing various objects of different material under a variety of circumstances,

12 Dr. Wells' Memoir on the Theory of Dew, which had become very scarce, was reprinted by Longmans and Co. in 1866. It is very brief, and well deserves to be carefully read by every student of scientific method. Sir John Herschel (Natural Philosophy, § 168) speaks of the speculation as 'one of the most beautiful specimens' he can call to mind 'of inductive experimental enquiry lying within a moderate compass.' Mr. Mill also employs it as one of his Miscellaneous Examples in Bk. III. ch. ix. of his Logic.

he showed that, whatever the texture of the object, the state of the att phere, &c., it is an invariable condition on of dew that the object on which it is of the de depos , sall be colder than the surrounding atmosphere .e greater coldness of the object being itself product by the radiation of heat from its surface. This, J quote the words of Sir John Herschel, is the case not only with 'nocturnal dew,' but with 'the analogous phenomena' of 'the moisture which bedews a cold metal or stone when we breathe upon it; that which appears on a glass of water fresh from the well in hot weather; that which appears on the inside of windows when sudden rain or hail chills the external air; that which runs down our walls when, after a long frost, a warm moist thaw comes on.'

It is by the Method of Agreement that we discover the symptoms of a disease, the signs of a political revolution, national characteristics, the order of superposition among geological strata, grammatical rules, and the like.

The first division of Bacon's instantia solitaria coincides with the cases contemplated in the Method of Agreement, as the second coincides with the cases contemplated in the Method of Difference. The example employed in the first is so remarkable both in itself, and as an anticipation of Newton's Speculations on Colour, that I may adduce it as an additional instance of the Method of Agreement:—

'Exempli gratia: si fiat inquisitio de natura coloris, instantiæ solitariæ sunt prismata, gemmæ crystallinæ, quæ

parietem. Item rores, &c. Istæ enime a habent commune cum coloribus fixis in floribus, gene coloratis, metallis, lignis, &c. præter ipsum colorem. Ifacile colligitur, quod color nil aliud sit quam modificatio imaginis lucis immissæ et receptæ: in priore genera, per gradus diversos incidentiæ; in posteriore, per tex tras et schematismos varios corporis. Istæ autem instantaæ sunt solitariæ quatenus ad similitudinem 18.

In attempting to ascertain the cause of a given effect, a, it may happen that we find a particular antecedent, A, frequently, but not invariably, accompanying it. If, in those cases which present both a and A, no other common circumstance can be detected, we may infer that A is probably a cause of a. I say 'a cause,' for the fact that a may be present without A is a proof that A is not the only cause. My meaning will be plain from the following example:—

We compare instances in which bodies are known to assume a crystalline structure, but which have no other point of agreement; in the great majority of instances, though not in all, we find that these bodies have assumed their crystalline structure during the process of solidification from a fluid state, either gaseous or liquid, and, so far as we can ascertain, these cases have no other circumstance in common. From these facts it may be reasonably inferred that the passage from a fluid to

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¹⁸ Novum Organum, Lib. II. aph. xxii.

a solid state is a cause, though not the only cause, of crystallization 14.

Again, when A is frequently, though not invariably, followed by a, and there is, so far as we can ascertain, no other common antecedent, we are justified in suspecting that A is a cause of a, and that, in the cases where a does not occur, the operation of A is counteracted by some other cause. If, for example, a certain occupation or mode of living is found to be usually, though not invariably, attended by a particular form of disease, we seem to be justified in regarding this occupation or mode of living as a cause of the disease, and in explaining the few cases in which the disease does not occur as due to exceptional and counteracting circumstances.

Similarly, when a and b are found in frequent, though not invariable, conjunction 16, and, in the cases where

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This example is adopted, with considerable modifications, from one which occurs in Mr. Mill's Logic, Bk. III ch. viii. § 1. I am indebted to Sir John Herschel for pointing out to me that Mr. Mill's example (which I had originally adopted as it stood) is too broadly stated. 'The solidification of a substance from a liquid (it should be fluid) state is not 'an invariable,' but only an usual 'antecedent of its crystallization.' The reader will find several exceptions noticed in Watts' Dictionary of Chemistry, art. Crystallization.

The invariable conjunction of two phenomena, when the presence of the one implies the presence of the other, and the absence of the one the absence of the other, is a case falling under the Double Method of Agreement, to be explained presently; but those cases, in which we simply know that a given phenomenon is invariably preceded or invariably followed by another, fall under the Method of Agreement just discussed. If a given phenomenon is, so far as we know, invariably preceded by another, this fact justifies

they are found together, there occurs, so far as we can ascertain, no other common circumstance, we are justified in suspecting that there exists some causal connexion between them.

The student, who is acquainted with the science of Medicine, will find a good illustration of the extreme difficulty attending the application of the Method of Agreement, as well as of the Joint Method of Agreement and Difference (to be noticed presently), in the disputes which still occur as to the cause of the mental disease which is known as Atactic Aphasia, that is, the condition in which, with reference to certain sounds, the patient has lost the power of co-ordinating the muscles of speech. The French physiologist, M. Broca, laid down the position that this disease is invariably due to a lesion of the third frontal convolution of the left hemisphere of the brain, the disease being invariably attended by the specific lesion, and the lesion never occurring without the disease. His followers maintain that the instances are decisive in favour of this theory, while the apparent exceptions admit us in suspecting (though it does not prove) that the antecedent is not only a cause, but the only cause, of the given phenomenon. Such a conclusion can only be proved (even approximately) by the Double Method of Agreement. It is, however, as already pointed out, not in the invariableness of the conjunction, but in the fact that the instances examined present, so far as we can ascertain, only two phenomena in common, that the cogency of the Method of Agree-But of this fact invariableness of antecedence (or of ment consists. consequence) furnishes one of the strongest proofs, inasmuch as such invariableness implies a very wide variation of circumstances; hence the stress laid upon it in some of the examples adduced above.

of a satisfactory explanation; his opponents, on the other hand, assert that there are well-established cases both of atactic aphasia without the specific lesion, and of the lesion without aphasia 14.

METHOD OF DIFFERENCE.

CANON.

If an instance in which the phenomenon under investigation occurs, and an instance in which it does not occur, have every circumstance in common save one, that one occurring only in the former; the circumstance in which alone the two instances differ, is the effect, or cause, or a necessary part of the cause, of the phenomenon.

The circumstances a, b, c are found in conjunction with d, e, f, and the omission or disappearance of the circumstance a is found to be attended by the disappearance of the circumstance d. It is inferred that a and d are so connected that one is cause (or a necessary part of the cause) and the other effect. If, moreover, it can be ascertained that a is the antecedent and d the con-

Reports, vol. ii.; a Pamphlet by Dr. Frederic Bateman of Norwich, published by J. E. Adlard, Bartholomew Close, London, 1868; Dr. Reynolds' System of Medicine, vol. ii. pp. 442-444; and various reports of discussions published in the Lancet and other medical journals. I have to thank my friends, Professors Acland and Rolleston, for their kindness in supplying me with information on this interesting subject, and regret that my space prevents me from pursuing it at greater length.

sequent, or that, though there are instances in which d occurs without a, there are no instances in which a occurs without d, we may proceed to infer (in the latter case, on the ground that a phenomenon may have more than one cause, but that a cause, unless counteracted by some other cause, must be attended by its effect) that a is the cause, and d the effect. Similarly, if the circumstances a, b, c are found in conjunction with d, e, f, and the introduction of the circumstance x into the former set of phenomena is found to be attended by the appearance of the circumstance y in the latter set of phenomena (so that they may be represented respectively as a, b, c, x; d, e, f, y), it may be inferred that x and y are related as cause and effect; or, if x be the antecedent and y the consequent, or the appearance of x be invariably attended by the appearance of y while the appearance of y is not invariably attended by the appearance of x, that x is the cause and y the effect. The reasons on which the Canon rests are obvious. All other circumstances remaining the same, if the introduction or omission of any circumstance be followed by a change in the remaining circumstances, that change must be due to such introduction or omission, as an effect to a cause; or, if two new circumstances enter simultaneously, without producing any other change in the phenomenon, these two circumstances (except on the improbable supposition that they are two causes exactly counteracting each other) must be related as cause and effect, though we may be unable to say which of the two is cause and

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which effect. 'The Method of Agreement,' says Mr. Mill, 'stands on the ground that whatever can be eliminated, is not connected with the phenomenon by any law. The Method of Difference has for its foundation that whatever can not be eliminated, is connected with the phenomenon by a law.' In the Method of Difference, the instances agree in everything, except in the possession of two circumstances which are present in the one instance and absent in the other. In the Method of Agreement, the various instances compared (for here we generally require more than two instances) agree in nothing, except in the possession of two circumstances which are common to all the instances. One Method is called the Method of Agreement, because we compare various instances to see in what they agree; the other is called the Method of Difference, because we compare an instance in which the phenomenon occurs with another in which it does not occur, in order to see in what they differ.

Instances of the Method of Difference are not far to seek. A piece of paper is thrown into a stove; we have no hesitation in regarding its apparent consumption as the effect of the heat of the fire, for we feel assured that the sudden increase of temperature is the only new circumstance to which the piece of paper is exposed, and that, therefore, any change in the condition of the paper must be due to that cause. A bullet is fired from a gun, or a dose of prussic acid is administered, and an animal instantly falls down dead. There is no hesitation in

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ascribing the death to the gun-shot wound or the dose of poison. Nor is this confidence the effect of any wide experience, for, if it were the first time that we had seen a gun fired or a dose of poison administered, we should have no hesitation in ascribing the altered condition of the animal to this novel cause; we should know that there was only one new circumstance operating upon it, and, consequently, that any change in its condition must be due to that one circumstance. In all these instances, there is the introduction of a new antecedent. x, to which the new consequent, y, must be due. But, if the omission of one circumstance be attended by the omission of another, we may argue with equal confidence. I withdraw my hand from this book which is resting upon it, and the book instantly falls to the ground; there is no hesitation in referring the altered position of the book to the withdrawal of my support. A man is deprived of food, and he dies; we have no hesitation in ascribing the disappearance of the phenomenon we call life to the withdrawal of the means by which it is maintained. In these instances, we have certain antecedents, followed by certain consequents, and, observing the simultaneous or successive disappearance of A and a, we have no hesitation in connecting the two as cause and effect.

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All crucial instances (instantiæ 17 crucis, as they are

¹⁷ Inter prærogativas instantiarum ponemus loco decimo quarto instantias crucis; translato vocabulo a crucibus, quæ, erectæ in bivils, indicant et signant viarum separationes. Has etiam instantias

called by Bacon) are applications of the Method of Difference. A crucial instance is some observation or experiment which enables us at once to decide between two or more rival hypotheses. It will be familiar to every one in the form of the *chemical test*, as where we apply an acid for the purpose of determining the character of a metal, or a metal for the purpose of detecting latent poison. According to the metaphor, there are two or more ways before us, and the observation or experiment acts as a 'guide-post' (crux) in determining us which to take. The following beautiful example of a Crucial Instance is borrowed from Sir John Herschel 18.

'A curious example is given by M. Fresnel, as decisive, in his mind, of the question between the two great opinions on the nature of light, which, since the time of

decisorias, et judiciales, et in casibus nonnullis instantias oraculi, et mandati, appellare consuevimus. Earum ratio talis est. Cum in inquisitione naturse alicujus, intellectus ponitur tanquam in sequilibrio, ut incertus sit, utri naturarum e duabus, vel quandoque pluribus, causa naturæ inqusitæ attribui aut assignari debeat, propter complurium naturarum concursum frequentem et ordinarium; instantie crucis ostendunt consortium untus ex naturis (quoad naturam inquisitam) fidum et indissolubile, alterius autem varium et separabile; unde terminatur quæstio, et recipitur natura illa prior pro causa, missa altera et repudiata. Itaque hujusmodi instantiæ sunt maximæ lucis, et quasi magnæ auctoritatis; ita ut curriculum interpretationis quandoque in illas desinat, et per illas perficiator. Interdum autem instantiæ crucis illæ occurrent et inveniunter inter jampridem notatas; at ut plummum novæ sunt, et de industria atque ex composito quæsitæ et applicatæ, et diligentia sedula et acri tandem erutæ.'-Novum Organum, Lib. II. aph. xxxvi.

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¹⁴ Discourse on the Study of Natural Philosophy, & 218.

Newton and Huyghens, have divided philosophers;' that is, between what is called 'the emission theory,' according to which light consists of actual particles emitted from luminous bodies, and what is called 'the undulatory theory,' according to which light consists in the vibrations of an elastic medium pervading all space.

'When two very clean glasses are laid one on the other, if they be not perfectly flat, but one or both in an almost imperceptible degree convex or prominent, beautiful and vivid colours will be seen between them; and if these be viewed through a red glass, their appearance will be that of alternate dark and bright stripes. These stripes are formed between the two surfaces in apparent contact, as any one may satisfy himself by using, instead of a flat plate of glass for the upper one, a triangular-shaped piece, called a prism, like a threecornered stick, and looking through the inclined side of it next the eye, by which arrangement the reflexion of light from the upper surface is prevented from intermixing with that from the surfaces in contact. Now, the coloured stripes thus produced are explicable on both theories, and are appealed to by both as strong confirmatory facts; but there is a difference in one circumstance according as one or the other theory is employed to explain them. In the case of the Huyghenian doctrine, the intervals between the bright stripes ought to appear absolutely black; in the other, half bright, when so viewed through a prism. This curious case of difference was tried as soon as the opposing consequences of the two theories were noted by M. Fresnel, and the result is stated by him to be decisive in favour of that theory which makes light to consist in the vibrations of an elastic medium 10.

19 Mr. Mill (Logic, Bk. III. ch. xiv. § 6) maintains that it does not follow from this experiment that 'the phenomena of light are results

The following is an example of a similar kind. It had been determined, from theoretical considerations, that, on the assumption of the undulatory theory, the velocity of light must be less in the more highly refracting medium, while, according to the emission theory, it ought to be greater. When M. Foucault had invented his apparatus for determining the velocity of light, it became possible to submit the question to direct experiment; and it was established by himself and M. Fizeau that the velocity of light is less in water (the more highly refracting medium) than in air, in the inverse proportion of the refractive indices. The result is, therefore, decisive in favour of the undulatory, or, at least, against the emission theory **O.

There is no science, perhaps, in which the Method of Difference is so extensively used as the science of Chemistry, and that because chemistry is emphatically a science of experiment. Almost any chemical experiment will serve as an instance of the Method of Difference. Mix, for example, chloride of mercury with iodide of potassium, and the result will be a colourless liquid at the top of the vessel with a brilliant red precipitate at

of the laws of elastic fluids, but at most that they are governed by laws partially identical with these.' But, though the experiment may not be decisive as in favour of the Undulatory Theory, it is undoubtedly decisive as against the Emission Theory. It may be necessary to add that the term 'fluids' would now be repudiated by those who hold the Undulatory Theory.

³⁰ See Lloyd's Wave Theory of Light, 3rd ed. Arts. 41, 42; Ganot's Physics, English translation, 12th edition, Art. 506.

this result to the mixture of the two liquids; and two similar experiments will enable us to determine that the chlorine has been set free from the mercury and united with the potassium, which itself has been set free from the iodine with which it was previously united, while the iodine has united with the mercury, the former producing chloride of potassium (dissolved in the colourless liquid), the latter iodide of mercury (the red precipitate).

The science of Heat (or, as Dr. Whewell proposes to call it, Thermotics) also furnishes excellent examples of the Method of Difference. The following instances are adapted from Professor Tyndall's *Heat a Mode of Motion* ²¹:—

'Here is a brass tube, four inches long, and of threequarters of an inch interior diameter. It is stopped at the bottom and screwed on to a whirling table, by means of which the upright tube can be caused to rotate very rapidly. These two pieces of oak are united by a hinge, in which are two semicircular grooves, intended to embrace the brass tube. Thus the pieces of wood form a kind of tongs, the gentle squeezing of which produces friction when the tube rotates. I partially fill the tube with cold water, stop it with a cork to prevent the splashing out of the liquid, and now put the machine in motion. As the action continues, the temperature of the water rises, and now the tube is too hot to be held in the fingers. Continuing the action a little longer, the cork is driven out with explosive violence, the steam which follows it producing by its precipitation a small cloud in the atmosphere.'

[&]quot; Third Edition, ch. i. §§ 14-16.

In this experiment it will be noticed that only one new antecedent is introduced, namely the motion of the machine; hence the increased temperature of the water and the various effects which follow upon it are due to the motion as a cause. The experiment, then, shows that heat is generated by the action of mechanical force.

The converse of this proposition, namely that heat is consumed in mechanical work, or, as it is often stated, transmuted into mechanical energy, is proved by the two next experiments.

'This strong vessel is filled at the present moment with compressed air. It has lain here for some hours, so that the temperature of the air within the vessel is now the same as that of the air of the room without it. At the present moment this inner air is pressing against the sides of the vessel, and if this cock be opened a portion of the air will rush violently out. The word "rush," however, but vaguely expresses the true state of things; the air which issues is driven out by the air behind it; this latter accomplishes the work of urging forward the stream of air. And what will be the condition of the working air during this process? It will be chilled. The air executes work, and the only agent it can call upon to perform the work is the heat to which the elastic force with which it presses against the sides of the vessel is entirely due. A portion of this heat will be consumed, and a lowering of temperature will be the consequence. Observe the experiment. I will turn the cock, and allow the current of air from the vessel to strike against the face of the pile "2".

That is, the thermo-electric pile, a delicate instrument for indicating very small changes of temperature. It is by means of this instrument that it has recently been shown that we receive heat (though, of course, in infinitesimal quantities) from the moon's rays.

The magnetic needle instantly responds; its red end is driven towards me, thus declaring that the pile has been *chilled* by the current of air.'

'Here moreover is a bottle of soda-water, slightly warmer than the pile, as you see by the deflexion it produces. Cut the string which holds it, the cork is driven out by the elastic force of the carbonic acid gas; the gas performs work, in so doing it consumes heat, and now the deflexion produced by the bottle is that of cold.'

The last experiment furnishes a good instance of the extreme simplicity of the examples by which scientific truths may often be illustrated.

The uncertainty which, as we have seen, always attaches to conclusions arrived at by the Method of Agreement renders it desirable that they should, wherever it is possible, be confirmed by an application of the Method of Difference. A beautiful instance of such a confirmation is adduced by Mr. Mill in the case of Crystallization, The Method of Agreement has already led us to the conclusion that the solidification of a substance from a fluid state is a very frequent antecedent of its crystallization, and so, probably, one, at least, of its causes. But the Method of Difference completes the evidence, and enables us to state positively that it is a cause.

'For in this case we are able, after detecting the antecedent A, to produce it artificially, and, by finding that a follows it, verify the result of our induction. The importance of thus reversing the proof was never more strikingly manifested than when, by keeping a phial of water charged with siliceous particles undisturbed for years, a chemist (I believe Dr. Wollaston) succeeded in obtaining crystals of quartz; and in the equally interesting experiment in which Sir James Hall produced artificial marble, by the cooling of its materials from fusion under immense pressure: two admirable examples of the light which may be thrown upon the most secret processes of nature by well-contrived interrogation of her²³.'

It will be noticed that the Method of Difference is specially adapted to the discovery of the effects of given causes, whereas, where it is our object to discover the cause of a given effect, we are usually compelled to have recourse to the Method of Agreement. The Method of Agreement is, in fact, mainly a Method of Observation, whereas the Method of Difference is mainly a Method of Experiment. We may indeed arrange the conditions of an experiment so as to satisfy the requirements of the Method of Agreement, and Nature may (as in the familiar case of lightning) herself satisfy the requirements of the Method of Difference, but, as a rule, it will be found that arguments based on observations fall under the former, and arguments based on experiments under the latter Method. It is hardly necessary to add that, wherever we have our choice between the two methods, we should invariably select the Method of Difference.

²⁹ Mill's Logic, Bk. III. ch. viii. § 1. I have been obliged, in accordance with what has been said on p. 146, to state, with considerable modifications, the conclusion in this instance as arrived at by the Method of Agreement. The account of the application to it of the Method of Difference has been stated in Mr. Mill's own words.

In the employment of the Method of Difference, the greatest care should be taken to introduce only one new antecedent, or at least only one new antecedent which can influence the result. As the whole force of the argument based on this Method depends on the assumption that any change which takes place in the phenomenon is due to the antecedent then and there introduced, it is plain that we can place no reliance on our conclusion unless we feel perfectly assured that no other antecedent has intervened. If, for instance, it is our object to ascertain the temperature of the atmosphere, we must take the greatest care that our thermometer is not affected by the heat radiated from or conducted by other bodies. The most curious examples of the disregard of this caution may be found in the History of Medicine. Something perfectly inert has been administered to a patient in combination with some powerful drug, some important alterations in his diet, or some strict régime; then the effects of the drug, diet, or régime have been unwittingly ascribed to the inert substance. Had the ancients recognised that instead of one cause acting on falling bodies, as appeared to them to be the case, there were really two, the action of gravity tending downwards and the resistance of the atmosphere pressing upwards, they could never have fallen into the gross error of supposing that bodies fall in times inversely proportional to their weights.

DOUBLE METHOD OF AGREEMENT.

CANON.

If two or more instances in which the phenomenon occurs have only one other circumstance in common, while two or more instances, falling within the same department of investigation, from which the phenomenon is absent have nothing in common save the absence of that circumstance; that circumstance is the effect, or the cause, or a necessary part of the cause, of the phenomenon. Moreover (supposing the requirements of the Method to be rigorously fulfilled), the circumstance proved by the Method to be the cause is the only cause of the phenomenon.

The uncertainty attaching to the Method of Agreement may, even where it is impossible to have recourse to the Method of Difference, be, to some extent, remedied by the employment of what is called by Mr. Mill the Joint Method of Agreement and Difference, or the Indirect Method of

In recent editions I have inserted in the statement of the Canon the words 'falling within the same department of investigation,' because, as has been pointed out to me, the student might otherwise not see that, for the purposes of comparison, the positive and negative instances must be in pari materia. Thus, if the subject of enquiry is language, the negative as well as the positive instances must be sought in the department of language; or, if the subject of enquiry lies within the sphere of morals, or of physical forces, or of living organisms, the negative as well as the positive instances must be sought within those respective departments. Practically, however, there is no occasion for definite rules on this head, as the commonsense of the investigator is quite sufficient to keep him within the limits of the enquiry.

Difference. This Method consists in a double employment of the Method of Agreement and a comparison of the results thus obtained, the comparison assimilating it to the Method of Difference. We, first of all, compare cases in which the phenomenon occurs, and, so far as we can ascertain, find them to agree in the possession of only one other circumstance. But, though we may not be justified in regarding this inference as certain, we may increase our assurance by proceeding to compare cases in which the phenomenon does not occur. If these cases agree in nothing but the non-possession of the circumstance which the other cases agreed in possessing, we have a set of negative instances agreeing in nothing but the absence of the given phenomenon and the absence of the aforesaid circumstance. The set of negative instances may now be compared with the set of positive instances, and we may argue thus: The positive instances agree in nothing but the presence of the given phenomenon and this other circumstance, and the negative instances agree in nothing but the absence of the given phenomenon and this other circumstance. Hence we may regard it as a highly probable inference that they are connected together as cause and effect. I say 'highly probable,' for, as we are not absolutely certain that the conditions of the Method of Agreement have been satisfied in the case of the positive instances, so, from the extreme difficulty of proving a negative, we must be still less certain that they have been satisfied in the case of the negative instances. What (in addition

to another advantage, to be noticed presently) is gained by the Method is a sort of double assurance, so far as the assurance goes. If the one set of instances agreed in nothing but the presence of the two circumstances, and if the other set of instances agreed in nothing but the absence of the two circumstances, then we should be able to infer, by the Method of Difference, that the introduction of the given phenomenon (which we will suppose to be the consequent) always follows on the introduction of the other circumstance (which we will suppose to be the antecedent), and, vice versa, that the removal of the given phenomenon always follows on the removal of the other circumstance, or, in other words, that the given phenomenon is the effect and the other circumstance the cause.

But this Method, supposing its conditions to be rigorously satisfied, possesses one advantage peculiar to itself. The Single Method of Agreement, as we have seen, is always theoretically open to the objection arising from Plurality of Causes, but this Method, if the set of negative instances be perfect, is not only free from that objection, but also sustains the conclusion that the inferred cause is the *only* cause of the phenomenon in question (or, in case we do not know which is antecedent and which is consequent, that a and b are so connected that one of them is the cause and the only cause of the other). 'In the joint method,' says Mr. Mill²⁶, 'it is supposed not only that the instances in

^{*} Mill's Logic, Bk. III. ch. x. § 2.

which a is agree only in containing A, but also that the instances in which a is not agree only in not containing A. Now, if this be so, A must be not only the cause of a, but the only possible cause: for if there were another, as for example B, then in the instances in which a is not, B must have been absent as well as A, and it would not be true that these instances agree only in not containing A.' It may be asked, then, if the negative branch of the argument be so forcible, why should we employ the positive branch? It is by means of the positive branch that we are, as it were, put on the track of the one other circumstance in which the instances presenting the given phenomenon agree, and by means of the negative branch that we prove the accuracy of our conclusion. 'It is generally,' continues Mr. Mill, 'altogether impossible to work the Method of Agreement by negative instances without positive ones: it is so much more difficult to exhaust the field of negation than that of affirmation.'

It is plain that the conditions of the Joint Method can only be rigorously fulfilled where there is an invariable conjunction between two phenomena, so that the two are (unless counteracting circumstances intervene) always present together and always absent together. For, if A be the *only* cause of a, the effect a cannot be present without the cause A, nor can the cause A be present without being attended by the effect a. Hence, invariable conjunction may be regarded as a sign that the conditions of this Method are fulfilled, and it is from the observation of such an invariable conjunction that the

argument frequently proceeds. In such cases, the number of instances, both positive and negative, which have been observed, is supposed to be so great and of such variety as to have excluded all other common circumstances except the presence or absence of the two phenomena in question.

The Joint Method of Agreement and Difference (or the Indirect Method of Difference, or, as I should prefer to call it, the Double Method of Agreement) is being continually employed by us in the ordinary affairs of life. If, when I take a particular kind of food, I find that I invariably suffer from some particular form of illness, whereas, when I leave it off, I cease to suffer, I entertain a double assurance that the food is the cause of my illness. I have observed that a certain plant is invariably plentiful on a particular soil; if, with a wide experience, I fail to find it growing on any other soil, I feel confirmed in my belief that there is in this particular soil some chemical constituent, or some peculiar combination of chemical constituents, which is highly favourable, if not essential, to the growth of the plant.

Dr. Wells' Essay on the Theory of Dew presents an extremely instructive instance of the application of the Double Method of Agreement:—

'It appears' (I am here quoting from Mr. Mill²⁶) 'that the instances in which much dew is deposited, which are very various, agree in this, and, so far as we are able to observe, in this only, that they either radiate heat rapidly or conduct

Mill's Logic, Bk. III. ch. ix. § 3.

it slowly: qualities between which there is no other circumstance of agreement than that, by virtue of either, the body tends to lose heat from the surface more rapidly than it can be restored from within. The instances, on the contrary, in which no dew, or but a small quantity of it, is formed, and which are also extremely various, agree (as far as we can observe) in nothing except in not having this same property. We seem, therefore, to have detected the characteristic difference between the substances on which dew is produced, and those on which it is not produced. And thus have been realized the requisitions of what we have termed the Indirect Method of Difference, or the Joint Method of Agreement and Difference.'

Several beautiful illustrations of the Joint Method of Agreement and Difference may be found in the recent discoveries made by means of Spectrum Analysis. I shall select one which is peculiarly interesting on account of its employment in the attempt to determine the constitution of the sun and some of the other heavenly bodies.

A very thin sheet of light proceeding from incandescent hydrogen is passed through a prism, and it is invariably found (with the exception of the third case mentioned in note 27) that in the spectrum thus obtained there are, in proportion to the intensity of the light, one, two, or more bright lines occupying precisely the same relative position. Moreover, very thin sheets of white light proceeding from various incandescent substances are passed through incandescent hydrogen, and the emergent light is then separated into its constituent elements by a prism. In the spectra thus obtained it is found that there are invariably (with the above-named

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exception) dark (or, under certain circumstances, bright²⁷) lines occupying exactly the same positions in the spectrum as the lines above mentioned. Hence it is inferred, by the Method of Agreement, that a sheet of light, whether it proceed directly from incandescent hydrogen itself, or be transmitted through it from some other incandescent substance, will (allowing for the above exception) invariably produce these lines. But, if we try the same experiments with any other element than incandescent hydrogen, although we may obtain bright or dark lines, we never find these lines occupying the same positions in the spectrum as the lines in question.

Here, then, we have the negative instances of the Double Method; and it is inferred (subject, of course, to the assumption that our knowledge of the negative instances is sufficiently complete) that the presence in the spectrum of these lines is invariably due either to a sheet of light proceeding directly from incandescent hydrogen, or to a sheet transmitted through it from some other incandescent substance; that is to say, that one or other of these is the cause, and the *only* cause of the presence

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The darkness of the lines is due to the property possessed by incandescent media of absorbing sheets of light of the same refrangibility as those emitted by them. When the absorption exerted upon the transmitted light is more than compensated by the luminosity of the hydrogen light, these lines, instead of being dark, appear bright, as is also the case when the sheet of light proceeds directly from incandescent hydrogen itself. There is still a third case. When the hydrogen emits as much light as it absorbs, there will be no line, dark or bright.

in the spectrum of these particular lines. When these lines are bright, it is doubtful whether the rays proceed directly from incandescent hydrogen or have been transmitted through it, but, when they are dark, the sheets must have been transmitted. Wherever, therefore, dark lines occupying these positions occur in the spectrum we may infer (deductively) the passage of the sheet of light through a medium composed wholly or partially of incandescent hydrogen. But we detect such lines in the spectrum of the sun and several of the stars, and hence (unless we suppose it possible or not improbable that there is in the sun or other stars some element agreeing in this respect with hydrogen, but differing in others) we may conclude that the sun and these other stars are surrounded with an atmosphere of incandescent hydrogen ³⁴.

The following examples are selected from a subject of a widely different character, the History of Language. M. Auguste Brachet, in his Historical Grammar of the

It must be understood that, in this example, I have not stated the historical steps by which the discovery was arrived at, but simply attempted to give a logical analysis of the arguments by which it would now be established. It was the exact coincidence of the bright lines in the hydrogen spectrum with the dark lines in the solar spectrum, which first led to the belief that hydrogen enters into the constitution of the solar atmosphere. It is now, however, rendered possible, through an ingenious contrivance, to separate, as it were, the solar atmosphere from the glowing body within it, and thus to obtain these lines bright instead of dark. The student will find a brief account of these discoveries in Professor Stokes' Address to the British Association in 1869.

French Tongue**, lays down the position that there are three sure tests by which we can discriminate between popular words derived from the Peasant Latin (lingua Latina rustica) by a regular process, and Latin words of learned origin imported into Modern French by scholars. These tests are (1) the continuance of the tonic accent; (2) the suppression of the short vowel; (3) the loss of the middle or medial consonant. It will be seen that it is by the employment of the Double Method of Agreement that M. Brachet arrives at these conclusions.

'Look at such words (i. e. words of popular origin) carefully, and you will see that the syllable accented in Latin continues to be so in French; or, in other words, that the accent remains where it was in Latin. This continuance of the accent is a general and absolute law: all words belonging to popular and real French respect the Latin accent: all such words as portique from pórtique, or viatique from viáticum, which break this law, will be found to be of learned origin, introduced into the language at a later time by men who were ignorant of the laws which nature had imposed on the transformation from Latin to French. We may lay it down as an infallible law, that The Latin accent continues in French in all words of popular origin; all words which violate this law are of learned origin: thus—

| LATIN. | POPULAR WORDS. | LEARNED WORDS. |
|------------|----------------|----------------|
| Alúmine | alún | alumine |
| Angelus | ánge | angelús |
| Blasphemum | blåme | òlasphéme |
| Cáncer | châncre | cancér |
| Cómputum | cómpte | compili |
| Débitum | détte | débit |
| Décima | dime | décime, &c. |

Dr. Kitchin's Translation, p. 32, 7th ed. pp. 44-48.

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We have seen that the tonic accent is a sure touchstone by which to distinguish popular from learned words. There is another means, as certain, by which to recognise the age and origin of words—the loss of the short vowel. Every Latin word, as we have said, is made up of one accented vowel, and others not accented—one tonic and others atonic. The tonic always remains; but of the atonics the short vowel, which immediately precedes the tonic vowel, always disappears in French: as in—

Bon(I)tátem bonté

San(I)tátem santé

Pos(I)túra posture

Clar(I)tátem clarté

Sep(tI)mána semaine (O. Fr. sepmaine)

Com(I)tátus comté

Pop(à)látus peuplé, &c.

'Words such as circuler, circulare, which break this law and keep the short vowel, are always of learned origin; all words of popular origin lose it, as cercler. This will be seen from the following examples:—

LATIN. POPULAR WORDS. LEARNED WORDS. Ang(ŭ)latus angulé anglé Hissph(ë)mare blåmer (O, Fr, blasmer) blasphémer Cap(I)tále capital cheptel Car(1)tátem cherté charité Circ(ŭ)láre cercler circulter, &cc.

'The third characteristic, serving to distinguish popular from learned words, is the loss of the medial consonant, i.e. of the consonant which stands between two vowels, like the t in maturus. We will at once give the law of this change:—All French words which drop the medial consonant are popular in origin, while words of learned origin retain it. Thus the Latin vocalis becomes, in popular French, voyelle, in learned French, vocale. There are innumerable examples of this: as—

| LATIN. | POPULAR WORDS. | LEARNED WORDS. |
|---------------------------------|----------------|----------------|
| $\mathbf{Au}(\mathbf{g})$ ústus | aoAt | auguste |
| Advo(a)átus | avout | avocat |

Lunk,

LATIN. POPULAR WORDS. LEARNED WORDS.

Anti(ph)one antienne antiphone
Oro(d)ontie créance crédence
Communi(o)are communier communiquer, &c.'

The requisitions of the Double Method of Agreement may be far from being rigorously fulfilled, and still two phenomena may be so frequently present together and so frequently absent together, that we may be justified in suspecting some causal connexion between them. Unless they were invariably absent together, as well as invariably present, and unless they were the only circumstances which were invariably present and absent together, we should not be justified in regarding one as the cause, and the only cause, of the other; but the mere detection of the fact that they are frequently present and absent together may justify us in believing that there is between them some causal connexion. The precise character of this causal connexion may hereafter be determined by one of the other inductive methods, or by bringing the case under a previous deduction. following instances will serve as illustrations of what has been here said.

Sir John Herschel conceives that he has detected a connexion between a full moon and a calm night: 'The only effect distinctly connected with its [the moon's] position with regard to the sun, which can be reckoned upon with any degree of certainty, is its tendency to clear the sky of cloud, and to produce not only a serene but a calm night, when so near the full as to appear round to

the eye—a tendency of which we have assured ourselves by long-continued and registered observation.' The precise nature of the causal connexion can here be determined: 'The effect in question, so far as the clearance of the sky is concerned, is traceable to a distinct physical cause, the warmth radiated from its [the full moon's] highly-heated surface; though why the effect should not continue for several nights after the full, remains problematic ***50.'

In this example, there is not, of course, an invariable connexion between the clear night and the full moon; for, in the determination of the weather, there are so many and so various causes at work that they must necessarily modify or counteract each other. The moon might exercise considerable influence, might, as Sir John Herschel says, have a tendency to produce a calm night and still be overpowered by other influences. It is sufficient, in order to lead us to suspect some causal connexion between the two phenomena, that we should find a calm night proportionably oftener, and oftener in a considerable proportion, when there is a full moon than when there is not. Thus, suppose that, after a long series of observations of nights when there is a full moon, we find the proportion of calm nights to nights which cannot be called calm to be as 5 to 2 (I am, of course, taking an imaginary case), and the proportion on ordinary nights to be as 3 to 2, there can be little doubt

^{*} Herschel's Familiar Lectures on Scientific Subjects, pp. 146.

that the full moon is, in some way or other, connected with the larger proportion of calm nights.

The employment of the Double Method of Agreement may lead to the detection of facts of causation in many instances of a similar kind. Thus, suppose that, in a particular part of the country, a particular wind is found to be proportionably oftener attended with rain than other winds, we begin to suspect that there is some causal connexion between rain and this wind, so that, when the wind blows, we may expect rain, at least with more confidence than when other winds blow; and, if the proportion in which rain accompanies this wind be much greater than that in which it accompanies other winds, our expectation is proportionably strengthened, and we have no hesitation in speaking of the quarter from which the wind blows as 'the rainy quarter.' In this case, the cause is, of course, to be sought in the character of the tract over which the wind blows. Similarly, if, after sufficiently long observation, we find the death-rate in some particular place decidedly larger than in the surrounding neighbourhood, we have no hesitation in ascribing the fact to some peculiarity either in the place or the population, and we at once begin to consider whether there is anything exceptional in the soil, the climate, the habits or occupations of the people, and the like, which, either alone or in conjunction with other circumstances, would account for the phenomenon.

In all cases of this kind, we are, as it were, set on the track of a cause by discovering that some phenomenon is

present in a proportionably greater number of instances when some other phenomenon is present than when it is absent. The cause itself may hereafter be detected either by one of the other inductive methods, or by bringing the case under a previous deduction. Thus, we know that the surface of that part of the moon which we call 'full' is highly heated, and that it is the tendency of warmth radiated from a highly-heated surface to clear the atmosphere. Hence the series of observed phenomena is, in this case, accounted for by being brought deductively under previous inductions.

METHOD OF RESIDUES.

CANON.

Subtract from any phenomenon such part as is known to be the effect of certain antecedents, and the residue of the phenomenon is the effect of the remaining antecedents.

If the antecedents are A, B, C, D, and the complex phenomenon can be resolved into the consequents a, β , γ , δ , ϵ , of which γ , δ , ϵ are ascertained by previous inductions or deductions to be due to C, D, then the remaining consequents a, β must be referred to the remaining antecedents A, B. Given that the total result is due to a certain number of antecedents, and that part of the result is due to a portion of those antecedents; the residue of the result must necessarily be due to the remaining antecedents. This rule appears so obvious as to be hardly worth stating; it has, however, as will be seen

from the examples given below, been mainly instrumental in leading to many of the most important discoveries of modern times. 'It is by this process, in fact,' says Sir John Herschel³¹, 'that science, in its present advanced state, is chiefly promoted. Most of the phenomena which nature presents are very complicated; and when the effects of all known causes are estimated with exactness, and subducted, the residual facts are constantly appearing in the form of phenomena altogether new, and leading to the most important conclusions.'

There is one difficulty connected with this Method. Subtraction being a deductive process, why is the Method of Residues included among the inductive methods? The Method, it must be confessed, is rather of a deductive than an inductive character, but as, in assigning the residual consequent to the residual antecedent, we assume the Law of Universal Causation, and as, moreover, the method is generally applied to the result of previous inductions and generally suggests subsequent inductions, it may vindicate its claim to discussion in this place. by induction that we usually ascertain that y, d, e are due to C, D; by the Method of Residues we determine that the remaining consequents a, & must be due to the remaining antecedents A, B; we then generally proceed to decide by one of the other inductive methods which of the remaining consequents is due to which of the remaining antecedents.

The following are instances of the employment of the

n Discourse on the Study of Natural Philosophy, § 158.

Method of Residues, and it will be noticed that the science of astronomy is peculiarly rich in such examples 32:—

'The planet Jupiter is attended by four satellites which revolve round it in orbits very nearly circular, and whose dimensions, forms, and situations with respect to that of the planet itself are now perfectly well known. The periodical times of their respective revolutions are also ascertained with extreme precision, and all the particulars of their motions have been investigated with extraordinary care and perseverance. The three interior of them are so near the planet, and the planes of their orbits so little inclined to that in which it revolves round the sun, that they pass through its shadow, and therefore undergo eclipse, at every revolution. These eclipses have been assiduously observed ever since the discovery of the satellites, and their times of occurrence registered. As they afford a means of determining the longitudes of places, the prediction beforehand of the exact times of their occurrence becomes an object of great importance; and it is evident enough that, all the particulars of their motions being known (as well as of that of the planet itself, and therefore of the size and situation of its shadow), there would be no difficulty in making such prediction (starting from the time of some one observed eclipse of each as an epoch); provided always each eclipse were seen at the identical moment when it actually happened. Moreover, on that supposition, the times recorded of all the subsequent

In the first and second editions the acceleration (or diminution of the periodic times) of Encke's comet (see Herschel's *Discourse on the Study of Natural Philosophy*, § 159) was given as an example of residual phenomena. The cause of this phenomenon is, however, so doubtful, that I have thought it best to omit the instance in the later editions.

eclipses ought to agree with the times so predicted. This however, proved not to be the case. The observed times were cometimes earlier, sometimes later than the predicted; not, however, capriciously, but according to a regular law of increase and decrease in the amount of discordance, the difference either way increasing to a maximum,—then diminishing, vanishing, and passing over to a maximum the others. /ay, and the total amount of fluctuation to and fro being about 16th 27°. Soon after this discrepancy between the predicted and observed times of eclipse was noticed, it was suggested that such a disagreement would necessarily arise 'the transmission of light were not instantaneous. This suggestion was converted into a certainty by Roemer, a Danisa astronomer, who ascertained that they always happenel earlier than their calculated time when the earth in the verse of its annual revolution approached nearest to Jupiter, and later when receding farthest: so that in effect the extreme difference of the errors or total extent of fluctuation the 16m 27s in question—is no other than the time takentby light to travel over the diameter of the earth's orbit, that being the extreme difference of the distances of the two planets at different points of their respective revolutions. At present, in our almanacs a due allowance of time for the transmission of light at this rate, assuming a uniform velocity, is made in the calculation of these eclipses; and the discrepancy in question between the observed and predicted times has ceased to exist 88.7

The circumstances which led to the discovery of the planet Neptune furnish, perhaps, the most striking instance of the employment of the Method of Residues. From the year 1804 it had been noticed that the orbit of the planet Uranus was subject to an amount of per-

Herschel's Familiar Lectures on Scientific Subjects, p. 226, &c.

turbation which could not be accounted for from the influence of the known planets.

Of the various hypotheses formed to account for ' (the perturbation), during the progress of its development, none seemed to have any degree of rational probability but that of the existence of an exterior, and hitherto undiscovered, planet, disturbing, according to the received laws of p etary disturbance, the motion of Uranus by its attraction, or rather superposing its disturbance on those produced by Jupi er and Saturn, the only two of the old planets which exercise any sensible disturbing action on that planet. Accordingsy, this was the explanation which naturally, and almost of necessity, suggested itself to those conversant with the planeta y perturbations who considered the subject with any de, ee of The idea, however, of setting out from the observed anomalous deviations, and employing them as data to ascertain the distance and situation of the unknown body, or, in other words, to resolve the inverse problem of perturbations, " given the disturbances to find the orbit and 'lace in that orbit of the disturbing planet," appears to have occurred only to two mathematicians, Mr. Adams in England and M. Leverrier in France, with sufficient distinctness and hopefulness of success to induce them to attempt its solution. Both succeeded, and their solutions, arrived at with perfect independence, and by each in entire ignorance of the other's attempt, were found to agree in a surprising manner when the nature and difficulty of the problem is considered; the calculations of M. Leverrier assigning for the heliocentric longitude of the disturbing planet for the 23rd Sept. 1846, 326° o', and those of Mr. Adams (brought to the same date) 329° 19', differing only 3° 19'; the plane of its orbit deviating very slightly, if at all, from that of the ecliptic.

'On the day above mentioned—a day for ever memorable in the annals of astronomy—Dr. Galle, one of the astronomers

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of the Royal Observatory at Berlin, received a letter from M. Leverrier, announcing to him the result he had arrived at, and requesting him to look for the disturbing planet in or near the place assigned by his calculation. He did so, and on that very night actually found it. A star of the eighth magnitude was seen by him and by M. Encke in a situation where no star was marked as existing in Dr. Bremiker's chart, then recently published by the Berlin Academy. The next night it was found to have moved from its place, and was therefore assuredly a planet. Subsequent observations and calculations have fully demonstrated this planet, to which the name of Neptune has been assigned, to be really that body to whose disturbing attraction, according to the Newtonian law of gravity, the observed anomalies in the motion of Uranus were owing²⁴.'

Besides furnishing an instance of the method of Residues, the above example is also a happy illustration of the combination of deduction with observation which has been so eminently fertile in astronomical research.

'Almost all the greatest discoveries in astronomy have resulted from the consideration of what we have elsewhere termed RESIDUAL PHENOMENA, of a quantitative or numerical kind, that is to say, of such portions of the numerical or quantitative results of observation as remain outstanding and unaccounted for after subducting and allowing for all that would result from the strict application of known principles. It was thus that the grand discovery of the precession of the equinoxes resulted, as a residual phenomenon, from the imperfect explanation of the return of the seasons by the return of the sun to the same apparent place among the fixed stars. Thus, also, aberration and nutation resulted as residual phenomena from that portion of the changes of the apparent

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Herschel's Outlines of Astronomy, Fourth Edition, §§ 767, 768.

places of the fixed stars which are left unaccounted for by precession. And thus again the apparent proper motions of the stars are the observed residues of their apparent movements outstanding and unaccounted for by strict calculation of the effects of precession, nutation, and aberration. The nearest approach which human theories can make to perfection is to diminish this residue, this caput mortuum of observation, as it may be considered, as much as practicable, and, if possible, to reduce it to nothing, either by showing that something has been neglected in our estimation of known causes, or by reasoning upon it as a new fact, and on the principle of the inductive philosophy ascending from the effect to its cause or causes³⁵.

'Many of the new elements of chemistry have been detected in the investigation of residual phenomena. Thus, Arfwedson discovered lithia by perceiving an excess of weight in the sulphate produced from a small portion of what he considered as magnesia present in a mineral he had analysed. It is on this principle, too, that the small concentrated residues of great operations in the arts are almost sure to be the lurking places of new chemical ingredients: witness iodine, brome, selenium, and the new metals accompanying platina in the experiments of Wollaston and Tennant. It was a happy thought of Glauber to examine what everybody else threw away³⁶.'

'The unforeseen effects of changes in legislation, or of improvements in the useful arts, may often be discerned by the Method of Residues. In comparing statistical accounts, for example, or other registers of facts, for a series of years, we perceive at a certain period an altered state of circumstances, which is unexplained by the ordinary course of events, but which must have some cause. For this residuary

³⁵ Herschel's Outlines of Astronomy, § 856.

²⁶ Herschel's Discourse on the Study of Natural Philosophy, § 161.

phenomenon, we seek an explanation until it is furnished by the incidental operation of some collateral cause. ample, on comparing the accounts of live cattle and sheep annually sold in Smithfield market for some years past, it appears that there is a large increase in cattle, while the sheep are nearly stationary. The consumption of meat in London may be presumed to have increased, at least in proportion to the increase of its population; and there is no reason for supposing that the consumption of beef has increased faster There is, therefore, a residuary phenothan that of mutton. menon-viz. the stationary numbers of the sheep sold in Smithfield—for which we have to find a cause. is the increased transport of dead meat to the metropolis, owing to steam navigation and railways, and the greater convenience of sending mutton than beef in a slaughtered state.

'Again: on comparing the consumption of wine with that of spirits and beer in England during the last sixty years³⁷, we find that the former has remained stationary, while the latter has undergone a great increase. The general causes, such as increase of population and wealth, which have increased the consumption of spirits and beer, have not increased the consumption of wine. For this residuary phenomenon, a special cause must be sought; and it may be found principally in the alteration of habits among the upper classes with respect to drinking³⁴.'

This passage was written in 1852. Since that time, owing to the reduction of the duties, the greater familiarity of Englishmen with foreign countries and habits, and, perhaps, the taste for a more refined style of living, the consumption of wine has enormously increased (First Edition, 1870). On the other hand, owing to the apread of Temperance Societies, and of more temperate habits in all classes of the population, the consumption of all alcoholic drinks has now, for some years, been steadily diminishing.

³⁸ Sir George Cornewall Lewis on the Methods of Observation and Reasoning in Politics, vol. i. p. 356.

I shall conclude my instances with what Sir John Herschel truly calls 'a very elegant example,' the difference between the observed and calculated velocities of sound. I quote from Professor Tyndall's Lectures on Sound:—

'I now come to one of the most delicate points in the whole theory of sound. The velocity through air has been determined by direct experiment; but knowing the elasticity and density of the air, it is possible without any experiment at all to calculate the velocity with which a sound-wave is transmitted through it. Sir Isaac Newton made this calculation, and found the velocity at the freezing temperature to be 916 feet a second. This is about one-sixth less than actual observation had proved the velocity to be, and the most curious suppositions were made to account for the discrepancy. Newton himself threw out the conjecture that it was only in passing from particle to particle of the air that sound required time for its transmission; that it moved instantaneously through the particles themselves. He then supposed the line along which sound passes to be occupied by air-particles for one-sixth of its extent, and thus he sought to make good the missing velocity. The very art and ingenuity of this assumption were sufficient to ensure its rejection; other theories were therefore advanced, but the great French mathematician Laplace was the first to completely solve the enigma. I shall now endeavour to make you thoroughly acquainted with his solution.

'I hold in my hand a strong cylinder of glass, accurately bored, and quite smooth within. Into this cylinder, which is closed at the bottom, fits this air-tight piston. By pushing the piston down, I condense the air beneath it; and, when I do so, heat is developed. Attaching a scrap of amadou to the bottom of the piston, I can ignite it by the heat generated by

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compression. Dipping a bit of cotton wool into bisulphide of carbon, and attaching it to the piston, when the latter is forced down, a flash of light, due to the ignition of the bisulphide of carbon vapour, is observed within the tube. It is thus proved that, when air is compressed, heat is generated. By another experiment, I can show you that, when air is rarefied, cold is developed. This brass box contains a quantity of condensed air. I open the cock, and permit the air to discharge itself against a suitable thermometer; the sinking of the instrument declares the chilling of the air.

'All that you have heard regarding the transmission of a sonorous pulse through air, is, I trust, still fresh in your minds. As the pulse advances, it squeezes the particles of air together, and two results follow from this compression of the air. Firstly, its elasticity is augmented through the mere augmentation of its density. Secondly, its elasticity is augmented by the heat developed by compression. It was the change of elasticity which resulted from a change of density that Newton took into account, and he entirely overlooked the augmentation of elasticity due to the second cause above mentioned. Over and above, then, the elasticity involved in Newton's calculation, we have an additional elasticity due to changes of temperature produced by the sound itself. When both are taken into account, the calculated and the observed velocity agree perfectly **.'

It is not necessary, for our purposes, to pursue the quotation, but the student, who wishes to see an example of the extreme delicacy and caution with which it is requisite to conduct physical researches, may with great advantage read the remainder of the chapter.

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³⁰ Lectures on Sound, ch. i.

METHOD OF CONCOMITANT VARIATIONS.

CANON.

Whatever phenomenon varies in any manner whenever another phenomenon varies in some particular manner, is either a cause or an effect of that phenomenon, or is connected with it through some fact of causation.

This Method is really a peculiar application, or series of applications, of the Method of Difference. It is employed in those cases where a phenomenon cannot be made to disappear altogether, but where we have the power of augmenting or diminishing its quantity, or at least where Nature presents it in greater or smaller amounts. Thus, suppose we drop a quantity of quicksilver into a glass tube, we shall find that every sensible \ augmentation of the temperature of the surrounding atmosphere is accompanied by a sensible augmentation of the volume of the quicksilver in the tube, and, vice versá, that every sensible diminution of the temperature is accompanied by a sensible diminution of the volume of the quicksilver. Now each particular experiment is an application of the Method of Difference, and, providing we have ascertained that the conditions of that Method have been rigorously satisfied, partakes of its cogency. That certain definite augmentations of temperature will increase the volume of quicksilver by, say, one-twentieth, one-thirtieth, or one-fiftieth part, is an

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[&]quot; On p. 186 will be found a rider to this Canon.

absolutely certain inference, supposing due care to have been taken in the performance of the experiments, and is simply a result of the Method of Difference. But, inasmuch as there are limits above and below which we cannot try the experiment, or intermediate points of temperature at which we do not find it convenient to do so, the question arises whether we are justified, in virtue of the experiments already tried, in asserting that the volume of the quicksilver will invariably expand or contract in proportion to the increasing or diminishing temperature of the surrounding media. We are justified in making such an assertion, and for this reason. The cause which occasions the quicksilver to expand or contract at two definite points must, if it continue to act, and if it be counteracted by no other cause, operate at all intermediate points; and, similarly, the cause which occasions it to expand or contract up to a certain point must, on the same suppositions, go on producing a like effect. This fact is implied in the very notion of Causation. We arrive, then, at the conclusion that the volume of the quicksilver is invariably dependent on the temperature of the surrounding medium; in other words, that augmentation of temperature is the cause of its expansion 41.

It may be asked, Why not employ the Method of

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⁴¹ The student acquainted with the phraseology of Mathematics will understand my meaning, when I say that the Method of Concomitant Variations is really an integration of a (supposed) infinite number of applications of the Method of Difference.

Difference once and for all? Because, ex hypothesi, the phenomenon is one which is only capable of augmentation or diminution, and cannot be made to vanish. We may reduce to a minimum the resistance to motion, but we cannot remove the resistance altogether. We may more and more diminish the heat of a body, but we cannot wholly deprive the body of its heat. Hence we can apply the Method of Difference to the several augmentations and diminutions of the phenomenon, but we cannot apply it to the phenomenon as a whole.

In the example given above, we know that augmentation of temperature and augmentation of volume are related as cause and effect, because, in the experiments, we can assure ourselves that they are the only two circumstances which vary in common; if we were not certain of this fact, there might be some third circumstance which was the cause of both. Moreover, we know that augmentation of temperature is the cause and augmentation of volume the effect, because, in this case, the former is the antecedent and the latter the consequent. There is another class of cases where, though we are not able to determine which of two circumstances is cause and which is effect, we may regard the relation as being one of cause and effect, inasmuch as we feel confident that there is present no third circumstance varying proportionately with the other two. But, if we cannot be confident even of this fact, the two circumstances may, for aught we know, both be effects of the same cause; as, for instance, the loudness of a clap of thunder varies

with the intensity of a flash of lightning, though neither is the cause of the other, both alike being effects of the electrical condition of the atmosphere. Hence will be seen the importance of the concluding words of the Canon, 'or is connected with it through some fact of causation.' The first and second cases differ from the third in this, that in both of them we suppose a rigorous fulfilment of the requisitions of the Method of Difference as applied to those individual observations or experiments on which the Method of Concomitant Variations is founded, and which it, as it were, sums up. In the last case, however, we suppose that there is some uncertainty as to whether the requisitions of the Method of Difference have been rigorously fulfilled or not. It will thus be seen that the statement of the Canon, as given above, is adapted to the weakest case. I may add to it the following rider:--

If we can assure ourselves that there is no third phenomenon varying concurrently with these two, we may affirm that the one phenomenon is either the cause or the effect of the other.

The Method of Concomitant Variations may be used for two purposes, either to establish a causal connexion, or to determine the law according to which two phenomena vary. Thus, it may either establish the fact that any increase of temperature causes quicksilver to expand, or it may determine the exact rate according to which this expansion takes place, a determination which is, in fact, effected by the ordinary thermometer. In the latter

case, the application of the Method is not confined to those permanent natural agents referred to above, the influence of which we cannot altogether remove; it may come in as supplementary to the Method of Difference. Thus it is by the Method of Difference that we discover that certain kinds of impurity in the atmosphere produce certain kinds of disease, but, if we could ascertain the relation subsisting between the amount of impurity in the atmosphere and the amount of disease, it would be by an application of the Method of Concomitant Variations.

In the latter class of enquiries, the attempt to determine the numerical relations according to which two phenomena vary, the utmost caution is required as soon as our inference outsteps the limits of our observations. In the first place, there is always the possibility of the intervention of some counteracting cause. In the case of water, we found that, at 39°, instead of continuing to contract as it becomes colder, it ceases at that point to do so, and thenceforward begins to expand. 'No counteracting cause intervening' is, however, a qualification with which we must understand all our inductions, by whatever method they may have been arrived at. But there is an element of uncertainty which is peculiar to the Method of Concomitant Variations as applied to determine the law or rate of variation between two phenomena, especially when the range of our observations is confined within comparatively narrow limits. 'Any one,' says Mr. Mill 42, 'who has the slightest acquaint-

[&]quot; Mill's Logic, Bk. III. ch. viii. § 7.

ance with mathematics, is aware that very different laws of variation may produce numerical results which differ but slightly from one another within narrow limits; and it is often only when the absolute amounts of variation are considerable, that the difference between the results given by one law and by another becomes appreciable. When, therefore, such variations in the quantity of the antecedents as we have the means of observing are small in comparison with the total quantities, there is much danger lest we should mistake the numerical law, and be led to miscalculate the variations which would take place beyond the limits; a miscalculation which would vitiate any conclusion respecting the dependence of the effect upon the cause, that could be founded on those variations. Examples are not wanting of such mistakes. "The formulæ," says Sir John Herschel, "which have been empirically deduced for the elasticity of steam (till very recently), and those for the resistance of fluids, and other similar subjects," when relied on beyond the limits of the observations from which they were deduced, "have almost invariably failed to support the theoretical structures which have been erected on them."" however, it must be noticed, is an uncertainty which does not vitiate the method, but simply renders necessary the exercise of the utmost caution in its application.

Perhaps no simpler instance of the Method of Concomitant Variations can be given than the experimental proof of the First Law of Motion, which Law may be stated thus: that all bodies in motion continue to move in a straight line with uniform velocity until acted upon by some new force.

'This assertion,' I am quoting from Mr. Mill43, ' is in open opposition to first appearances; all terrestrial objects, when in motion, gradually abate their velocity and at last stop; which accordingly the ancients, with their inductio per enumerationem simplicem, imagined to be the law. Every moving body, however, encounters various obstacles, as friction, the resistance of the atmosphere, &c., which we know by daily experience to be causes capable of destroying motion. It was suggested that the whole of the retardation might be owing to these causes. How was this enquired into? If the obstacles could have been entirely removed, the case would have been amenable to the Method of Difference. They could not be removed, they could only be diminished, and the case, therefore, admitted only of the Method of Concomitant Variations. This accordingly being employed, it was found that every diminution of the obstacles diminished the retardation of the motion: and, inasmuch as in this case (unlike the case of heat) the total quantities both of the antecedent and of the consequent were known, it was practicable to estimate, with an approach to accuracy, both the amount of the retardation and the amount of the retarding causes or resistances, and to judge how near they both were to being exhausted; and it appeared that the effect dwindled as rapidly [as the cause], and at each step was as far on the road towards annihilation as the cause was. The simple oscillation of a weight suspended from a fixed point, and moved a little out of the perpendicular, which in ordinary circumstances lasts but a few minutes, was prolonged in Borda's experiments to more than thirty hours, by diminishing as much as possible the friction at the point of suspension, and by making the body oscillate in a space exhausted as

⁴⁸ Mill's Logic, Bk. III. ch. viti. § 7.

nearly as possible of its air. There could therefore be no hesitation in assigning the whole of the retardation of motion to the influence of the obstacles: and since, after subducting this retardation from the total phenomenon, the remainder was an uniform velocity, the result was the proposition known as the first law of motion.'

I have already employed as an illustration the fact that a change in the temperature of a body is always accompanied by a change in its volume. The following extract places the same fact in a new light, and shows that the nature of substance (whether solid, liquid, or aëriform) depends on, and, at considerable intervals, varies with, the temperature to which it is exposed.

'The most striking and important of the effects of heat consist, however, in the liquefaction of solid substances, and the conversion of the liquids so produced into vapour. There is no solid substance known which, by a sufficiently intense heat, may not be melted, and finally dissipated in vapour; and this analogy is so extensive and cogent, that we cannot but suppose that all those bodies, which are liquid under ordinary circumstances, owe their liquidity to heat, and would freeze or become solid if their heat could be sufficiently reduced. In many we see this to be the case in ordinary winters; for some, severe frosts are requisite; others freeze only with the most intense artificial colds; and some have hitherto resisted all our endeavours; yet the number of these last is few, and they will probably cease to be exceptions as our means of producing cold become enlarged.

'A similar analogy leads us to conclude that all aeriform fluids are merely liquids kept in the state of vapour by heat. Many of them have been actually condensed into the liquid state by cold accompanied with violent pressure; and, as our means of applying these causes of condensation have improved, more and more refractory ones have successively yielded. Hence we are fairly entitled to extend our conclusion to those which we have not yet been able to succeed with; and thus we are led to regard it as a general fact, that the liquid and aëriform or vaporous states are entirely dependent on heat; that, were it not for this cause, there would be nothing but solids in nature; and that, on the other hand, nothing but a sufficient intensity of heat is requisite to destroy the cohesion of every substance, and reduce all bodies, first to liquids, and then into vapour.

An interesting application of the Method of Concomitant Variations is found in the arguments by which it is established that refrigeration at night (when the sun's rays are withdrawn) is, cateris paribus, proportional to the dryness of the atmosphere. Thus, in the British Isles, where the atmosphere almost always contains a large amount of aqueous vapour, the difference between

* Herschel's Discourse on the Study of Natural Philosophy, §§ 357, 358.

Sir John Herschel's conjecture has been verified with regard to aeriform fluids, but not as yet with regard to liquids. The experiments of Cailletet and Pictet (an account of which may be found in the Academy of Jan. 12th, 1878, and in Nature of Jan. 3rd and 17th of the same year) have conclusively shown that even oxygen, hydrogen, and nitrogen admit of liquefaction, and, therefore, probably of solidification. A brief account of these experiments is given in Ganot's Physics, Translation, 12th ed. § 382. Thus, the old distinction between permanent and non-permanent gases has been entirely effaced. By a legitimate analogy, it may be inferred, with a very high degree of probability, that all liquids admit of solidification. But some liquids, such as alcohol, ether, and bisulphide of carbon, have hitherto resisted all attempts to solidify them, even at the lowest known temperature. See Ganot, § 343.

the temperature at day and night is comparatively slight, whereas, in countries far inland, where the atmosphere is extremely dry, the variations of temperature are comparatively large. This phenomenon is due to the fact that masses of aqueous vapour, though they intercept, also radiate heat. Hence, while during the day they protect us from the excessive heat of the sun, they intercept the heat which is radiated from the earth's surface during the night, and, at the same time, return to it some portion of the heat they have absorbed during the day.

'A freedom of escape,' says Professor Tyndall⁴⁵, 'would occur at the earth's surface generally, were the aqueous vapour removed from the air above it, for the great body of the atmosphere is a practical vacuum, as regards the transmission of radiant heat. The withdrawal of the sun from any region over which the atmosphere is dry, must be followed by quick refrigeration. The moon would be rendered entirely uninhabitable by beings like ourselves through the operation of this single cause; with a radiation, uninterrupted by aqueous vapour, the difference between her monthly maxima and minima must be enormous. The winters of Thibet are almost unendurable, from the same cause. Witness how the isothermal lines dip from the north into Asia, in winter, as a proof of the low temperature of this region. Humboldt has dwelt upon the "frigorific power" of the central portions of this continent, and controverted the idea that it was to be explained by reference to the elevation; there being vast expanses of country, not much above the sea-level, with an exceedingly low temperature. But, not knowing the influence which we are now studying, Humboldt, I imagine, omitted the most potent cause of the cold. The

⁴⁰ Tyndall's Heat a Mode of Motion, § 492.

refrigeration at night is extreme when the air is dry. The removal, for a single summer night, of the aqueous vapour from the atmosphere which covers England, would be attended by the destruction of every plant which a freezing temperature could kill. In Sahara, where "the soil is fire and the wind is flame," the cold at night is often painful to bear. Ice has been formed in this region at night. In Australia, also, the diurnal range of temperature is very great, amounting, commonly, to between 40 and 50 degrees. In short, it may be safely predicted that, wherever the air is dry, the daily thermometric range will be great. This, however, is quite different from saying that, where the air is clear, the thermometric range will be great. Great clearness to light is perfectly compatible with great opacity to heat; the atmosphere may be charged with aqueous vapour while a deep blue sky is overhead, and on such occasions the terrestrial radiation would, notwithstanding the "cleamess," be intercepted.'

The science of Geology abounds in instances of the employment of the Method of Concomitant Variations. In fact, as the agents with which it is concerned, land and water, subsidence and elevation, deposition and denudation, are constantly present and acting on the earth's surface, and as it is impossible to cause the influence of any one of them to vanish altogether, the geologist is compelled in his explanations and arguments to avail himself mainly of this method. The following extract from Lyell's *Principles of Geology* furnishes a good illustration, and will be peculiarly interesting to any one who has visited the place. It is designed as an explanation of the alternate subsidence and elevation of

the famous temple of Jupiter Serapis, at Pozzuoli, on the Bay of Naples.

'We can scarcely avoid the conclusion, as Mr. Babbage has hinted, "that the action of heat is in some way or other the cause of the phenomena of the change of level of the temple. Its own hot spring, its immediate contiguity to the Solfatara, its nearness to the Monte Nuovo, the hot spring at the baths of Nero on the opposite side of the Bay of Baiæ, the boiling springs and ancient volcanos of Ischia on one side and Vesuvius on the other, are the most prominent of a multitude of facts which point to that conclusion." And when we reflect on the dates of the principal oscillations of level, and the volcanic history of the country before described, we seem to discover a connexion between each era of upheaval and a local development of volcanic heat, and again between each era of depression and the local quiescence or dormant condition of the subterranean igneous causes. Thus for example, before the Christian era, when so many vents were in frequent eruption in Ischia, and when Avernus and other points in the Phlegræan Fields were celebrated for their volcanic aspect and character, the ground on which the temple stood was several feet above water. Vesuvius was then regarded as a spent volcano; but when, after the Christian era, the fires of that mountain were rekindled, scarcely a single outburst was ever witnessed in Ischia, or around the Bay of Baiæ. Then the temple was sinking. Vesuvius, at a subsequent period, became nearly dormant for five centuries preceding the great outbreak of 1631, and in that interval the Solfatara was in eruption A.D. 1198, Ischia in 1302, and Monte Nuovo was formed in 1538. Then the foundations on which the temple stood were rising again. Lastly, Vesuvius once more became a most active vent, and has been so ever since, and during the same lapse of time the area of the temple, so far as we know anything of its history, has been subsiding.

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'These phenomena would agree well with the hypothesis, that when the subterranean heat is on the increase, and when lava is forming without obtaining an easy vent, like that afforded by a great habitual chimney, such as Vesuvius, the incumbent surface is uplifted, but when the heated rocks below are cooling and contracting, and sheets of lava are slowly consolidating and diminishing in volume, then the incumbent land subsides.'

Laplace's Nebular Hypothesis, that stellar systems, like our solar system, are formed from the gradual condensation of nebular masses, is supported by an appeal to this method. 'We see,' conceives Laplace, 'among these nebulæ' (which are diffused along the Milky Way), 'instances of all degrees of condensation, from the most loosely diffused fluid, to that separation and solidification of parts by which suns and satellites and planets are formed: and thus we have before us instances of systems in all their stages; as in a forest we see trees in every period of growth 47.'

Physiology (so far as it is based on Anatomy, as distinct from direct experiment), for like reasons with Geology, mainly employs the Method of Concomitant Variations. It is very seldom, in this science, that we obtain a phenomenon present in one set of instances

⁴⁶ Lyell's Principles of Geology, tenth edition, ch. xxx.

Whewell's Novum Organon Renovatum, Bk. III. ch. viii. sect. 2. § 9. This example is adduced by Dr. Whewell as an instance of what he calls the Method of Gradation, which, however, must not be confounded with Mill's Method of Concomitant Variations. The example, so far as it can be relied on, serves equally well as an instance of either method.

and entirely absent in another; but we frequently find a phenomenon which, within certain limits, presents itself in the most variable quantities. If, then, we find another phenomenon varying as it varies, we may argue with tolerable confidence that the two phenomena either stand to each other in the relation of cause and effect, or are, at least, common effects of some unknown cause. Thus, it appears to be established that, not only in different species, but in different individuals of the same species, there is some relation between the manifestations of intelligence and the amount of cerebral development, understanding the latter expression to include not only bulk of brain but also complexity and depth of convolutions.

'With some apparent exceptions,' says Dr. Carpenter⁴⁸, a classical authority on most physiological questions, 'which there would probably be no great difficulty in explaining if we were in possession of all the requisite data, there is a very close correspondence between the relative development of the Cerebrum in the several tribes of Vertebrata and the degree of Intelligence they respectively possess—using the latter term as a comprehensive expression for that series of mental actions which consists in the *intentional* adaptation of means to ends, based on definite *ideas* as to the nature of both.'

And again :--

As we ascend the Mammalian series, we find the Cerebrum becoming more and more elongated posteriorly by the development of the middle lobes, and the intercerebral conmissure becomes more complete; but we must ascend as

[&]quot; Carpenter's Principles of Human Physiology, sixth edition, 1864.

high as the Carnivora, before we find the least vestige of the posterior lobes; and the rudiment which these possess is so rapidly enlarged in the Quadrumana, that in some of that group the posterior lobes are as fully developed in reference to the Cerebrum as a whole, and as completely cover in the Cerebellum, as in the human subject. The attention which has yet been given to this department of enquiry, has not hitherto done more than confirm the statement already made, with regard to the general correspondence between the development of the Cerebrum and the manifestations of Intelligence; very decided evidence of which is furnished by the great enlargement of the Cerebrum, and the corresponding alteration in the form of the Cranium, which present themselves in those races of Dogs most distinguished for their educability, when compared with those whose condition approximates most closely to what was probably their original state of wildness.

'This general inference, drawn from Comparative Anatomy, is borne out by observation of the human species. When the Cerebrum is fully developed, it offers innumerable diversities of form and size among various individuals; and there are as many diversities of character. It may be doubted if two individuals were ever exactly alike in this respect. That a Cerebrum which is greatly under the average size is incapable of performing its proper functions, and that the possessor of it must necessarily be more or less idiotic, there can be no reasonable doubt. On the other hand, that a large, well-developed Cerebrum is found to exist in persons who have made themselves conspicuous in the world in virtue of their intellectual achievements, may be stated as a proposition of equal generality.'

Dr. Thurnam 46, taking the brain-weights of ten dis-

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On the Weight of the Brain, by John Thurnam, M.D. London, J E. Adlard. 1866.

tinguished men, who died between the ages of fifty and seventy, calculates the average weight of their brains to have been 54'7 ounces. The average weight of the brains of ordinary men, dying between the same ages, is 47'1 ounces. These facts give in favour of 'cultivated and intellectual man' an excess of 7.6 ounces, or 15 per cent. Though, as a general rule, the connexion between intellectual and cerebral development appears to be substantiated, we must, however, be very cautious in drawing any inferences as to particular cases. Megalocephaly, or pathological enlargement of the brain, is a recognised disease, and is frequently attended with idiotcy. class of cases, no doubt, if our means of investigation were adequate, we should discover some peculiarity either in the chemical composition or in the anatomical structure of the brain which would enable us to explain the exceptions in conformity with the rule.

It is, perhaps, needless to add that we are not justified in drawing any further inference from these data, than that the brain is the *organ* of intelligence, and that there is some definite relation between the organ and its functions.

Another interesting application of the Method of Concomitant Variations may be found in one of the arguments by which the distinction between Formed and Germinal Material is established. Any piece of glandular tissue, if examined under a microscope, will be found to consist of two parts, one of which will take a tint from carmine, the other not. The portion which takes

the tint is called Germinal, the portion which will not take it is called Formed Material. The former is living matter, capable of growth and germination; the latter is dead matter, capable of no change but decay. Now, if this distinction between the two kinds of matter be well founded, we may reasonably expect to find the germinal matter developed in much larger proportions in the younger than in the older specimens of animals and plants, and in what may be called the more active than in what may be called the more passive parts of animal and vegetable organisms. And this is the case. In the pith of rush, elder, &c. we find that, in the spring, there are many portions of the cells which will take the carmine tint; in summer, few; in autumn, none. In the crystalline lens of the eyes of young animals the portions which will take it preponderate, becoming proportionately fewer as we examine the eyes of older specimens. the grey matter of the brain we find many parts which will take the carmine tint, in the white matter but few. In a grain of wheat, when formed, there is, in the perisperm, no portion which will take it, in the white matter but a small portion, while in the embryo it is often difficult to discover any part which does not take it. These instances might be multiplied to any extent 60.

In physiological and medical researches, we must be peculiarly careful to bear in mind that, though two pheno-

The student will find this subject fully treated in Dr. Lionel Beale's Lectures on the Simple Tissue of the Human Body, and in other works of the same author.

mena may vary proportionately, it by no means follows that one is cause and the other effect. They may both be common effects of the same cause. Thus, though the prevalence of cholera is said to be constantly attended by the appearance of certain low forms of organic life, namely, fungi or phytozoa, it by no means follows that these fungi or phytozoa are the cause of cholera. Both phenomena alike may be effects of certain conditions of the atmosphere. Nothing but direct experiment can determine between these two theories.

The Method of Concomitant Variations is that which is most frequently employed in the Science of Language. It is found, for instance, that between two dissimilar words employed at different epochs to express the same idea may be interpolated a number of intermediate forms employed at intermediate epochs, which make the transition from the one word to the other gradual and natural. From this circumstance it is inferred that the word used at the later epoch is derived from that used at the earlier epoch, certain tendencies of speech being regarded as the cause of the divergence. 'Thus, at first sight,' says M. Brachet 51, 'it is hard to see that âme is derived from anima; but history, our guiding-line, shows us that in the thirteenth century the word was written anme, in the eleventh aneme, in the tenth anime, which leads us straight to the Latin anima.' In this case there can be no doubt of the truth of the conclusion.

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M. Brachet's Historical Grammar of the French Tongue, Dr. Kitchin's Translation, p. 42. Seventh Edition, p. 53.

Similarly, the loss of declension in the transition from the Latin Language to the French is easily explained when we take into account the following considerations:—

'The tendency to simplify and reduce the number of cases was early felt in the popular Latin: the cases expressed shades of thought too delicate and subtle for the coarse mind of the Barbarian. And so, being unable to handle the learned and complicated machinery of the Latin declensions, he constructed a system of his own, simplifying its springs, and reducing the number of the effects at the price of frequently reproducing the same form. Thus the Roman distinguished by means of case-terminations the place where one is, from the place to which one is going: "veniunt ad domum," "sunt in domo." But the Barbarian, unable to grasp these finer shades, saw no use in this distinction, and said, in either case alike, "sum in domum," "venio ad domum."

'Thus, from the fifth century downwards, long before the first written records of the French language, popular Latin reduced the number of cases to two: (1) the nominative to mark the subject; and (2) that case which occurred most frequently in conversation, the accusative, to mark the object or relation. From that time onwards the Latin declension was reduced to this:—subject, murus; object, murum.

'The French language is the product of the slow development of popular Latin; and French grammar, which was originally nothing but a continuation of the Latin grammar, inherited, and in fact possessed from its infancy, a completely regular declension: subject, murs, murus; object, mur, murum: and people said "ce murs est haut;" "j'ai construit un mur."

'This declension in two cases forms the exact difference between ancient and modern French. It disappeared in the fourteenth century, not without leaving many traces in the language, which look like so many insoluble exceptions, but find their explanation and historic justification in our knowledge of the Old French declension 52.

Here the conclusion is that French Grammar is derived from Latin Grammar, certain peculiarities of the period intervening between the use of the Latin and modern French languages being regarded as the cause of the differences between them.

Again, nothing at first sight would appear more improbable than that the French word suis and the Greek word sim are derived from the same root. But, when we compare the old French word sui, the Latin sum, the Old Latin esum, and the Old Greek form $\delta\sigma\mu$, the connexion of the two words and their ultimate derivation from a common root becomes a certainty. Here the divergence may be definitely accounted for by the various influences operating upon people (like the Latins and Greeks) occupying different tracts of country, exposed to different circumstances, having the organs of speech differently modified, and the like.

Amongst the above examples it will be noticed that some have been included, the conclusions of which are by no means absolutely certain. In these cases, the deficiency of proof is due not to any formal inconclusiveness in the Method of Concomitant Variations, or in that of Difference, on which it is based, but to the existence of a doubt as to whether the requirements of those

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⁵⁸ M. Brachet's Historical Grammar of the French Tongue, Dr. Kitchin's Translation, p. 88. Seventh Edition, pp. 98-100.

methods have been stringently fulfilled. In any but the Experimental Sciences it is always extremely difficult to assure ourselves that we are acquainted with all the circumstances which may influence, or may be influenced by, any given phenomenon. Moreover, as is the case, for instance, with regard to the concomitance between cerebral development and the manifestation of intelligence, there may be many known points of difference between the observed cases besides those which are taken into account, and the value of the conclusion will depend on the extent to which we have ascertained that these other points of difference are not pertinent, or not equally pertinent with those which we have taken into account, to the circumstance or circumstances which we are investigating.

The application of the Method of Concomitant Variations to determine the numerical relations subsisting between two phenomena may be illustrated from the experiments by which the measure of the accelerating force of gravity was established. The fact, that the higher the point from which a body falls, the greater is the velocity acquired, is patent to observation, though, if we analyse the process by which we arrive at the conclusion, it is by the Method of Concomitant Variations. The rate of acceleration, however, is a very difficult and delicate problem to solve. By means of the oscillating pendulum or Atwood's machine (which it is unnecessary to describe here) it is shown (1) that gravity is an uniformly accelerating force, that is, that the increments of velocity in equal times are equal; (2) that the rate of increase varies

slightly at different places on the earth's surface; (3) that, in the latitude of Greenwich, in vacuo, and at high-water mark, the rate of acceleration for every second of time is $32^{\circ}19$ inches, the space traversed in the first second of time, if the body fall from rest, being half that quantity, so that the spaces traversed in successive units of time vary as the odd numbers $1, 3, 5 \dots (2n-1)$. A slight degree of attention will show that it is by the Method of Concomitant Variations that all these conclusions are obtained ⁵⁵.

The conclusions based on statistics in moral and social enquiries are also instances of this application of the Method of Concomitant Variations. It is argued that, if the same causes continue to operate with like intensity and no new causes intervene, the numerical relations established between two classes of social phenomena, as, for instance, deficient education and crime, may be expected to remain constant.

A very important application of the Method of Concomitant Variations is what is now commonly known as the *Historical Method*. The Method designated by this name is, in fact, simply the Method of Concomitant Variations applied to facts supplied by history or to a record of observations on the same classes of facts as those with which history deals. It is specially applicable to those sciences which deal with man as a progressive

⁵³ The student who wishes for more detailed information on this subject is referred to Professor Price's *Infinitesimal Calculus*, vol. iii. chap. viii. sect. 3.

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being, or, at least, a being capable of progress. Thus, a certain institution, custom, or opinion is traced throughout various stages of society, and its growth or decline is connected with that of some other institution, custom, or opinion, or with the general state of civilisation prevalent throughout these periods, it being argued, in the 'latter case, that, as civilisation advances, the institution, custom, or opinion has grown or declined, as the case may be. This method has of late years been employed with great success in the domains of law, morals, religion, art, and language 64; and it is sufficient to refer the student for examples to works such as those of Sir Henry Maine, Sir John Lubbock, Professor Max Müller, and Dr. Tylor. The gradual process by which the organisation of the family passes into that of the state, or by which the primitive feeling of resentment is developed into that strict sense of justice which distinguishes civilised man would be amongst the many striking illustrations of this method which are afforded by writers on morals and society, both ancient and modern. When the method is combined with deductions from the science of Psychology, stating a priori what might be expected from a general knowledge of human nature, it is called by Mr. Mill the Inverse Deductive Method. Under this head I shall briefly advert to it again, in the chapter on the Relation of Induction to Deduction 16.

The instances given on pp. 200-202 are examples of the application of the Historical Method to the Science of Language.

There is one objection to the employment of the Historical Method, which at least demands an answer. The progress, say, of

The Method of Concomitant Variations, especially when applied to subjects other than physical, such as law, morals, language, social statistics, &c., is often called vaguely the *Comparative Method*.

morality, art, or some particular institution, is compared with the progress of general civilisation. But perhaps this very circumstance is amongst the most important considerations to be taken into account in estimating the stage of civilisation to which any people The scientific enquirer, therefore, who or class has attained. employs the Historical Method seems to be open to the objection that he is making one quality vary as an aggregate of qualities of which it is itself one; for, supposing the extreme case of the other qualities which make up the aggregate being all constant, we should then have the identical proposition that the quality or institution in question varies as itself. But, as a matter of fact, we know that the other qualities which make up the aggregate of circumstances which we call civilisation are far from being constant. Moreover, they are all so intertwined with one another that almost any one of them varies directly as almost any other. Amongst these various circumstances, however, we are able to detect one on which all the others seem to be specially dependent. This is, to state it in the most general terms, the intellectual condition prevalent at the given time, in the given place, or amongst the given class. Not only do we find, as a matter of fact, that the current intellectual beliefs and the degree of development of the intellectual faculties is the best index to the state of the other constituents which make up civilisation, but also we should expect a priori that these latter circumstances would be mainly determined by the former. For it is by the exercise of reason that man learns, in an infinite variety of ways, to adapt himself to the various circumstances which surround him, that he discovers the means of gratifying his higher tastes, and that he is enabled to enter into the feelings and understand the wants of others. On this relation between the state of the intellectual faculties and the aggregate of circumstances which constitute civilisation, the student may consult Mr. Mill's Logic, Bk. VI. ch. x. § 7.

The term 'Historical,' as designating this Method, is somewhat

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Briefly to review these Methods, it will be seen that we can only arrive at absolute certainty by means of one or other of the Methods of Difference, Residues, or Concomitant Variations, while the Method of Agreement and the Joint Method of Agreement and Difference give conclusions only of more or less probability, a probability, however, which sometimes amounts to moral certainty. The Joint Method of Agreement and Difference, or the Double Method of Agreement, possesses one advantage over all the other Methods, namely that, supposing it to have been satisfactorily ascertained by this Method that A is the cause of a, it will follow that it is the only cause.

It should also be borne in mind that a wide distinction exists between those cases in which the induction indicates the precise character of the causal connexion which subsists between two or more phenomena and those in which it simply points out that there exists a causal connexion of some kind or other. In the latter case a new induction is required in order to show what the nature of the causal connexion is.

It may be noticed, finally, that the Inductive Methods are strictly reducible to two only, the Method of Agreement and the Method of Difference; the Joint Method of Agreement and Difference being a double employment of the Method of Agreement, supplemented by an employmisleading, because, though the facts to which the Method is applied may be mainly supplied by history, they are also, to a large extent, taken from the contemporary observation of tribes and peoples living in different stages, or different phases, of civilisation with reference to the matters of enquiry.

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ment of the Method of Difference, the Method of Concomitant Variations being a series of employments of the Method of Difference, and the Method of Residues, though employed in an inductive enquiry, being rather of the nature of a deductive than an inductive method.

Note 1.- In the preceding chapter no allusion, or only a casual one, has been made to a circumstance which frequently occasions an insuperable difficulty in the application of the Inductive Methods, namely, the Intermixture of Effects. It has been supposed that the antecedents A, B, C, D, &c. are followed by the consequents a, β , γ , δ , ϵ , &c., the effects being regarded as heterogeneous and not homogeneous. But, suppose the effect of A to be a, of B to be $-\frac{a}{2}$, of C to be γ , of D to be $\frac{\gamma}{3}$, and of E to be $-\frac{\gamma}{2}$, the total effect of A, B, C, D, E will be $\frac{a}{2} + \frac{5\gamma}{6}$. It is obvious how difficult it would be in this case to discover either the exact portion of the effect which is due to each cause or the several causes which operate to produce the total effect. We might have, in fact, as in mechanical action and reaction, A producing a and B producing - a, each cause thus neutralising the effect of the other, so that we might entertain no suspicion that the causes A and B were in operation at all. In these cases, our main resource is Deduction. Having ascertained separately by

one or other of the various inductive methods, or from

previous deductions, the effects, say of A, B, C D, we

calculate deductively their combined effect, and then, by subtracting, according to the Method of Residues, the sum of the known causes from the total aggregate of causes and the known portion of the effect from the total effect, we simplify, if we do not solve, the problem. On the insufficiency, under ordinary circumstances, of the Inductive Methods, without the aid of Deduction, to grapple with cases of this kind⁵⁸, and on the nature of the assistance rendered by Deduction, the reader may consult Mr. Mill's Logic, Bk. III. ch. x. § 4-8, and ch. xi.

In cases of this kind, where the action of one cause is augmented, diminished, or wholly counteracted by that of another, it must not be supposed that any part of its appropriate effect has failed to be produced, even though it may have disappeared wholly or partially in the total

Since the appearance of the first edition of this work, it has been pointed out by Mr. Bain that 'Concomitant Variation is the only one of the [Inductive] Methods that can operate to advantage in such cases.' I take the liberty of transcribing the passage: 'If a cause happens to vary alone, the effect will also vary alone, and cause and effect may be thus singled out under the greatest complications. Thus, when the appetite for food increases with the cold, we have a strong evidence of connexion between those two facts, although other circumstances may operate in the same direction.

'The assigning of the respective parts of the sun and moon, in the action of the Tides, may be effected, to a certain degree of exactness, by the variation of the amount according to the positions of the two attracting bodies.

'By a series of experiments of Concomitant Variations, directed to ascertain the elimination of nitrogen in the human body under varieties of muscular exercise, Dr. Parkes obtained the remarkable conclusion, that a muscle grows during exercise and loses bulk during the subsequent rest.'—Bain's Logic, Bk. III. ch. viii. § 6.

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result. An object may remain at rest, when subject to two equal forces acting in opposite directions, but we cannot say of either of these forces that it is inoperative: each, it is true, prevents any visible effect resulting from the other; but then this is the very effect which it produces, and the correct mode of describing either of the opposing forces would be to say that it has a tendency to make the given object move with a certain velocity in a certain direction. The student cannot too constantly bear in mind that every cause invariably produces its full effect, though other causes may prevent that effect from manifesting itself with all the intensity with which it would manifest itself, if it acted alone; that there are, strictly speaking, no exceptions to laws of nature, though these laws, in their manifold action and reaction, may modify or even neutralise each other. The aphorism 'Every rule has an exception,' is only true, even in Grammar, either because the rule is inexactly stated or because it conflicts with some other rule known or unknown.

Note 2.—The Canons for the Inductive Methods were first stated by Mr. Mill, and the importance now attached to them in most analyses of inductive enquiries is mainly due to his influence. The methods are, however, as Mr. Mill himself states, 'distinctly recognised' in Sir John Herschel's Discourse on the Study of Natural Philosophy, so often quoted in this work, 'though not so clearly characterised and defined, nor their correlation so fully shown, as has appeared to me desirable.' In

the Second Book of Bacon's Novum Organum, we find some approximations, very rough, it is true, to formal inductive methods. The 'instantiæ crucis' have already been adduced as examples of the Method of Difference, and the 'instantiæ solitariæ' as comprising examples of both the Method of Agreement and the Method of Difference; but the part of the Novum Organum to which I am now alluding, and which is intended to be of more universal application than the 'instantiæ crucis' and the 'instantiæ solitariæ,' is contained in the early Aphorisms of the Second Book. Certain Tables of Instances are there given for the purpose of providing materials with which to conduct an investigation into what Bacon called the 'Form 57,' corresponding pretty nearly, at least in this connexion, with what we should call the 'Cause,' of Heat. The instances are very far from satisfying the conditions of Mr. Mill's Methods, but the principles on which they are arranged in Tables bear a close analogy to the principles on which the Canons are constructed. The best mode, perhaps, of enabling the student to perceive the extent of the resemblance is to state the conditions with which the instances in Bacon's Tables would be required to conform, in order to satisfy the requirements of Mr. Mill's Methods.

If the 'Instantiæ convenientes in natura calidi' 68 were

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⁵⁷ On the meaning attached by Bacon to the word 'Form,' and its relation to 'Essence' and 'Cause,' see the Introduction to my Edition of the *Novum Organum*, § 8.

⁵⁰ Novum Organum, Lib. II. Aph. xi.

so related to one another that, besides the given phenomenon (heat), only one other circumstance were common to them all, that other circumstance might be regarded, with more or less probability, as the cause (or effect) of heat, or, at least, as connected with it through some fact of causation. Such instances would then come under the Method of Agreement.

If one instance in the Table of Agreement ('Instantiæ convenientes in natura calidi') were so related to one of the instances in the Table of Privation ('Instantiæ in proximo, quæ privantur natura calidi') so as to have every circumstance in common with it, except that the former, besides presenting the phenomenon of heat which is supposed to be absent in the latter, also presented some other circumstance which was absent from the latter, this other circumstance would be the cause (or effect), or a necessary part of the cause, of heat. We should here have the Method of Difference.

If, in the 'Tabula graduum, sive comparative in calido 'o,' we could discover some one phenomenon which increased and diminished proportionately with the increase and diminution of heat, that phenomenon would be the cause or the effect of heat, or, at least, connected with it through some fact of causation, and the conditions would thus conform with the requirements of the Method of Concomitant Variations. If it could be shown that this phenomenon and heat were the only circumstances which varied concurrently, then the phenomenon would

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^{*} Novum Organum, Lib. II. Aph. xxii. * Id. Aph. xiii.

be proved to be either the cause or the effect of heat, and would conform with the requirements of the rider to this last Method (p. 186).

The 'Exemplum exclusivæ, sive rejectionis naturarum a forma calidi' 1 (which is based on the foregoing Tables) bears some, though, it must be acknowledged, a very slight, resemblance to the Method of Residues. These 'rejectiones' consist in excluding some possible explanation of the phenomenon, either because an instance, which does not present the phenomenon, does present the assigned cause, or because an instance, which does present the phenomenon, does not present the assigned cause 42 (and similarly with regard to increase and decrease). As an example of the former case, we may take the following 'rejectio': 'Per radios lunæ (which were then supposed to be cold) et aliarum stellarum rejice lucem et lumen.' As examples of the latter, we may take the two following: 'Per radios solis, rejice naturam elementarem (that is, 'terrestrial nature,' which is composed of 'the four elements'); Per ignem communem, et maxime per ignes subterraneos (qui remotissimi sunt, et plurimum intercluduntur a radiis cœlestibus) rejice naturam coelestem.' By a succession of these 'rejectiones,' we limit the number of possible explanations, amongst which we are to look for the true one. Bacon's 'rejec-

⁴ Novum Organum, Lib. II. Aph. xviii.

The latter, of course, is not a legitimate argument. The effect may be due to several distinct causes, a fact which was not recognised by Bacon. See my notes on *Novum Organum*, Lib. II. Aph. zvi.

tions,'however, not being, as a matter of fact, exhaustive, lead to a purely negative result; they may save us from unnecessary trouble in seeking for a cause where it cannot be found, but they do not, like the Method of Residues, leave a definite number of antecedents which either constitute the cause, or amongst which we know that the cause is to be sought.

It is plain that if there were a certain number only of possible causes of the given phenomenon, and by the method of rejections we could exclude all but one, this one remaining cause would be the undoubted cause of the given phenomenon. This case Bacon appears to have regarded as the perfect type of Induction, and as alone capable of affording certainty ⁶⁵.

Note 3.—Dr. Whewell (in a pamphlet published in 1849, which is now embodied in the Philosophy of Discovery ") questions the utility of the Four Methods.

It must be understood that, in this note, I am simply comparing the 'Tables' of Bacon with the 'Methods' of Mr. Mill. On the relation of the 'Tables' to each other and on the special importance attached by Bacon to the 'Rejections,' the student may consult § 9 of the Introduction to my edition of the Novum Organum (Clarendon Press) and my notes to the earlier aphorisms of the Second Book.

In comparing the logical procedure of Bacon and Mill, it should be carefully borne in mind that Bacon contemplated the concurrent use of all the Tables, as preparatory to his Method of Rejections, and regarded the construction of the Tables and the subsequent application to them of the Method of Rejections as constituting only one process. On the other hand, each of Mr. Mill's Methods may be worked independently, and lead to a final conclusion.

⁶⁴ See Philosophy of Discovery, ch. xxii. The criticism of Mr.

'Upon these methods,' he says, 'the obvious thing to remark is, that they take for granted the very thing which is most difficult to discover, the reduction of the phenomena to formulæ such as are here presented to us.' He also objects that, as a matter of fact, no discoveries have ever been made by the employment of these methods. 'Who will carry these formulæ through the history of the sciences, as they have really grown up, and show us that these four methods have been operative in their formation; or that any light is thrown upon the steps of their progress by reference to these formulæ?'

The first objection is, as Mr. Mill points out, of the same character with the objections raised by Locke and other writers of the eighteenth century against the Rules of Syllogistic Reasoning. The reply, in either case, is that Logic does not profess to supply arguments, but to test them. Men have certainly reasoned, and reasoned with the greatest success, without any conscious use of the rules of Logic. But it is the province of a system of Logic to analyse the arguments commonly employed, to discriminate between those which are correct and those which are incorrect, and thus to enable men to detect, in the case of others, and to avoid, in their own case, erroneous methods of reasoning. To think of appropriate arguments is undoubtedly more difficult than to test them; but this fact does not obviate the necessity of submitting them to a test. Nor is it a more real objec-

Mill's Methods will be found in §§ 38-48. Mr. Mill replies in a note at the end of Bk. III. ch. ix.

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tion that men, who know nothing of the technical rules of Logic, often reason faultlessly themselves, and show remarkable acuteness in detecting inconclusive reasoning in the arguments of others. Many men speak grammatically without having learnt any system of grammar; in the same manner, many men reason logically without having learnt any system of Logic. But the great majority of men, there can be little doubt, may derive assistance both from one and the other. Grammar fulfils its functions when it raises the student to the level of the most correct speakers; similarly, Logic fulfils its functions when it raises the student to the level of the best reasoners. As applied to the syllogistic rules and formulæ, this defence would now be generally admitted, but it holds equally good of the methods under which it may be shown that our inductive arguments may ultimately be arranged. 'The business of Inductive Logic,' says Mr. Mill, 'is to provide rules and models (such as the Syllogism and its rules are for ratiocination) to which if inductive arguments conform, those arguments are conclusive, and not otherwise. This is what the Four Methods profess to be, and what I believe they are universally considered to be by experimental philosophers, who had practised all of them long before any one sought to reduce the practice to theory.'

With regard to the second objection, that these methods have not been operative in the formation of the sciences, Dr. Whewell seems to ignore the distinction between the conscious and the unconscious employment

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of a method. It is undoubtedly true that in records of scientific investigations we seldom find the formal language in which the Inductive Canons are expressed. It seems to me equally true that in such records we invariably detect the employment of the Canons themselves. Discoveries are of two kinds: they are either entirely the result of patient research, or they are first suggested to the mind by some brilliant thought, and afterwards verified by rigorous proof. In the former case, the discoverer must have made sure of his ground as he proceeded, and, so far as his method was inductive, he could only do so by appealing, consciously or unconsciously, to one or more of the inductive methods; if he acted otherwise, he arrived at a true result by mere accident. In discussing the latter case, I must repeat what has already been stated, that it is not the office of Logic, either inductive or deductive, to suggest thoughts, but to analyse and to test them. Now, in the case we are supposing, the discovery really consists of two parts -the original conception and the subsequent process by which it is determined to be the true explanation of the phenomenon. However striking and appropriate the conception, we have no right to regard it as the true explanation of the phenomenon till it has been subjected to the most rigorous investigation. This investigation must be either inductive or deductive, or both. But, so far as it is inductive, it must conform with the requirements of the Inductive Canons, or else it will not result in positive proof, or even approximate

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closely to it. As in the former case, unless the discoverer has, consciously or unconsciously, reasoned in strict conformity with the requirements of Logic, he has no right to feel any confidence in the result of his researches.

It may be added that appropriate conceptions, promising to be fertile in scientific results, are only likely, as a rule, to occur to persons whose minds have been habitually disciplined by the strict observance, conscious or unconscious, of the laws of reasoning. Originality is not a quality, as some seem to think, which admits of no psychological explanation.

I have not thought it desirable to discuss more recent criticisms of the Inductive Methods, because, apart from the stress which they lay on the difficulty of satisfying the conditions of the Canons (a difficulty which is acknowledged on all sides to exist, at least in many cases), I cannot think that they have added materially to the objections raised by Dr. Whewell.

... The student is particularly requested to read, in connexion with this chapter, the 'Preface to the Third Edition,' reprinted at the beginning of the Book. This Preface deals with certain controverted points respecting the certainty of Inductive Reasoning and the nature of the assumptions made in it, with which, though they could not conveniently be introduced into the body of the book, it is desirable that the student should acquaint himself.

CHAPTER IV.

Of Imperfect Inductions.

AN argument from the particular to the general, or from particulars to adjacent particulars, may fall short of absolute proof, or even of moral certainty, while it commends itself as possessing more or less of probability. Arguments of this character may be called Imperfect Inductions. Under this head fall imperfect applications of the experimental or inductive methods, the argument from analogy, and incomplete cases of *Inductio per enumerationem simplicem*.

The Inductio per enumerationem simplicem is, as already noticed, when complete [Inductio Completa], a deductive, and not an inductive, argument. When incomplete, it is an inductive argument, for it is an inference of the general from the particular or the unknown from the known. This form of Induction affords certainty only when, as in the case of the Laws of Universal Causation and of the Uniformity of Nature, or of the Mathematical Axioms,

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See p. 125, note 2, and Deductive Logic, Part III. chap. i. appended note 2.

it is grounded upon universal experience, and we feel assured that, if there had been at any time or were now in any place any instance to the contrary, it would not have escaped our notice. But, in ordinary cases, the incomplete Inductio per enumerationem simplicem affords only a presumption, sometimes very slight, sometimes tolerably strong, in favour of the position which it is adduced to establish. I perceive, say in five, ten, or twenty cases, that the phenomenon a is attended by the phenomenon δ , and, knowing of no cases in which the one phenomenon is not attended by the other, I begin to suspect that a and b are connected together in the way of causation. Such a surmise may afterwards be proved by the aid of one or other of the five methods to be correct, and, in that case, it is taken out of the category of inductions per enumerationem simplicem, and becomes an instance of a scientific induction. neither proved nor disproved, it still has a certain amount of probability in its favour, that amount depending on the two following considerations: (1) the number of positive instances which have occurred to us; (2) the likelihood, if there be any negative instances, of our having met with them. The first of these considerations deserves little weight, unless supported by the other. A native of the North of Europe, some centuries ago, might, if the mere accumulation of positive instances were sufficient, have taken it for a certain truth that all men had white complexions. His own personal observation, as well as the reports of travellers and the traditions

of his race, would have furnished numberless instances in favour of the position. But, before drawing the inference, he ought to have reflected that he possessed information about a small portion only of the inhabitants of the earth's surface, that a difference of climate might produce a difference of complexion, and that there was no reason for supposing that the anatomical structure of man, or the various characteristics which we denominate human, are necessarily connected with a skin of one particular colour. But, on the other hand, we may affirm with tolerable certainty that all the varieties of beings possessing the physical structure of man have the capacity of articulate speech; for, if there were any races exhibiting the one set of phenomena without the other, there is every probability, with our present knowledge of the earth's surface, that we should be acquainted with their existence. In this instance the first consideration, which in itself would deserve little weight, is converted into a certainty almost absolute by the support which it derives from the second.

It cannot be too strongly impressed on the mind of the student that a mere enumeratio simplex, that is, a mere assemblage of positive instances, unless we have reason to suppose that, were there any instances to the contrary, they would have become known to us, is simply worthless. 'Inductio quæ procedit per enumerationem simplicem res puerilis est.' But if the enumeratio simplex be accompanied by a well-grounded conviction that there are no instances to the contrary, it may afford a very

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high degree of probability, and, if we can assure ourselves that there are no instances to the contrary, to us individually it will afford certainty.

It might seem that an Inductio per Enumerationem Simplicem is always an employment of the Method of Agreement. But there is this essential difference. The Method of Agreement is a method of elimination, selecting some and rejecting other instances, and founding its conclusion not on the quantity but on the character of the instances which it selects. The Inductio per Enumerationem Simplicem, on the other hand, depends for its validity on the number of instances; the instances, indeed, must be gathered from every available field, and hence sometimes we speak of their variety as well as their quantity, but the one essential characteristic of the method is that it does not select, but accumulate instances. A few well-selected instances are often sufficient to satisfy the requirements of the Method of Agreement. The same number, when we abstract the grounds on which they were selected, would be utterly insufficient to justify an Inductio per Enumerationem Simplicem.

It may in fact be remarked of all the Experimental Methods that they are devices for saving labour. The range of our experience is often insufficient to justify an argument founded on an Inductio per Enumerationem Simplicem, but by means of the Experimental or Inductive Methods we so *select* our instances as to bring the particular case which we are investigating under the

general laws of Universal Causation and the Uniformity of Nature. The validity of the induction in question is thus artificially connected with the validity of these universally accepted inductions, and we are enabled to argue from the truth of the latter to that of the former.

Uncontradicted experience, of course, implies a great variety of instances, and, from this point of view, every well-grounded Inductio per Enumerationem Simplicem might be represented as an application of the Method of Agreement. But to represent it in this form would often weaken its force. For, while our experience may be so wide as to justify us in affirming the constant union of two or more circumstances, the number of other common circumstances, known or suspected, with which these are found in invariable combination, may be so large as to render it impossible for us to satisfy even approximately the conditions of the Method of Agreement. Here, as elsewhere, an argument often admits of being stated in two ways, and it is the office of the logician to state it in that form in which it carries the largest amount of conviction, or rather offers the most satisfactory kind of proof.

It is, as I have already pointed out in the First Chapter, by means of an Inductio per Enumerationem Simplicem that we establish what have been called Inductions of Co-existence. This is the case, when, as the result of a wide experience, two phenomena

² Pp. 7-9.

are found to be invariably co-existent, but we have no evidence to connect them as cause and effect, or even as effects of the same cause. Such are the attributes which are found to be invariably united in the same Natural Kinds, that is to say, in the same species of plants, animals, and minerals; such are the two properties of Inertia and Gravity which are found united in all matter. In all these cases, there is probably some causal connexion, hitherto undetected, between the coexisting phenomena; but while we are unable to apply with any success the more refined inductive methods, we must content ourselves with regarding the uniformity as simply one of co-existence. If we made any progress towards the discovery of a causal connexion, the uniformity would be transferred to another category, and would rank amongst the inductions discussed in the last chapter. Meanwhile, these inductions, depending simply on uncontradicted experience, and being at present inaccessible to the Methods of Elimination. must be regarded as generalisations awaiting further investigation *.

The term 'Empirical Generalisation' or 'Empirical

^{*} For a further discussion of the Uniformities of Co-existence, the reader is referred to Mr. Bain's Logic, Bk. iii. ch. 3. I am disposed to estimate more highly than Mr. Bain the probability that these uniformities might, if our knowledge were extended, be ultimately resolved into Uniformities of Causation, and hence they do not appear to me to require any separate or detailed treatment in a work on Logic.

Law' might be conveniently appropriated to express those secondary laws (as distinct from Ultimate Laws of Nature') which are the result of an Inductio per Enumerationem Simplicem. Though these expressions are employed with great latitude, it is usually regarded as characteristic of an Empirical Law or Generalisation that it can only be received as true within the limits of the data from which it is derived, that at another time, at another place, or under different circumstances from those under which the observations were made, it might be found to break down. It is true that, owing to the conflict of causes, this description applies to many of the conclusions arrived at by means of the Inductive

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⁴ Some of these Ultimate Laws of Nature, such as the Law of Universal Causation, the Law of the Conservation of Energy, the invariable co-existence of Inertia with Gravity, &c., appear to rest simply on uncontradicted experience, that is to say, on an Inductio per Enumerationem Simplicem, and still it would seem paradoxical to speak of them as merely 'Empirical Laws.' An Empirical Law might, perhaps, be defined as a secondary law, the causal derivation of which is not yet known or even surmised with any probability, or as a subordinate generalisation arrived at by an Inductio per Enumerationem Simplicem; definitions which, it will be perceived, are really identical. I have, however, avoided any special discussion of what are called 'Empirical Laws,' both on account of the extremely indeterminate use of the expression, and because such a discussion is calculated, in my opinion, needlessly to perplex the student by the complicated questions to which it leads. The advanced student can refer to Mr. Mill's Logic, Bk. III. ch. xv., and Bk. V. ch. v. § 4, but he will be introduced, I venture to suggest, to more difficulties than he will find solved.

See Herschel's Discourse on the Study of Natural Philosophy,
 187, and Mill's Logic, Bk. III. ch. xvi. § 4.

Methods, but it is peculiarly applicable to the results of the Inductio per Enumerationem Simplicem, and it would be extremely convenient to possess an expression by which the results of this method might be at once distinguished from those of scientific induction on the one hand, and those of analogy (to be discussed presently) on the other. Instances of Empirical Laws in this restricted sense are such generalisations as that certain animals or flowers are of a certain colour, that certain tribes of men are less capable of civilisation than others, and, perhaps, that certain appearances of sky are indicative of certain changes of weather. There are, of course, some cases in which it is difficult to determine whether a given conclusion has been arrived at by the Inductio per Enumerationem Simplicem or by an imperfect application of the Method of Agreement, that is to say, whether it is based on instances taken indifferently, or on selected instances.

Another form of imperfect induction is the Argument from Analogy 7. Here we do not argue from a number

[•] The colours of flowers, however, seem to be in a fair way of being accounted for by the peculiarities of their mode of fertilisation. See a most interesting work on the Colours of Flowers, by Mr. Grant Allen, published in Macmillans' *Nature Series*, 1882.

It will be observed that the word 'Analogy' is here employed in the sense of 'resemblance.' In the stricter and more ancient meaning of the term, it signifies an equality of relations (ἐσότητ λόγων). See Aristotle's Ethics, Bk. v. 3 (8). The reader will find the two significations of the word 'Analogy' discriminated in the Elements of Deductive Logic, Part III. ch. i. note 2.

of instances, as in the case of Inductio per Enumerationem Simplicem, but from a number of points of resemblance. The argument is not, that, because S, T, U, V, W, &c. exhibit the union of m with a, b, c, we may therefore expect to find m in Z, or wherever else a, b, c may occur; but that, because X and Y (any two or more instances) agree in the possession of certain qualities a, b, c, we may expect to find the quality m which is presented by X exhibited also in Y. The argument is based, not on the number of *instances* in which the two sets of qualities are found united, but on the number of qualities which are found to be common to two or more instances: the argument is not that I have so often observed a, b, c in conjunction with m

Archbishop Whately defines Analogy as a resemblance of Relations. This definition, if intended to represent the ancient signification of the word, is incorrect. The Aristotelian Analogy is an equality, not a resemblance of relations. The instance given in Eth. Nic. i. 6 (12) is that, in man, the reason (vovs) bears to the living principle (ψυχή) the same relation that the faculty of vision (δψιε) bears to the body (σῶμα): ὡς γὰρ ἐν σώματι δψις, ἐν ψυχἢ νοῦς. The assertion, in this instance, it will be noticed, is that the relation to each other of the two former members of the analogy is, not similar to, but the same as, that of the two latter. The Aristotelian term άναλογία, in fact, exactly corresponds with the term Proportion as employed by mathematicians, and it was by the word Proportio, when not availing themselves of the Greek word Analogia itself, that the Romans expressed this form of argument. See Quinctilian, Inst. Orat. i. 6: 'Analogia quam proxime ex Græco transferentes in Latinum proportionem vocaverunt, hæc vis est: Ut id, quod dubium est, ad aliquid simile, de quo non quæritur, referat; ut incerta certis probet.' I am indebted for this quotation to Mr. Austin's Lectures on Jurisprudence, vol. iii. p. 255.

that I believe these qualities to be conjoined invariably, but that I know X and Y to resemble each other in so many points that I believe them to resemble each other in all.

Thus, because the moon resembles the earth in being a large spheroid revolving round another body, as well as in various other particulars, it may be argued that it probably resembles the earth also in sustaining animal and vegetable life on its surface. But, if every ground of resemblance furnishes a probable reason for assigning to the one body any property known to belong to the other, it is evident that every ground of dissimilarity will also furnish a probable reason for denying of the first body any property known to belong to the second. In estimating, therefore, the value of an analogical argument, we must strike a balance between the known points of resemblance and the known points of difference, and according as the one or the other preponderate, and in the proportion in which the one or the other preponderate, is the weight of the argument to be regarded as inclining. If, for instance, the phenomenon A is known to resemble the phenomenon B in four points, whereas the known points of difference between them are three, and it is discovered that some new property belongs to A but it is uncertain whether it also belongs to B, the value of the analogical argument that it does belong to B will be represented by 4:3.

Before, however, we are justified in drawing this inference, it is necessary to observe certain cautions.

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In the first place, we must have no evidence that there is any causal connexion between the new property and any of the known points of resemblance or difference. If we have such evidence, the argument ceases to be analogical, and, if not a perfect induction, is an imperfect induction of the kind to be described presently. We know, for instance, that animal and vegetable life on the surface of the earth could not exist without moisture; but, so far as we are able to ascertain, there is no moisture on the surface of the moon. Hence we appear to be justified in concluding, not by analogy, but by the Method of Difference (assuming, of course, the accuracy of the observations), that animal and vegetable life, in the sense ordinarily attached to those terms, are not to be found on the moon's surface 5. Again, we happen to know two men who bear a considerable resemblance to each other in character and opinions. One of these men acts in a particular way, and we infer, analogically, that the other will act similarly. But, suppose we ascertain that the act of the former man was due to some particular characteristic, say avarice. The inference will now no longer depend on the ratio of the known points of resemblance to the known points of difference in the characters and opinions of the two men, that is, on analogy, but it will depend mainly on the presence or absence, the strength or weak-

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See the essay Of the Plurality of Worlds (usually attributed to Dr. Whewell), ch. ix. sect. 7-9. The whole of this essay furnishes excellent examples of the employment of the Argument from Analogy, and also illustrates the extreme caution and delicacy which are requisite in estimating its value.

ness, of this particular characteristic in the second man, and, in a subsidiary degree, on the presence or absence, the strength or weakness, of corroborating or countervailing motives; that is, it will depend, not on analogy, but on other modes of induction.

Secondly, though there must be no evidence to connect the property in question with any of the known points of resemblance or difference, there must, on the other hand, be no evidence to disconnect it. If there be such evidence, the point of resemblance or difference with which we know or believe it to be unconnected must, in estimating the value of the analogy, be left out of consideration. The reason is obvious. When we are enquiring whether this property is more likely to be connected with the known points of resemblance or the known points of difference, it is plain that we must only take into account those points with which there is, at least, some chance of its being connected.

Thirdly, we must have no reason to suspect that any of the known points of resemblance or difference, of which the argument takes account, are causally connected with each other. If the compared phenomena agree in the possession of the properties a, b, c, d, e, and of these properties b is an effect of (or causally connected with) a, and d is an effect of (or causally connected with) c, the only properties which ought to be taken into account in estimating the value of the analogy are a, c, e. The moon is supposed to differ from the earth in having no clouds and no water, but, as these two properties

are mutually connected in the way of cause and effect, they can only be allowed to count as one item in instituting a comparison, for the purposes of analogy, between the known points of resemblance and the known points of difference in the two bodies. The enormous difference, on the other hand, between the maximum and minimum temperature of any place on the moon's surface, owing to the extreme length of the lunar days and nights and the absence of any sensible atmosphere, constitutes a distinct point of difference, and, as such, furnishes an additional argument against the habitation of the moon. When we ask to which side the argument from analogy inclines, we are asking whether it is more probable that the property in question (known to belong to the one phenomenon, but not known either to belong or not to belong to the other) is connected, by way of causation, with one of the known points of resemblance, or with one of the known points of difference: but, in calculating the probability, it is essential that every point should, so far as we know, be independent of every other; for it is only in virtue of each being supposed to be an ultimate property or to point to an ultimate property that it has any claim to be taken into the account. Thus, if any two of the properties are found to be joint effects of the same cause or to stand to each other in the relation of cause and effect, they furnish only one argument instead of two. If we say of A that he is likely, under some particular conjuncture of circumstances, to act in the same manner as

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B, because they are both of them vain and selfish, we shall not strengthen our argument by adding a number of characteristics which are deducible from vanity and selfishness, or by adducing a number of individual acts in which these qualities have been exhibited.

Fourthly, it is only when we have reason to suppose that we are acquainted with a considerable proportion of the properties of two objects, that the argument from analogy can have much weight. If we know only a few properties out of a large number, they may happen to be precisely those which are exceptional rather than representative, points of similarity where the objects themselves are mainly dissimilar, or points of dissimilarity where the objects are mainly similar. Thus, we know that in some respects the planet Mars closely resembles the earth, as, for instance, in having an atmosphere, a surface distributed into land and water, and probably a temperature in which life similar to that on our own globe might exist: but it would be very rash to conclude from these data that it also resembles the earth in sustaining animal and vegetable life on its surface; for, though life, such as we understand it, does not appear to be impossible on the planet Mars as it appears to be on many of the other celestial bodies, the number of properties with which we are acquainted is so small as compared with the number of properties with which we are unacquainted that there is little or nothing on which to ground even a probable conclusion. On the other hand, the analogy by which Kepler boldly extended the

three laws gained from the observation of the motion of Mars to the remaining planets was a perfectly sound one; for the orbit of a planet, as compared with the condition of its surface, is a very simple phenomenon, and what was known of the orbits of the other planets made it appear more likely that they would correspond with the orbit of Mars than that they would differ from it.

The value of the Argument from Analogy, then, we see, depends on the ratio of the ascertained points of resemblance to (1) the ascertained points of difference, (2) the entire assemblage of the properties of the objects compared. If the ascertained resemblances are numerous, the ascertained differences few, and we have reason to think that we are well acquainted with the objects compared, the argument from analogy is very forcible. If, on the other hand, the ascertained resemblances only slightly exceed in number the ascertained differences, or if we have reason to suppose that there are numerous properties in the compared objects with which we are unacquainted, the value of the argument from analogy may be very slight. It is commonly said that the value of an argument from analogy ranges from certainty to zero. If it reaches certainty, the argument becomes a complete induction; if it falls to zero, it ceases to be an argument at all; if the probability is expressed by less than one-half, that is, if the number of ascertained resemblances be less than the number of ascertained differences, it is usual to say that analogy

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is against the possession by the one object of a quality known to belong to the other, or, in other words, in favour of their differing in the possession of this quality rather than agreeing in it.

'Besides the competition between analogy and diversity,' says Mr. Mill', 'there may be a competition of conflicting analogies.' An object may be known to resemble one object in some particulars and another in others, and it may be a question with which of the two it ought to be classed, or which of the two it is the more likely to resemble in some unknown property. Thus, for some time it was a question whether a sponge was an animal or a vegetable substance; and it is often by conflicting analogies that we attempt to determine to which of two or more masters a painting or a statue should be ascribed.

The extreme caution which is requisite in employing the Argument from Analogy may be illustrated by the following scientific errors which have resulted from a hasty and inconsiderate employment of this mode of reasoning.

Sir W. Grove, in his Correlation of Physical Forces 10, while combating the once fashionable doctrine of electrical fluids, brings into juxta-position two very interesting instances of hasty analogies.

'The progressive stages,' he says, 'in the History of Physical Philosophy will account in a great measure for the adoption by the early electricians of the theories of fluids.

Mill's Logic, Bk. III. ch. xx. § 2.

¹⁶ Fifth edition, p. 135.

'The ancients, when they witnessed a natural phenomenon, removed from ordinary analogies, and unexplained by any mechanical action known to them, referred it to a soul, a spiritual or preternatural power: thus amber and the magnet were supposed by Thales to have a soul; the functions of digestion, assimilation, &c., were supposed by Paracelsus to be effected by a spirit (the Archæus). Air and gases were also at first deemed spiritual, but subsequently became invested with a more material character; and the word gas, from geist, a ghost or spirit, affords us an instance of the gradual transmission of a spiritual into a physical conception.

'The establishment by Torricelli of the ponderable character of air and gas, showed that substances which had been deemed spiritual and essentially different from ponderable matters were possessed of its attributes. A less superstitious mode of reasoning ensued, and now aëriform fluids were shown to be analogous in many of their actions to liquids or known fluids. A belief in the existence of other fluids, differing from air as this differed from water, grew up, and, when a new phenomenon presented itself, recourse was had to a hypothetic fluid for explaining the phenomenon and connecting it with others; the mind, once possessed of the idea of a fluid, soon invested it with the necessary powers and properties, and grafted upon it a luxuriant vegetation of imaginary offshoots.'

Most of my readers will be aware of the difficulties experienced by the early geologists in accounting for the fact that the strata of our own and other northern countries often contain remains of animals and shells akin to those which are now to be found only in the torrid zone. This difficulty is easily explained by supposing a different distribution of land and water over the

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surface of the globe from that which at present exists. But we must pause before we admit the inference that, because these animals and shells are akin to those which are now found only in warm climates, they must, therefore, have subsisted in a similar temperature.

'When reasoning on such phenomena,' says Sir Charles Lyell¹¹, 'the reader must always bear in mind that the fossil individuals belonged to species of elephant, rhinoceros, hippopotamus, bear, tiger, and hyæna, distinct from those which now dwell within or near the tropics. Dr. Fleming, in a discussion on this subject, has well remarked that a near resemblance in form and osteological structure is not always followed, in the existing creation, by a similarity of geographical distribution; and we must therefore be on our guard against deciding too confidently, from mere analogy of anatomical structure, respecting the habits and physiological peculiarities of species now no more. "The zebra delights to roam over the tropical plains; while the horse can maintain its existence throughout an Iceland winter. The buffalo, like the zebra, prefers a high temperature, and cannot thrive even where the common ox prospers. The musk ox, on the other hand, though nearly resembling the buffalo, prefers the stinted herbage of the arctic regions, and is able, by its periodical migrations, to outlive a northern winter. The jackal (Canis aureus) inhabits Africa, the warmer parts of Asia, and Greece; while the isatis (Canis lagopus) resides in the arctic regions. The African hare and the polar hare have their geographical distribution expressed in their trivial names;" and different species of bears thrive in tropical, temperate, and arctic latitudes.

'Recent investigations have placed beyond all doubt the

¹² Lyell's Principles of Geology, ch. vi. (ninth edition); ch. x. (tenth edition).

important fact that a species of tiger, identical with that of Bengal, is common in the neigbourhood of Lake Aral, near Sussac, in the forty-fifth degree of north latitude; and from time to time this animal is now seen in Siberia, in a latitude as far north as the parallel of Berlin and Hamburgh. Humboldt remarks that the part of Southern Asia now inhabited by this Indian species of tiger is separated from the Himalaya by two great chains of mountains, each covered with perpetual snow,-the chain of Kuenlun, lat. 35° N., and that of Mouztagh, lat. 42°, -so that it is impossible that these animals should merely have made excursions from India, so as to have penetrated in summer to the forty-eighth and fiftythird degrees of north latitude. They must remain all the winter north of the Mouztagh, or Celestial Mountains. The fast tiger, killed in 1828, on the Lena, in lat. 524°, was in a climate colder than that of Petersburg and Stockholm.'

Neither through Analogy nor through Induction by Simple Enumeration can we establish a fact of Causation, though the conclusions of either of these methods may suggest to us such a fact. When we begin to suspect that any one circumstance or set of circumstances is the cause or the effect of another, or connected with it in the way of causation, we ought at once to attempt to apply, if possible, one or more of the Experimental Methods. If we can satisfy ourselves that their conditions, or those of any one of them, have been rigorously fulfilled, we have, of course, obtained a Valid Induction, giving us either absolute or moral certainty. But something considerably short of a rigorous fulfilment of these conditions may still lead to a conclusion, possessing more or less of probability. We may, for in-

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stance, to take the Method of Agreement, feel uncertain whether a and b (any two circumstances) are the only material circumstances which the cases we have examined exhibit in common; but still we may have examined so many, so various, and so well selected instances, that we may be justified in regarding it as highly probable that the two circumstances stand to each other in the relation of cause and effect, or are, at least, connected in the way of causation. Similarly, to take the Method of Difference, in the act of introducing a new antecedent, we may have unwittingly introduced some other new antecedent, or, in omitting an antecedent, we may have unwittingly introduced or omitted some other antecedent; but still we may have exercised such extreme caution as to justify us in feeling an assurance amounting almost, though not altogether, to certainty that the experiment has been rightly performed. The less our assurance of this fact, the slighter is the probability of the conclusion.

There remains one case, which is attended with some perplexity. It sometimes happens that, though we may be unable to establish a fact of causation between two particular phenomena, we may be able to show that some one phenomenon stands in a causal relation to some one or other of a definite number of other phenomena. Thus, supposing a vegetable to be transplanted to a distant part of the world, we may be able to assure ourselves, by excluding other causes of difference, that

any new qualities which it may assume are due either to difference of climate, or to difference of soil, or to both these causes conjointly, though our knowledge may not enable us to assign amongst these alternatives the particular cause or combination of causes to which the effect is due. Now ought such an Inference to be classified as a perfect or an imperfect Induction? If we content ourselves with stating the alternatives, the inference should be regarded, so far as it goes, as a Perfect Induction; for within the limits stated the conclusion may be considered absolutely certain. But if, on any grounds, we suppose one of these alternatives to be more probable than the others, and we state this as our conclusion, the inference is, of course, only a probable one, and should rank as an Imperfect Induction.

The same remarks will apply to those cases in which there is any uncertainty as to the nature of the fact of causation. If the inference be, say, that the two phenomena either are one cause and the other effect, or stand to each other in the relation of cause and effect, though we may be unable to determine which of the two is cause and which is effect, or are both of them effects of the same cause (adding any other alternatives which the particular case may require), the inference is, so far as it goes, a Perfect Induction. But, if one or some only of these alternatives be selected, on any grounds short of absolute or moral certainty, to the exclusion of the others, the inference is only probable, and must be regarded as metely an Imperfect Induction.

Briefly to sum up the contents of this chapter, Imperfect Inductions are the results either of an Induction per Enumerationem Simplicem (to which I propose to appropriate the expression 'Empirical Generalisations'), or of the Argument from Analogy (which I call Analogies), or of an imperfect fulfilment of one or other of the Inductive Methods (to which we might, perhaps, advantageously appropriate the expression 'Incomplete Inductions'). In the two former cases there can be no more than an intimation of a Fact of Causation, while in the last we conceive ourselves to be on the way towards establishing one.

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CHAPTER V.

On the relation of Induction to Deduction, and on Verification.

THE results of our inductions are summed up in general propositions, which are not unfrequently stated in the shape of mathematical formulæ. These general propositions, the results of inductive reasoning, become, in turn, the data from which deductive reasoning proceeds. Though the major premiss of any single deductive argument may itself be the result of deduction, it will invariably be found, as pointed out long ago by Aristotle¹, that the ultimate major premiss of a chain of deductive reasoning is a result of induction. There must be some limit to the generality of the propositions under which our deductive inferences can be subsumed, and, when we have reached this limit, the only evidence on which the ultimate major premiss can repose, if it depend on evidence at all, must be inductive. Thus, most of the deductions in the science of Astronomy, and

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^{1 &#}x27;Η μέν δή ἐπαγανγή ἀρχή ἐστι καὶ τοῦ καθόλου, ὁ δὲ συλλογισμὸς ἐκ τῶν καθόλου. Εἰσὶν ἄρα ἀρχαὶ ἰξ ὧν ὁ συλλογισμὸς, ὧν οὐκ ἔστι συλλογισμός ἐπαγανγή ἄρα.—Εth. Nic. vi. 3 (3). Cp. Eth. Nic. vi. 6 8 (9); Metaphysics, i. 1; Posterior Analytics, ii. 19.

many of those in the science of Mechanics, depend ultimately on the Law of Universal Gravitation; but this Law itself is the result of an induction based upon a variety of facts, including both the fall of bodies to the earth and the motion of the planets in their orbits. Again, a large number of geometrical deductions may be traced up to the ultimate major premiss: 'Things that are equal to the same thing are equal to one another.' But this proposition, if not referred directly to induction, is classed under the head of intuitive conceptions, the most probable, though perhaps not the most commonly received, explanation of which is that which derives them from the accumulated experience of generations, transmitted hereditarily from father to son.

A Deductive Inference combines the results of previous inductions or deductions, and evolves new propositions as the consequence, or, to put the matter in a slightly different point of view, as expressing the total result, of these combinations. I append a few easy examples of the manner in which the results of induction are employed in a deductive argument.

To begin with a very simple instance, but one which will serve as a good illustration of the stage at which our investigations cease to be inductive and become deductive;—suppose we have ascertained by previous inductions, that A produces α , B produces β , C produces $-\frac{\alpha}{2}$, D produces $\frac{\alpha}{2}$, and E produces $\frac{\alpha}{3}$, we know, by calculation—that is, by deductive reasoning—that the total effect of A, B, C, D, E is $\beta + \frac{\alpha}{3}$. In this case

the simple rules of Algebra, governing the addition and subtraction of quantities, combined with the special data here furnished, are the premisses from which our deductive reasoning proceeds.

The proposition proved in Euclid, Book i. Prop. 38, that 'Triangles upon equal bases, and between the same parallels, are equal to one another,' is derived from, or is the total result of, the previous deductions (1) that 'Parallelograms upon equal bases, and between the same parallels, are equal to one another,' (2) that 'Triangles formed by the diagonal of a parallelogram are each of them equal to half the parallelogram' (i. 34), and (3) the previous induction that 'the halves of equal things are equal.'

What is called the Hydrostatic Paradox, namely, that a man standing on the upper of two boards, which form the ends of an air-tight leather bag, and blowing through a small tube opening into the space between the board, can easily raise his own weight, is a combination of two propositions, both gained from experience by means of induction, these propositions being (1) that fluids transmit pressure equally in all directions, (2) that, the greater the pressure brought to bear on any surface from below, the greater the weight which it will sustain (otherwise expressed by the Mechanical Law that action and reaction are equal).

To take another very simple instance of a similar kind. One of the earliest and easiest problems in the Science of Optics is the following: 'A conical pencil of rays is incident upon a plane reflecting surface; to determine the form of the reflected pencil.' The solution, that the reflected pencil will be a cone having for its vertex a certain imaginary point, which can be geometrically determined, on the other side of the surface, is derived from a combination of the experimental truth, gained by induction, that 'the angle of reflexion is equal to the angle of incidence' with the geometrical propositions stated in Euclid i. 8 and i. 29.

In the Science of Political Economy, Ricardo's Theory of Rent, when stated in the slightly modified form that 'the rent of land represents the pecuniary value of the advantages which such land possesses over the least valuable land in cultivation,' is an easy deduction from two principles which are supplied by every one's experience, namely, (1) that land varies in value, and (2) that there is some land either so bad or so disadvantageously situated as to be not worth the cultivating ².

Professor Cairnes' work on the Slave Power furnishes a remarkable example of the successful application of the deductive method to the determination of economical questions. The economical effects of slavery are thus traced. We learn from observation and induction that slave labour is subject to certain characteristic defects:

^{*} The student will find an easy exposition of this Theory in Fawcett's Manual of Political Economy, Bk. II, ch. iii. ad init. As originally stated, Ricardo's theory neglected to take account of advantages of situation, such as proximity to a market, and regarded the value of land as depending solely on its fertility.

it is given reluctantly; it is unskilful; and, lastly, it is wanting in versatility. As a consequence of these characteristics, it can only be employed with profit when it is possible to organise it on a large scale. It requires constant supervision, and this for small numbers or for dispersed workmen would be too costly to be remunerative. The slaves must, consequently, be worked in large gangs. Now there are only four products which repay this mode of cultivation, namely, cotton, sugar, tobacco, and rice. Hence a country in which slave labour prevails is practically restricted to these four products, for it is another characteristic of slave labour, under its modern form, that free labour cannot exist side by side with it. But, besides restricting cultivation to these four products, some or all of which have a peculiar tendency to exhaust the soil, slave labour, from its want of versatility, imposes a still further restriction. 'The difficulty of teaching the slave anything is so great -the result of the compulsory ignorance in which he is kept, combined with want of intelligent interest in his work - that the only chance of rendering his labour profitable is, when he has once learned a lesson, to keep him to that lesson for life. Accordingly, where agricultural operations are carried on by slaves, the business of each gang is always restricted to the raising of a single product. Whatever crop be best suited to the character of the soil and the nature of slave industry, whether cotton, tobacco, sugar, or rice, that crop is cultivated, and that crop only. Rotation of crops is thus precluded

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by the conditions of the case. The soil is tasked again and again to yield the same product, and the inevitable result follows. After a short series of years its fertility is completely exhausted, the planter abandons the ground which he has rendered worthless, and passes on to seek in new soils for that fertility under which alone the agencies at his disposal can be profitably employed.' Thus, from the characteristics of slave labour may be deduced the economical effect of exhaustion of the soil on which it prevails, and the consequent necessity of constantly seeking to extend the area of cultivation. From the peculiar character of the crops which can alone be successfully raised by slave labour may be explained the former prevalence of slavery in the Southern, and its absence in the Northern, States of the American Union; and from the necessity of constantly seeking fertile virgin soil for the employment of slave labour may be explained the former policy of the Southern States, which was invariably endeavouring to bring newly constituted States under the dominion of slave institutions *.

These examples of the combination of inductive with deductive reasoning might be multiplied to any extent. Mechanics, Astronomy, and the Mathematico-physical sciences generally, furnish, perhaps, the most striking instances of it. The great importance of deduction as an instrument for the ascertainment of physical truths

² See Professor Cairnes on the Slave Power, ch. ii. His arguments are stated in a condensed form in Fawcett's Manual of Political Economy, Bk. II. ch. xi.

could hardly be illustrated more appropriately than by the following cases adduced by Sir John Herschel*:—

'It had been objected to the doctrine of Copernicus, that, were it true, Venus [and, it might have been added, Mercury, as the other inferior planet] should appear sometimes horned like the moon. To this he answered by admitting the conclusion, and averring that, should we ever be able to see its actual shape, it would appear so. It is easy to imagine with what force the application would strike every mind when the telescope confirmed this prediction, and showed the planet just as both the philosopher and his objectors had agreed it ought to appear. The history of science affords perhaps only one instance analogous to this. When Dr. Hutton expounded his theory of the consolidation of rocks by the application of heat, at a great depth below the bed of the ocean, and especially of that of marble by actual fusion; it was objected that, whatever might be the case with others, with calcareous or marble rocks, at least, it was impossible to grant such a cause of consolidation, since heat decomposes their substance and converts it into quicklime, by driving off the carbonic acid, and leaving a substance perfectly infusible, and incapable even of agglutination by heat. To this he replied, that the pressure under which the heat was applied would prevent the escape of the carbonic acid; and that being retained, it might be expected to give that fusibility to the compound which the simple quicklime wanted. next generation saw this anticipation converted into an observed fact, and verified by the direct experiments of Sir James Hall, who actually succeeded in melting marble, by retaining its carbonic acid under violent pressure.'

It should be noticed that, for the most part, in the actual conduct of scientific enquiry, there is a constant

^{*} Discourse on the Study of Natural Philosophy, § 299.

alternation of the processes of Induction and Deduction. A truth obtained inductively is often at once used, either by itself or in combination with other propositions, for the purpose of evolving new truths by deduction, while it may also be subsequently employed together with other inductions of the same order for the purpose of leading up inductively to propositions of a higher degree of generality. We are constantly passing from the one process to the other, and back again, and often it becomes exceedingly difficult to determine exactly how much of our ultimate conclusion is due to the one method, and how much to the other. It is an error (though this error has received the countenance of Bacon) to suppose that the process of induction should always be pursued continuously up to a certain point, and that from that point the process of deduction should proceed equally uninterruptedly. We may, and in fact should, frequently pause to consider to what deductive conclusions our inductive inferences lead, or to try whether they may not be connected by a chain of deductive reasoning with wider truths previously ascertained.

A very common instance of the constant interlacing of the inductive and deductive processes just noticed is to be found in the ordinary mode of framing and employing hypotheses. First, our hypotheses are always suggested by some fact, or facts, within our experience. They are thus based on a rough kind of induction. When framed,

On this subject, see the excellent criticism on Bacon in Mr. Mill's Logic, Bk. VI. ch. v. § 5.

we generally proceed to trace the consequences which would ensue on the supposition of their truth. This is a deductive process. Individual facts or inductions from individual facts are then compared with these results, and, if they agree with them, are regarded as confirmatory of the hypothesis. Of course, these processes may be frequently repeated, and are often so repeated, the hypothesis thus constantly gaining in probability, even though it may as yet have no claim to be regarded as an established truth. Lastly, if it attain the position of a valid induction, it must be by the application of one or other of the inductive methods, which converts its previous probability into scientific certainty. Or, perhaps, it may be finally established not by induction at all, but by being brought deductively under some more general law.

These remarks and the instances adduced above naturally lead to a discussion of the place to be assigned in scientific enquiry to the process called Verification. In Deductive Reasoning, especially when it involves elaborate calculations, there is always great danger lest we should have omitted to take into account some particular agency or element, or have miscalculated its effects, or have formed a false estimate of the combined effect of the various agencies or elements in operation. The only remedy against these possible errors, besides the employment of great caution in the conduct of the deductive process itself, is to be found in Verification, a word which,

in its stricter sense, appears to be applied to the process of testing, by means of an appeal to facts, the validity of the conclusions already arrived at by a course of deductive reasoning. Thus it had been deductively inferred from the Copernican theory that the planets Venus and Mercury ought to pass through phases, like the moon, and the application of the telescope, by means of which they were actually seen to assume these phases, furnished a triumphant verification of the inference. Every occurrence of an eclipse of the sun or moon or of the transit or occultation of a star, when it accords with the previous calculations of astronomers, is also an instance of Verification in this, the stricter, sense of the term. The discovery of the planet Neptune affords an excellent instance of the same kind. But the word is often used in a looser sense and extended to all cases in which an appeal is made to facts, as, for instance, when we perform an experiment in order to test the truth of a hypothesis, or where we employ the Method of Difference in order to supplement the characteristic uncertainty attaching to the employment of the Method of Agreement. Of the process denoted by this looser sense of the word, instances will readily occur to every one. Thus, the diminution in the periods of Encke's comet has been regarded by some astronomers (though, perhaps, erroneously) as a verification of the theory that space is filled with an interstellar medium; or, to take an instance from a very different class of subjects, the recent breaking-up of the slave-system in the Southern States of

America may be regarded as a verification of the prediction that slave and free institutions could not long co-exist under the same political form of government. For an instance of a case in which the Method of Difference is called in to verify a previous employment of the Method of Agreement, I may refer back to the enquiry into the cause of crystallization, already adduced in my discussion of those two methods.

There is a still wider application of the word Verification, by which it is extended to any corroboration of one mode of proof by means of another. It thus includes a deductive proof adduced in corroboration of an inductive one. The most common instance of this kind of verification is the inclusion of a partial under a more general law, the partial law having been arrived at inductively, and it being subsequently shown that the more general law leads deductively to it. Thus, the phenomena of the Tides had, prior to the epoch of Newton, been partially explained by the inductive method. Newton, by deducing these phenomena from the Law of Universal Gravitation, not only afforded a much more complete explanation, but also furnished the most convincing verification of the results already arrived at. Similarly, the laws of falling bodies on the earth's surface, which had already been proved inductively, were, from the time of Newton, brought under the law of universal gravitation, and proved deductively from it. The same was also the case with Kepler's Laws, when they were proved ⁶ See pp. 145, 146, 157, 158.

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deductively from the theorem of the Central Force. This mode of Verification is recommended by Mr. Mill, under the name of the Inverse Deductive or Historical Method, as specially applicable to generalisations on society which have been inferred inductively from the study of history or the observation of mankind. These generalisations are subsequently verified by being connected deductively with the general laws of mind or conduct which are furnished by the study of Psychology or Ethology?. It is thus shown that the generalisations of history are such as we might have anticipated à priori from a general knowledge of human nature, and each branch of the enquiry is made in this manner to afford a striking confirmation of the results arrived at by the other.

It frequently happens that what may be called a residual phenomenon affords an unexpected, and, on that account, a striking verification of some law which is not immediately the object of investigation. Thus, to recur to an instance already adduced for another purpose, when it was found that the difference between the observed and calculated velocities of sound was exactly

See above, pp. 204-207, and Mill's Logic, Bk. VI. ch. z. I cannot agree with Mr. Mill in attaching any special importance to the order in which the respective Methods are used in this enquiry. Though the inductive investigation, based on the facts of history or observation, generally precedes the deductive verification from the laws of psychology, we may, and sometimes do, begin with psychological generalisations, and subsequently verify them by an appeal to observed facts. The only essential point is, that the two Methods should be combined, so that the results arrived at by the one may corroborate the results arrived at by the other.

accounted for by the law of the development of heat by compression, this law acquired so novel and striking a confirmation as to leave no doubt of its truth or universality.

It need hardly be remarked that any verification of one inductive proof by another, or of an induction by a deduction, or of a deduction by an induction, should conform with the laws of deductive or inductive reasoning as the case may be. Verification is not a distinct mode of proof, but is simply a confirmation of one proof by another, sometimes of a deduction by an induction, sometimes of an induction by a deduction, and, finally, sometimes of one induction or deduction by another. It must also be borne in mind that the term is not infrequently employed to designate simply the confirmation of a hypothesis by an appeal to facts.

The student will, of course, understand that it is not always necessary to employ Verification. A proof may be so cogent as to need no confirmation. It would be absurd, for instance, to appeal to actual measurement as a verification of the proposition enunciated in *Euclid*, i. 47.

CHAPTER VI.

On the Fallacies incident to Induction.

THE errors incidental to inductive reasoning and to its various subsidiary processes have already, to a great extent, been noticed in the preceding chapters. In laying down the conditions essential to the correct conduct of a process, the mistakes which result from its incorrect conduct necessarily form part of our enquiry. Though, therefore, it may be convenient to pass the inductive fallacies in review, it is assumed that the student is already acquainted with the principal errors to which his processes and methods are liable.

A. To begin with the subsidiary processes, the errors incident to the process of observation, or 'the fallacies of mis-observation,' are well classified by Mr. Mill as those which arise from Non-observation and those which arise from Mal-observation.

- I. Non-observation may consist either (1) in neglecting some of the instances, or (2) in neglecting some of the circumstances attendant on a given instance.
 - (1) With respect to the non-observation of instances, it

was long ago pointed out by Bacon 1 that there is in the human mind a peculiar tendency to dwell on affirmative and to overlook negative instances. Familiar examples of this tendency will readily occur to every one. We think it a 'curious coincidence' that we should suddenly meet a man of whom we have just been talking, that some event should happen of which we dreamed the night before, or that the predictions of a fortune-teller or an almanac should be verified by the facts. The explanation of these 'curious coincidences' is that our attention is arrested by the affirmative instances, whereas

1 Intellectus humanus in its quæ semel placuerunt (aut quia recepta sunt et credita, aut quia delectant) alia etiam omnia trahit ad suffragationem et consensum cum illis: et licet major sit instantiarum vis et copia, quæ occurrunt in contrarium ; tamen eas aut non observat, aut contemnit, aut distinguendo summovet et rejicit, non sine magno et pernicioso prejudicio, quo prioribus illis syllepsibus auctoritas maneat inviolata. Itaque recte respondit ille, qui, cum suspensa tabula in templo ei monstraretur corum qui vota solverant quod naufragii periculo elapsi sint, atque interrogando premeretur, anne tum quidem Deorum numen agnosceret, quæsivit denuo, "At nbi sunt illi depicti qui post vota nuncupata perierint?" Eadem ratio est fere omnis superstitionis, ut in astrologicis, in somniis, ominibus, nemesibus, et hujusmodi; in quibus homines delectati hujusmodi vanitatibus advertunt eventus, ubi implentur; ast ubi fallunt, licet multo frequentius, tamen negligant et prætereunt. At longe subtilius serpit hoc malum in philosophiis et scientiis; in quibus quod semel placuit reliqua (licet multo firmiora et potiora) inficit, et in ordinem redigit. Quinetiam licer abfuerit ea, quam diximus, delectatio et vanitas, is tamen humano intellectui error est proprius et perpetuus, ut magis moveatur et excitetur affirmativis, quata negativis; cum rite et ordine æquum se utrique præbere debeat; quin contra, in omni axiomate vero constituendo, major est vis instantise negativae." -Novum Organum, Lib. I. Aph. xivi.

spondence between the one set of facts and the other altogether escape our notice. We probably talk scores of times during the day of persons whom we do not meet immediately afterwards; we frequently dream in the most circumstantial manner of events which never occur; and, where one prediction of a fortune-teller is verified, scores are probably falsified. The weather-prophets of the almanacs possess a considerable advantage in the fact that, whereas, at all times, there is at least a considerable chance of their predictions turning out true, there are certain periods, such as the equinoxes, at which particular kinds of weather may be anticipated with a probability amounting almost to certainty.

In former generations 'coincidences' of this kind were regarded not simply as 'curious' and 'remarkable,' but as proofs of some causal connexion between the events. To talk of a person was supposed to render his presence more likely; a verified prediction was regarded as evidence of second-sight; and a comet which was observed to be followed by a war was supposed to be, if not the cause of the war, at least a messenger sent from Heaven to proclaim its approach. The tendency to take note of affirmative, and to overlook negative instances, is one of the causes of that hasty generalisation of which I shall speak in a subsequent part of this chapter ².

< 10 kg

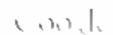
The following remarks of Sir John Herschel, in speaking of the verification of 'signs of the weather,' are so apposite, that I append them in a note.

This tendency is considerably intensified, if the affirmative instances are regarded as illustrations of some preconceived theory, or if the evidence afforded by them be supplemented by some powerful affection of the mind. It seldom happens that men can hold themselves entirely indifferent with respect to two rival

- 'We would strongly recommend any of our readers whose occupations lead them to attend to the "signs of the weather," and who, from hearing a particular weather adage often repeated, and from noticing themselves a few remarkable instances of its verification, have "begun to put faith in it," to commence keeping a note-book, and to set down without bias all the instances which occur to them of he recognised antecedent, and the occurrence or non-occurrence of the expected consequent, not omitting also to set down the cases in which it is left undecided; and, after so collecting a considerable number of instances (not less than a hundred), proceed to form his judgment on a fair comparison of the favourable, the unfavourable, and the undecided cases; remembering always that the absence of a majority one way or the other would be in itself an improbability, and that, therefore, to have any weight, the majority should be a very decided one, and that not only in itself, but in reference to the neutral instances. We are all involuntarily much more strongly impressed by the fulfilment than by the failure of a prediction, and it is only, when thus placing ourselves face to face with fact and experience, that we can fully divest ourselves of this bias.'-Familiar Lectures on Scientific Subjects, Lecture IV.
- ³ 'Habet enim unusquisque (præter aberrationes naturæ humanæ in genere) specum sive cavernam quandam individuam, quæ lumen naturæ frangit et corrumpit; vel propter differentias impressionum, prout occurrunt in animo præoccupato et prædisposito, aut in animo æquo et sedato.' —Bacon's *Novum Organum*, Lib. I. Aph. xlis.
- * Intellectus humanus luminis sleei non est; sed recipit infusionem a voluntate et affectibus; id quod generat ad quod vult scientias: quod enum mavult homo verum esse, id potius credit.'— Novum Organum, Lib. I. Aph. xlix.

opinions and apply themselves to the comparatively unexciting task of collecting evidence impartially on either side. To avoid taking a side on imperfect information, even where our interests or passions are not directly concerned, is one of the last and most difficult lessons learned by the scientific intellect, and by ordinary men it is regarded as a sign of a peculiarly frigid temperament, if not of an indifference to truth. Thus, when the theory involved in the idea of witchcraft had once been conceived and accepted, and especially when it had led to the invention of a new crime, it came to be held that the burden of proof lay with those who called its reality in question. Every story which confirmed the theory would be greedily received, while instances in which the supposed powers of the witch had failed, if noticed at all, would either leave but a slight impression on the mind, or be easily accounted for by supposing the intervention of a higher power. To the numerous class engaged in the administration of the laws, a not unnatural reluctance to question the justice of the principles on which they and their predecessors had been in the habit of acting would furnish an additional inducement to pass lightly over negative instances. Fear, or dread of eccentricity, would operate in the case of others; and thus a theory of the most preposterous character, which, to a mind not preoccupied, received little or no confirmation from facts , and the truth of which could

When a person was convinced that he was subject to the evil



easily have been brought to the test, maintained its ground, and throughout many centuries continued to produce the most mischievous results. The extent of the bias to which the mind, in its observation of instances, is exposed from the influence of strong affections, is patent to every one. A man of a desponding temperament will dwell on the number of those who have failed, a man of a sanguine temperament on the number of those who have succeeded, in their respective professions. A man with strong sympathies will see only virtues or good traits of character, where one of a malevolent or critical disposition will see only vices or blemishes. An ardent adberent of a religious sect or a political party will see nothing but good in those who agree with him, nothing but evil in those who adopt a different creed or profess to be guided by different principles of policy.

Many of the above errors might be otherwise described as arising from the confusion between absolute and relative frequency. We notice how often an event occurs, but we do not notice how much oftener it does not occur.

Not only will a preconceived opinion or a powerful affection come in aid of the natural tendency of men to dwell on affirmative and overlook negative instances, but they will often cause them to adhere to theories for which, whatever may have been the history of their formation,

practices of a witch, this conviction would, of course, sometimes produce the ill effects attributed to witchcraft itself. In other cases, some event, such as a death or an illness, which occurred in the ordinary course of nature, would confirm the suspicion.

there is absolutely no support whatever in fact. Thus, the theory which prevailed down to the time of Galileo , that bodies fall to the earth in times inversely proportional to their weights, so that a body weighing, say, five pounds, would fall in a time five times as short as a body weighing one pound, rested on absolutely no evidence except the fact that, in consequence of the resistance of the air, the heavier body, especially if it be of a denser material, reaches the ground in a shorter time than the lighter one; still, till Galileo made his experiments, at the end of the sixteenth century, from the leaning tower of Pisa, no one thought of bringing to a decisive test a theory which it was so easy to prove or disprove. Even, without having recourse to experiment, one would have imagined that the most casual observations of falling bodies would have revealed, to a mind not strongly pre-occupied, the strange inaccuracy of this theory. The reception accorded to the theory that the weight of the elements increases in a tenfold ratio, so that earth is ten times heavier than water, water ten times heavier than air, and air ten times heavier than fire, seems still more astounding?.

In Sir Thomas Browne's Enquiries into Vulgar and Common Errors, we have an examination of the propo-

Galilæi Systema Cosmicum, Dial. II.

⁷ This theory appears to have originated in a mistaken interpretation of a passage in Aristotle, *De Generatione et Corruptione*, H. 6. See my note on Bacon's *Novum Organum*, Lib. I. Aph. xlv.

Bk. IV. ch. vii.

sition that 'men weigh heavier dead than alive, and before meat than after.' Here are two extraordinary paradoxes which it was perfectly easy for any one to bring to a decisive test; and still, though an appeal to facts would at once have been fatal to them, they appear to have met with a very general reception. The grounds assigned for the prevalence of the latter opinion are so curious that they deserve to be transcribed. 'Many are also of opinion, and some learned men maintain, that men are lighter after meals than before, and that by a supply and addition of spirits obscuring the gross ponderosity of the aliment ingested; but the contrary hereof we have found in the trial of sundry persons in different sex and ages. And we conceive men may mistake, if they distinguish not the sense of levity unto themselves, and in regard of the scale, or decision of trutination. For after a draught of wine, a man may seem lighter in himself from sudden refection, although he be heavier in the balance, from a corporal and ponderous addition; but a man in the morning is lighter in the scale, because in sleep some pounds have perspired; and is also lighter unto himself, because he is refected.' It will be noticed that 'spirits' are supposed to possess the property of positive levity, and that, consequently, they are regarded as making any body into which they enter lighter than it was before. The theory that certain bodies are positively light is itself an instance of a fallacy of non-observation, but, as will be seen presently, of nonobservation of circumstances not of instances.

Another extraordinary instance of a statement which obtained acceptance without any foundation whatever in fact is noticed in an article in the *Quarterly Review* for January, 1865, on 'Aristotle's History of Animals.' Here, however, there appears to be no assignable reason for the mistake.

'Aristotle held some peculiar notions with respect to the skull. He says, "that part of the head which is covered with hair is called the cranium; the fore part of this is called the sinciput; this is the last formed, being the last part in the body which becomes hard." He correctly alludes here to the opening in the frontal bone of a young infant, which gradually becomes hardened by ossification; "the hinder part is the occiput, and between the occiput and sinciput is the crown of the head: the brain is placed beneath the sinciput, and the occiput is empty (!). The skull has sutures: in women there is but one placed in a circle (!); men have generally three joined in one, and a man's skull has been seen without any sutures at all." The often repeated question as to how far Aristotle's observations are the result of his own investigation, naturally suggests itself again here; bad Aristotle ever dissected a human body, he never would have asserted a proposition so manifestly false as that the back of the head is empty, or that women have one only suture placed in a circle.

The passage here noticed occurs in the Historia Animalium, Bk. I. ch. vii. Cp. Bk. III. ch. vii.

A still more remarkable instance of this description of fallacy is noticed in Mr. Lecky's History of European Morals from Augustus to Charlemagne.

Vol. i, p. 394.

'Aristotle, the greatest naturalist of Greece, had observed that it was a curious fact, that on the sea-shore no animal ever dies except during the ebbing of the tide. Several centuries later, Pliny, the greatest naturalist of an empire that was washed by many tidal seas, directed his attention to this statement. He declared that, after careful observations which had been made in Gaul, it had been found to be inaccurate, for what Aristotle stated of all animals, was in fact only true of man. It was in 1727 and the two following years, that scientific observations made at Rochefort and at Brest finally dissipated the delusion.'

I add one more instance, showing the extraordinary readiness with which men, even of remarkable acuteness and erudition, will accept the strangest fancies, though absolutely unsupported by evidence. It is taken from Glanvill's Scepsis Scientifica, published in 1665 10:—

'Besides this there is another way of secret conveyance that's whisper'd about the World, the truth of which I vouch not, but the possibility: it is conference at distance by sympathized handes. For say the relatours of this strange secret: The hands of two friends being allyed by the transferring of Flesh from one into the other, and the place of the Letters mutually agreed on; the least prick in the hand of one, the other will be sensible of, and that in the same part of his own. And thus the distant friend, by a new kind of Chiromancy, may read in his own hand what his correspondent had set down in his. For instance, would I in London acquaint my intimate in Paris, that I am well: I would then prick that part where I had appointed the letter [I] and, doing so in another place to signific that word was done, proceed to [A],

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\sum_{i=1}^{n} \]

¹⁰ Scepsis Scientifica, ch. 24.

thence to [M], and so on, till I had finisht what I intended to make known.'

The influence of some strong passion or affection in causing men to accept theories without any support from observation or experiment, and often in direct defiance of them, may be illustrated from almost all the more powerful feelings of human nature. The mythologies of every nation are full of the wildest and most improbable stories, originating partly in the strength of the religious sentiment, partly in that love of the marvellous which seems to be connatural to every race of mankind, partly in later misinterpretations of that poetical language in which early races are wont to clothe their ideas. stories of the transformation of men into beasts, of rivers flowing backwards, of images falling down from heaven, besides other tales still more fantastic, have been greedily received by generation after generation, in spite of all the analogies of nature and without one single instance to confirm them. The beliefs in ghosts, spiritrapping, and similar phenomena, seem to have their origin in man's insatiable craving for the marvellous, acting often in combination with the feelings of fear, hope, or curiosity. One of the most powerful agents in human affairs is the passion of avarice or the insatiable desire for the accumulation of wealth. In the middle ages, this passion led the alchemists, contrary to all experience, to the belief that it was open to men to become suddenly and enormously rich by discovering the secret of transmuting other metals into gold. In modern

times it has frequently led, and still leads, men to embark in the most desperate speculations, which no scientific calculation of chances would justify. In a lottery, for instance (which is a comparatively innocuous form of speculation), the value of the chance is, owing to the expenses of management and the profit required by the projectors, invariably much less than the price paid for the ticket. But, perhaps, the most remarkable exemplification of the unreasoning desire for sudden accessions of wealth is to be found in the pertinacity with which, in spite of every warning, men would, till within the last few years, expend large fortunes in sinking shafts for coal and other minerals in strata in which the universal experience of geologists and miners testified against their occurrence. In this, as in many other cases, the observations of competent authorities went for nothing; the passion was so absorbing that it alone determined action.

The fallacies due to non-observation of instances may be further exemplified by the tendency of the mind to acquiesce in the first instances which offer themselves 11, especially if they be of a striking kind 12, instead of care-

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¹¹ Axiomata, quæ in usu sunt, ex tenui et manipulari experientia, et pancis particularibus, quæ ut plurimum occurrunt, fluxere; et sunt fere ad mensuram eorum facta et extensa.'—Novum Organum, Lib. I. Aph. xxv.

¹⁸ 'Intellectus humanus illis, quæ simul et subito mentem ferire et subire possunt, maxime movetur; a quibus phantasia impleri et inflari consuevit : reliqua vero modo quodam, licet imperceptibili, ita se habere fingit et supponit, quomodo se habent pauca illa quibus mens

fully searching for other instances of a similar nature with which to compare and by means of which to interpret them. Thus, the phenomena of thunder and lightning would probably have received a much earlier explanation, had the attention of men been sooner directed to the instances of electricity which nature presents of a less striking kind and on a smaller scale. Again, the difficulties presented to early speculators by volcanoes and earthquakes would have been considerably diminished, had they been aware of the fact that there is hardly any portion of the earth's surface which is not undergoing a constant change of level by the process either of elevation or of subsidence, though such change is usually imperceptible to each single generation. The mistakes originating in this source of error are countless. We observe certain peculiarities in some particular representative of a class, profession, or nation, and then proceed to argue as if all the members of the class, profession, or nation were like him. Or, a person on his travels in some country is unfavourably impressed with the hotel-keepers, porters, and carriage-drivers, and then proceeds to denounce the whole nation to which they belong, as if the characteristics of a few exceptional classes were the characteristics of a nationality 13.

obsidetur; ad illum vero transcursum ad instantias remotas et heterogeneas, per quas axiomata tanquam igne probantur, tardus omnino intellectus est et inhabilis, nisi hoc illi per duras leges et violentum imperium imponatur.' Novum Organum, Lib. L. Aph. xlvii.

The history of the French language furnishes a striking instance of non-observation and of the curious and baseless theories to which

The student must have already perceived that I am trenching on Fallacies of Generalisation. When we proceed to treat insufficient evidence, or the absence of evidence, or popular beliefs which run counter to all

it may lead: 'It is well known that before certain feminine substantives, such as messe, mère, soif, faim, peur, &c., the adjective grand keeps its masculine termination, grand'messe, grand'mère, &c. Why so ? Grammarians, who are puzzled by nothing, tell us without hesitation that grand is here put for grands, and that the apostrophe marks the suppression of the final c. But the good sense of every scholar protests against this: after having learnt in childhood that e mute is cut off before a vowel, and never before a consonant, he is told that the e is here cut off without the slightest reason in such phrases as grand'route, &cc. The real explanation is in fact a very different one. In its beginning, French grammar was simply the continuation and prolongation of Latin grammar; consequently the Old French adjectives followed in all points the Latin adjective; those adjectives which had two terminations for masculine and feminine in Latin (as bonus, bona) had two in Old French, whereas those Latin adjectives which had but one (as grandis, fortis, &c.) had only one in French. In the thirteenth century men said une grand femme, grandis femina; une âme mortel, anima mortalis; une contume cruel, consuctudo crudelis; une plaine vert, planitles viridis, &c. In the fourteenth century the meaning of this distinction was no longer understood; and men, deeming it a mere irregularity, altered the form of the second to that of the first class of adjectives, and wrote grande, verte, forte, &c., after the pattern of bonne, &c. A trace of the older and more correct form survives in such expressions as grand'mère, grand'route, grand'faim, grand'garde, &c., which are the dibris of the older language. In the seventeenth century, Vaugelas and the grammarians of the age, in their ignorance of the historic reason of this usage, pompously decreed that the form of these words arose from an euphonic suppression of the e mute, which must be indicated by an apostrophe.'-Brachet's Historical Grammar of the French Tongue, Dr. Kitchin's Transl., Preface, p. vi : Seventh Edition, pp. xxvi-vit

the evidence available, as if they afforded perfectly sufficient evidence, the fallacy is one of inference, and, if the simulated inference be inductive, it is a Fallacy of Generalisation. But the absence or insufficiency of the evidence, if due to our not having kept our minds sufficiently open to facts or not having taken sufficient pains to collect all the facts pertinent to the question, is a Fallacy of Non-observation, and is a defect in the preliminary process rather than in the inductive inference itself. All the instances described above, I believe, fall under this head, though the inferences founded upon them, where they possess any show of justification at all, are cases of unwarranted Inductio per Enumerationem Simplicem, and so afford illustrations of Fallacies of Generalisation.

(2) The second division of the Fallacies of Non-observation is the fallacy which arises from overlooking some of the material circumstances attendant on a given instance. Here the defect is not in the number or pertinency of the instances, but in their character; the description of the instances themselves is untrustworthy. Till we have ascertained that we are fully acquainted with all the material circumstances of the cases examined, we cannot rely upon our facts, and, consequently, we have no right to proceed to ground any inference upon them. The circumstances,' says Sir John Herschel¹⁴, 'which

¹⁴ Herschel's Discourse on the Study of Natural Philosophy, § 111.

accompany any observed fact, are main features in its observation, at least until it is ascertained by sufficient experience what circumstances have nothing to do with it, and might therefore have been left unobserved without sacrificing the fact. In observing and recording a fact, therefore, altogether new, we ought not to omit any circumstance capable of being noted, lest some one of the omitted circumstances should be essentially connected with the fact. . . . For instance, in the fall of meteoric stones, flashes of fire are seen proceeding from a cloud, and a loud rattling noise like thunder is heard. These circumstances, and the sudden stroke and destruction ensuing, long caused them to be confounded with an effect of lightning, and called thunderbolts. But one circumstance is enough to mark the difference; the flash and sound have been perceived occasionally to emanate from a very small cloud insulated in a clear sky; a combination of circumstances which never happens in a thunder storm, but which is undoubtedly intimately connected with their real origin.'

The extreme difficulty of obtaining, by means of the thermometer, a correct measure of the temperature of the atmosphere, owing to the conduction of heat by the stand and its radiation from surrounding objects, and the consequent errors frequently made by observers from not sufficiently providing against, or allowing for, these sources of interference, will serve to every one as a familiar illustration of the great importance of the caution which it is here intended to furnish.

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The following examples, adduced by Mr. Mill¹³, are so interesting and appropriate, that I take the liberty of transcribing them:—

'Such, for instance [namely, the imperfect observation of particular facts], was one of the mistakes committed in the celebrated phlogistic theory; a doctrine which accounted for combustion by the extrication of a substance called phiogiston, supposed to be contained in all combustible matter. The hypothesis accorded tolerably well with superficial appearances: the ascent of flame naturally suggests the escape of a substance; and the visible residuum of ashes, in bulk and weight, generally falls extremely short of the combustible material. The error was non-observation of an important portion of the actual residue, namely, the gaseous products of combustion. When these were at last noticed and brought into account, it appeared to be an universal law that all substances gain instead of losing weight by undergoing combustion; and, after the usual attempt to accommodate the old theory to the new fact by means of an arbitrary hypothesis (that phlogiston had the quality of positive levity instead of gravity), chemists were conducted to the true explanation, namely, that, instead of a substance separated, there was on the contrary a substance absorbed.

'Many of the absurd practices which have been deemed to possess medicinal efficacy, have been indebted for their reputation to non-observance of some accompanying circumstance which was the real agent in the cures ascribed to them. Thus, of the sympathetic powder of Sir Kenelm Digby: "Whenever any wound had been inflicted, this powder was applied to the weapon that had inflicted it, which was, moreover, covered with ointment, and dressed two or three times a day. The wound itself, in the meantime, was directed to

¹⁵ System of Logic, Bk. V. ch. iv. § 4.

be brought together, and carefully bound up with clean linen rags, but, above all, to be let alone for seven days, at the end of which period the bandages were removed, when the wound was generally found perfectly united. The triumph of the cure was decreed to the mysterious agency of the sympathetic powder which had been so assiduously applied to the weapon, whereas it is hardly necessary to observe that the promptness of the cure depended upon the total exclusion of air from the wound, and upon the sanative operations of nature not having received any disturbance from the officious interference of art. The result, beyond all doubt, furnished the first hint which led surgeons to the improved practice of healing wounds by what is technically called the first intention 15.""

The next example I extract from Bp. Wilkins' very curious tractate, entitled A Discovery of a New World, or a Discourse tending to prove that 'tis probable there may be another Habitable World in the Moon:—

'He [that is, 'a late reverend and learned Bishop,' writing 'under the feigned name of Domingo Gonsales' 17] supposeth that there is a natural and usual passage for many creatures betwixt our earth and this planet. Thus, he says, those great multitude of locusts, wherewith divers countries have been destroyed, do proceed from thence. And if we peruse the authors who treat of them, we shall find that many times they fly in numberless troops or swarms, and for sundry days together before they fall are seen over those places in great high clouds, such as, coming nearer, are of extension enough

M Dr. Paris' Pharmacologia, pp. 23-24.

¹⁷ The small tract here referred to is republished in vol. viii. of the Harleian Miscellanies (Park's Edition). The author was Francis Godwin, afterwards Bishop of Hereford, and author of the well-known book De Prasulibus Anglia Commentarius.

to obscure the day, and hinder the light of the sun. From which, together with divers other such relations, he concludes that 'tis not altogether improbable they should proceed from the moon. Thus, likewise, he supposes the swallows, cuckoos, nightingales, with divers other fowl, which are with us only half a year, to fly up thither when they go from us. Amongst which kind, there is a wild swan in the East Indies, which at certain seasons of the year do constantly take their flight thither. Now, this bird being of a great strength, able to continue for a long flight, as also going usually in flocks like our wild geese, he supposeth that many of them together might be thought to carry the weight of a man; especially if an engine were so contrived (as he thinks it might) that each of them should bear an equal share in the burden. So that, by this means, 'tis easily conceivable how once a year a man might finish such a voyage; going along with these birds at the beginning of winter, and again returning with them in the spring 18.1

A more accurate and extended series of observations would, of course, have shown that the birds and locusts migrated from other parts of the earth's surface.

It is not necessary to multiply examples of the errors arising from slovenliness and inattention in the collection or examination of our instances. The necessity of maintaining the strictest caution and accuracy in the conduct of our observations and experiments has already been insisted upon in the Second Chapter of this work.

II. Besides the errors which originate in the neglect of instances or of some of the circumstances which are con-

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Wilkins' Discovery of a New World, Fifth Edition, p. 160.

nected with a given instance, there is another class of errors derived from mistaking for observation that which is not observation at all, but inference. To this class of errors Mr. Mill gives the name of Fallacies of Mal-Observation. That which is strictly matter of perception does not admit of being called in question; it is the ultimate basis of all our reasoning, and, if we are to repose any confidence whatever in the exercise of our faculties, must be taken for granted. But there are few of our perceptions, even of those which to the unphilosophical observer appear to be the simplest, which are not inextricably blended with inference. Thus, as is well known to every student of psychology, in what are familiarly called the perceptions of distance and of form, the only perception proper is that of the various tints of colour acting on the retina of the eye, and it is by a combination of this with perceptions of touch, and of the muscular sense, that the mind gains its power of determining form and distance. Now, a judgment of this kind, which is really due to inference, is, especially by the uneducated and unreflecting, perpetually mistaken for that which is due to direct observation; and thus what is really only an inference from facts is often emphatically asserted to be itself a matter of fact. 'In proportion,' says Mr. Mill 10, 'to any person's deficiency of knowledge and mental cultivation, is generally his inability to discriminate between his inferences and the perceptions on which they were grounded. Many a marvellous tale,

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Mill's Logic, Bk, V, ch, iv. § 5.

many a scandalous anecdote, owes its origin to this incapacity. The narrator relates, not what he saw or heard, but the impression which he derived from what he saw or heard, and of which perhaps the greater part consisted of inference, though the whole is related not as inference but as matter-of-fact. The difficulty of inducing witnesses to restrain within any moderate limits the intermixture of their inferences with the narrative of their perceptions, is well known to experienced cross-examiners; and still more is this the case when ignorant persons attempt to describe any natural phenomenon. "The simplest narrative," says Dugald Stewart, " of the most illiterate observer involves more or less of hypothesis; nay, in general, it will be found that, in proportion to his ignorance, the greater is the number of conjectural principles involved in his statements. A village apothecary (and, if possible, in a still greater degree, an experienced nurse) is seldom able to describe the plainest case, without employing a phraseology of which every word is a theory: whereas a simple and genuine specification of the phenomena which mark a particular disease; a specification unsophisticated by fancy, or by preconceived opinions, may be regarded as unequivocal evidence of a mind trained by long and successful study to the most difficult of all arts, that of the faithful interpretation of nature."

No better instance of the Fallacy of Mal-observation can be given than what was called the common-sense argument against the truth of the Copernican System.

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That the earth should move round the sun, men said, was impossible; for, every day, they saw the sun rise and set and perform his course in the heavens. They felt the earth at rest, they saw the sun in motion, and it was absurd to call upon them to disbelieve the direct evidence of their senses. It need hardly be said that what they mistook for the direct evidence of their senses was really an inference. What they saw was consistent with one or other of two hypotheses, that the sun moved, or that the earth moved; and, neglecting to take any account of the latter, they assumed the former. If it were not for the impressions of a contrary kind derived from the actual motion of the carriage, a man, whirled along in a railway train, might with equal justice maintain, by an appeal to the evidence of his eyesight, that the trees and the houses were running past him.

Ventriloquism supplies another familiar instance of the same error. A man who had never before been imposed upon by the tricks of a ventriloquist, and who was not aware of the character of the deception, would be positive in maintaining that he had the direct evidence of the sense of hearing in support of his belief that the sound he heard proceeded from a particular person or a particular part of the building other than that from which it really came. The fact, of course, is that the sound itself is all that is directly perceived by the sense of hearing; the reference of it to a particular person or a particular place is an act of inference grounded upon constant, or at least frequent, association. What is done by the ven-

triloquist is not to deceive the sense of hearing, but to mislead the faculty of judgment.

What are called 'delusions' and 'hallucinations' furnish a further instance of Mal-observation. . It seems to be now pretty generally agreed that these are due to morbid affections of the sensory ganglia. 'The patient's senses,' says Dr. Maudsley 20, speaking of what he calls sensorial insanity, ' are possessed with hallucinations, their ganglionic central cells being in a state of convulsive action; before the eyes are blood-red flames of fire, amidst which whosoever happens to present himself, appears as a devil, or otherwise horribly transformed; the ears are filled with a terrible roaring noise, or resound with a voice imperatively commanding him to save himself; the smell is perhaps one of sulphurous stifling; and the desperate and violent actions are, like the furious acts of the elephant, the convulsive reactions to such fearful hallucinations. The individual in such a state is a machine set in destructive motion, and he perpetrates the extremest violence or the most desperate murder without consciousness at the time, and without memory of it afterwards.' What is here said of delusions in that extreme form in which they assume unmistakeably the character of madness applies equally, as an explanation, to those less obtrusive, though far more frequent, forms in which they produce semi-insanity, monomania, melancholy, or partial and temporary deception. In all these cases, the

[&]quot; Maudsley, The Physiology and Pathology of Mind, ch. iv. p. 101.



sensations are really experienced; the error consists in referring the cause of the sensations to external objects rather than to the morbid condition or action of the brain itself. The testimony of others, or the inherent improbability of the things perceived, ought to be regarded, though they seldom are, as sufficient proof that the evidence of the senses is given under abnormal and untrustworthy conditions.

To the head of Mal-observation, or the substitution of gratuitous inference for accurate observation, may be referred the fallacy which may, perhaps, best be designated as Exaggerated Comparison. By the side of anything very large, we are apt, being prepossessed by the idea of largeness, to suppose that a small object is smaller than it really is, and, on the other hand, by the side of anything very small, being prepossessed by the idea of smallness, that a large object is larger than it really is. Similarly, of things bright or dark, of periods and distances long or short, of actions good or evil, of evidence probable or improbable, and the like. We are all familiar with the 'only half a mile off,' when we are approaching a town, which we shall probably find to be at least double or treble the distance named. The countryman, of whom we enquire, knows that, in comparison with long distances, the distance is short, and then, unconsciously exaggerating the shortness of the distance, proceeds to name some definite distance which, in his mind, is typical of shortness or which, he thinks, will sufficiently reassure the weary traveller. Instead of

recurring to his own actual experience of the time he takes to walk it, he draws a rapid inference from the fact that the distance is comparatively short to the particular distance which he names. In the same way, men are apt to underrate the probability of an argument as compared with certainty or a very high degree of probability, or, on the other hand, to overrate its probability, as compared with very faint indications of evidence. The concentration of our attention on one term of the comparison perverts our judgment with reference to the other term.

The description here given of the errors originating in Non-observation or Mal-observation includes, as will already have been perceived, the errors incident to artificial as well as to natural observation, that is, to experiment as well as to observation proper.

III. The errors incidental to the other operations preliminary to induction, namely, classification, nomenclature, terminology, and hypothesis, will be sufficiently apparent on a perusal of the sections appropriated to the discussion of those processes. In the steps intermediate between the observation of individual facts and the inductive inference itself, it is in the employment of artificial instead of natural classifications, and in the neglect of the rules designed to guard against the formation of illegitimate hypotheses, that the danger of error mainly lies.

B. The fallacies incidental to the performance of the inductive process itself may be called Fallacies of Generalisation. An error of this class is committed whenever, in arguments grounded on experience, we overrate the value of the evidence before us; that is, whenever we accept an imperfect induction as a perfect one, or whenever, in an induction confessedly imperfect, we underestimate the amount of imperfection.

Of the imperfect inductions, the argument from analogy is little likely to be mistaken for a perfect induction. The strength of the analogy is often grossly exaggerated, and an argument which possesses little or no probability is often adduced as affording highly probable evidence; but, as this kind of argument is very seldom at treated as affording absolute certainty, the discussion of false analogies may be reserved till I have completed the treat ment of those errors which consist in regarding imperfect as perfect inductions.

Excluding analogy, there are, as we have seen, two forms of imperfect induction, that which employs the incomplete Inductio per Enumerationem Simplicem and that which consists in an imperfect fulfilment of the conditions of the inductive methods. An argument of either of these classes may be, and frequently is, mistaken for a perfect induction. I shall first

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²¹ The geological example on p. 236 may perhaps be an instance of an analogical argument thus regarded. Many writers have certainly treated the inference as if its certainty admitted of no doubt.

notice the case in which scientific induction is simulated by the incomplete Inductio per Enumerationem Simplicem 22.

IV. When men first begin to argue from their experience of the past to their expectation of the future, or from the observation of what immediately surrounds them to the properties of distant objects, they seem naturally to fall into this unscientific and unreflective mode of reasoning. They have constantly seen two phenomena in conjunction, and, consequently, they cannot imagine them to be dissevered, or they have never seen two phenomena in conjunction, and, consequently, they cannot imagine them to be associated. The difficulties experienced by children in accommodating their conceptions to the wider experiences of men; the tendency of the uninstructed, and frequently even of the instructed, to invest with the peculiar circumstances of their own time or country the men of a former generation or of another land; the prejudices entertained against those of another creed, or party, or nationality, as if moral excellence were never dissociated from particular opinions or a particular lineage, - are all evidences of the limited character of our first efforts at generalisation. It is long before men learn to discriminate between the

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The student who has read the first and fourth Chapters hardly needs to be reminded that there are cases, however, in which the method of Inductio per Enumerationem Simplicem may, or even must, be employed. The fallacies here treated are due to the unnecessary or injudicious employment of the method.

material and immaterial circumstances attendant on any given phenomenon, to perceive the irrelevancy of the immaterial circumstances, and to recognise the necessity of insisting on a repetition of all the material circumstances before they anticipate a similar effect. But not only is the Inductio per Enumerationem Simplicem the mode of generalisation natural to immature and uninstructed minds; it is the method which, till the time of Bacon ²⁸, or at least till the era of those great discoveries which shortly preceded the time of Bacon, was almost universal. Aristotle, it is true, usually ²⁴ (for

23 Bacon seems to be never weary of condemning this unscientific procedure. Thus, in addition to the aphorism already quoted (p. 125), we have, amongst others, the following emphatic passages: 'Axiomata quæ in usu sunt ex tenui et manipulari experientia, et pancis particularibus, que ut plurimum occurrent, fluxere; et sunt fere ad mensuram corum facta et extensa: ut nil mirum sit, si ad nova particularia non ducant. Quod si forte instantia aliqua, non prius animadversa aut cognita, se offerat, axioma distinctione aliqua frivola salvatur, ubi emendari ipsum verius foret."-Nov. Org. Lib. I. Aph. xxv. 'At philosophiæ genus empiricum placita magis deformia et monstrosa educit, quam sophisticum aut rationale genus; quia non in luce notionum vulgarium (quæ licet tenuis sit et superficialis, tamen est quodammodo universalis, et ad multa pertinens) sed in paucorum experimentorum angustiis et obscuritate fundatum est. . . . Sed tamen circa hujusmodi philosophias cautio nullo modo prætermittenda erat ; quia mente jam prævidemus et auguramur, si quando homines, nostris monitis excitati, ad experientiam se serio contulerint (valere jussis doctrinis sophisticis), tum demum, propter præmaturam et præproperam intellectus festinationem et saltum sive volatum ad generalia et rerum principia, fore ut magnum ab hujusmodi philosophiis periculum immineat; cui malo etiam nunc obviam ire debemus.'-Aph. lxiv.

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²⁴ For exceptions, see Am. Post. I. 31, p. 88, a. 4-5; Top. VIII. 8,

he is not consistent on this point) requires that an induction should be based on an examination of all the instances; but this requirement being in the vast majority of cases (even if we suppose Aristotle to be speaking of species rather than individuals) impossible of fulfilment, he was obliged, whenever he had recourse to experience, to content himself with an inspection of those cases which were nearest at hand. Thus, in the very passage 25 in which he emphatically asserts that the minor premiss of the inductive syllogism (for he represents induction under the syllogistic form) should include all the instances, he argues that all animals which are deficient in bile are long-lived, because he finds this to be the case with the man, the horse, and the mule. Aristotle's works, and especially those on Natural History, abound in rash generalisations of this kind. 'It is a fact,' says Mr. Lewes 20, 'that normally in turtles, and exceptionally in elephants, horses, and oxen, there is an ossification of the septum of the heart. Aristotle saw or heard of one of these "bones" in the hearts of a horse and an ox, and forthwith generalised the observation p. 160, b. 3. For further information on Aristotle's theory of Induction, I must refer the student to the beginning of § 13, and, for a more detailed account of the causes of his failure in his physical researches than can well be given here, to § 11 of the Introduction to my edition of Bacon's Novum Organum.

Analytica Priora, il. 25.

^{*} Lewes' Aristotle, ch. xvi. § 399. On the other hand, the student, who is interested in the history of science, will do well to read, in arrest of judgment on Aristotle, Dr. William Ogle's Introduction to his translation of the De Partibus Animalium.

thus: "The heart is destitute of bones except in horses and in a species of ox; these, however, in consequence of their size, have something bony as a support, just as we find throughout the whole body "." His Spanish follower Funes Y Mendoça improves on this statement by saying that the bone acts like a stick to support the weight of the heart, which is very great.'

There is another passage in which Aristotle tells us that the cranium of a dog consists of a single bone 20.

'It is probable,' says the author of the review previously quoted 30, 'that Aristotle had got hold of the cranium of an old individual in which the sutures had become obliterated.'

The employment of the Inductio per Enumerationem Simplicem prevailed so universally from the time of Aristotle to the rise of modern science that it seems unnecessary to multiply instances of it during that period. But it may be instructive to illustrate from the history of more recent times the peculiar facility with which some even of the greatest discoverers have lapsed into this erroneous form of reasoning.

'Bichat,' says Mr. Lewes to tried to establish a generalisation which has been much admired, namely, that all the

[&]quot; De Partibus Animalium, Bk. III. ch. iv.

^{**} τὰ μὲν γὰρ ἔχει μονόστεον τὰ κρανίον, δισπερ ὁ κόων, τὰ δὲ συγκείμενον, δισπερ ἄνθρωπος.—Historia Animalium, Bk. III. ch. vii.

Quarterly Review, No. 233, Art. ii. The mention of the human skull, which had no sutures, is evidently borrowed from Herodotus, IX. 83.

[&]quot; Lewes' Aristotle, ch. xvi. § 399 d.

organs of Animal life are double and symmetrical, while all the organs of Vegetal life are single and asymmetrical. Unhappily the facts do not fit. In the commencement almost every organ is double and symmetrical; and only in the later stages of development do the differences appear. Even in the matured organism we find many striking exceptions to Bichat's generalisation. Thus the parotid, sublingual, and mammary glands, the lungs, the kidneys, ovaries, and testes, are all vegetal organs, and all generally double. And if the heart and uterus are classed as single organs, then must the brain and spinal cord be classed thus. While in birds the liver is double and symmetrical.'

'It is in a great degree true,' we are informed by Dr. Paris 31, 4 that the sensible qualities of plants, such as colour, taste, and smell, have an intimate relation to their properties, and may often lead by analogy to an indication of their powers; we have an example of this in the dark and gloomy aspect of the Lurida, which is indicative of their narcotic and very dangerous qualities, as Datura, Hyoscyamus, Atropa, and Nicotiana. Colour is certainly in many cases a test of activity; the deepest of coloured flowers, the Digitalis, for example, are the most active, and when the leaves of powerful plants lose their green hue, we may conclude that a corresponding deterioration has taken place with respect to their virtues: but Linnæus ascribed too much importance to such an indication, and his aphorisms are unsupported by facts; for instance, he says, "Color pallidus insipidum, viridis crudum, luteus amarum, ruber acidum, albus dulce, niger ingratum, indicat."'

The early history of Geology presents, in the controversy which was long carried on between the Neptunians and Vulcanians, a remarkable instance of the

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²¹ Pharmacologia, ninth ed. pp. 110, 111.

errors arising from a partial induction, as well as of the tenacity with which men will cling to views to which they have once committed themselves. The Neptunians, the student need hardly be told, referred all geological phenomena to the influence of water, while the Vulcanians greatly exaggerated the action of heat in the past history of the globe, and multiplied to an excess the number of formations to be ascribed to an igneous origin. Of the Neptunians, the great Saxon geologist Werner was the chief.

'Werner,' says Sir Charles Lyell's, 'had not travelled to distant countries; he had merely explored a small portion of Germany, and conceived, and persuaded others to believe, that the whole surface of our planet, and all the mountain chains in the world, were made after the model of his own province. It became a ruling object of ambition in the minds of his pupils to confirm the generalisations of their great master, and to discover in the most distant parts of the globe his "universal formations," which he supposed had been each in succession simultaneously precipitated over the whole earth from a common menstruum or "chaotic fluid." It now appears that the Saxon professor had misinterpreted many of the most important appearances even in the immediate neighbourhood of Freyberg. Thus, for example, within a day's journey of his school, the porphyry, called by him primitive, has been found not only to send forth veins or dikes through strata of the coal formation, but to overlie them in mass."

'In regard to basalt and other igneous rocks, Werner's theory was original, but it was also extremely erroneous.

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Lyell's Principles of Geology, ninth ed. Bk. I. ch. iv.

The basalts of Saxony and Hesse, to which his observations were chiefly confined, consisted of tabular masses capping the hills, and not connected with the levels of existing valleys, like many in Auvergne and the Vivarais. These basalts, and all other rocks of the same family in other countries, were, according to him, chemical precipitates from water. He denied that they were the products of submarine volcanoes; and even taught that, in the primeval ages of the world, there were no volcanoes.'

After describing the complete demolition of this theory by some of Werner's contemporaries, Sir Charles Lyell adds:—

'Notwithstanding this mass of evidence, the scholars of Werner were prepared to support his opinions to their utmost extent; maintaining, in the fulness of their faith, that even obsidian was an aqueous precipitate. As they were blinded by their veneration for the great teacher, they were impatient of opposition, and soon imbibed the spirit of a faction; and their opponents, the Vulcanists, were not long in becoming contaminated with the same intemperate zeal. Ridicule and irony were weapons more frequently employed than argument by the rival sects, till at last the controversy was carried on with a degree of bitterness almost unprecedented in questions of physical science. Desmarest alone, who had long before provided ample materials for refuting such a theory, kept aloof from the strife; and, whenever a zealous Neptunist wished to draw the old man into an argument, he was satisfied with replying "Go and see."

In the Science of Probability, there is an interesting example of the unreflecting application of the Inductio per Enumerationem Simplicem. Averages of a suffi-

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ciently trustworthy character can often be struck as to the frequency of such events as the number of deaths, the number of suicides, the number of lost letters which occur in a year. But the least reflexion ought to show that the accuracy of these calculations depends on the assumption that the causes in operation, so far as they affect these events, will continue to be much the same as at present. This, however, is a consideration which is frequently lost sight of, and thus averages, which may be perfectly true within certain limits and on certain hypotheses, are extended, as if they were true universally and unconditionally. Mr. Venn, in his work on the Logic of Chance 50, has drawn especial attention to this source of error. The following passage selected from that work will, perhaps, afford a sufficient illustration of the point in question :-

'Let us take, for example, the average duration of life. This, provided our data are sufficiently extensive, is known to be tolerably regular and uniform. But a very little consideration will show that there may be a superior as well as an inferior limit to the extent within which this uniformity can be observed. At the present time the average duration of life in England may be, say thirty; but a century ago it was decidedly less; several centuries ago it was very much less; whilst, if we possessed statistics referring to our early British ancestors, we should probably find that there has been since that time a still more marked improvement. What may be the future tendency no man can say for certain. It may be, and we hope will be the case, that, owing to sanitary

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³⁹ Venn's Logic of Chance, chap. i.

and other improvements, the duration of life will go on increasing steadily; it is quite conceivable that it should do so without limit. On the other hand, this duration might gradually tend towards some fixed length. Or, again, it is perfectly possible that future generations might prefer a short and a merry life, and therefore reduce their average. All that I am concerned to indicate is, that this uniformity (as we have hitherto called it) has varied, and, under the influence of future eddies in opinion and practice, may vary still; and this to any extent, and with any degree of irregularity. To borrow a term from Astronomy, we find our uniformity subject to what might be called an irregular secular variation.

'The above is a fair typical instance. If we had taken a less simple feature than the length of life, or one less closely connected with what may be called the great permanent uniformities of nature, we should have found the peculiarity under notice exhibited in a far more striking degree. The deaths from small-pox, for example, or the instances of duelling or accusations of witchcraft, if examined during a few successive years, would have shown a very tolerable degree of uniformity. But this uniformity has risen probably from zero; after various and very great fluctuations seems tending towards zero again; and may, for anything we know, undergo still greater fluctuations in future. Now these examples I consider to be only extreme ones, and not such very extreme ones, of what is the almost universal rule in nature. I shall endeavour to shew that even the few apparent exceptions, such as the proportions between male and female births, &c., may not be, and probably in reality are not, exceptions. A type that is persistent and invariable is scarcely to be found in nature36.

In these and similar cases, the fallacy arises from

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Wenn's Logic of Chance, ch. i. sect. 10, 11.

supposing that mere frequency of occurrence affords a sufficient guide to inference, without reflecting that the events depend on causes, and that, if the causes vary, the character of the events must vary with them.

Sometimes, frequency of occurrence, instead of furnishing an argument for the recurrence of an event, ought, if we duly reflect on the natural action of causes, actually to furnish an argument against it. Thus, a miner, instead of trusting to his rope, because it has served him so often, ought actually to distrust it, because it has been strained so much; a prodigal, who has frequently succeeded in borrowing from his friends, ought to begin to suspect that their patience may be exhausted; a timid man, who has on one or two occasions aroused his neighbours by a false alarm, instead of arguing from experience that they will come to his rescue again, ought rather to expect that, warned by the past, they will remain comfortably in their beds. It cannot be too often repeated, that we ought never to depend on frequency of occurrence, wherever it is possible to have recourse to facts of causation.

It is remarked by Mr. Mill that the Method of Simple Enumeration, though almost banished from the physical sciences, is still the common and received method of induction in whatever relates to man and society. The reason of this remark is to be sought in the extraordinary difficulty of subjecting this class of speculations to the more scientific methods. Moral and social phenomena are so complex that it is often next to impossible to

discover by elimination the true connexion between any two events or sets of facts. Take, for instance, such questions as the influence of any particular form of government upon the welfare of the people among whom it is established, the effects of religion, or of any particular form of religion, upon morals, the social and political conditions most favourable to the development of art or literature or science or commerce. be required to discover the cause of a given effect, our materials are a set of consequents constantly varying in their character and intensity, and a set of antecedents, often very numerous, any one of which may have an appreciable influence in the production of the effect in question; and it is obvious that to detect the precise degree in which the effect is due to any one of these antecedents, even supposing the task to be possible, will require the utmost skill, patience, and dispassionateness in the selection and comparison of instances. Nor, if it be required to discover the effect of a given cause, will the task be much simplified; for, though it may be possible to fix the precise time at which a new cause say a new form of religion, a new form of government, or a new commercial tariff—was introduced, yet, before it can be argued that any novel event which may appear to have resulted from it, is really due to it, as an effect to a cause, the enquirer is bound to satisfy himself (1) that the introduction of the new cause was not accompanied by other causes which may have wholly or partially produced the supposed effect, (2) that the new

cause and the supposed effect are not joint effects of some common cause which he may have overlooked. It is the extreme difficulty of bringing this class of questions within the requirements of scientific induction, that has led, on the one hand, to the employment of the loose Method of Inductio per Enumerationem Simplicem, or of a mere appeal to unsifted experience, and on the other to the disbelief in the possibility of arriving at any satisfactory conclusions upon them. At the same time, there can be little doubt that moral and social enquiries are beginning to emerge from the chaotic state of confusion in which they have hitherto been sunk, and that what are now dignified with the titles of the moral and political sciences, however imperfect they may be, are beginning to be something more than mere collections of random guesses, or conclusions drawn from the first undisciplined impressions of the teaching of experience.

To the class of fallacies originating in the employment of the incomplete Inductio per Enumerationem Simplicem may perhaps be referred the illegitimate use of the Argument from Authority. The opinions or predictions of a certain man or of a certain class of men upon some particular question or questions have been subsequently found to be verified by the issue of events or an examination of the facts. From this circumstance it is sufficiently rash to infer, without further warrant, that the correspondence between these predictions or opinions and the subsequent events or ascertained facts is the result of knowledge, and not of what we call

accident; but, not content even with this inference, men are apt to draw the far more unwarrantable one that this person or class of persons is to be accepted as an authority on all matters, or at least on all matters of the same or of an analogous kind. It is on this principle that a savage, or even an uneducated man in a civilised community, will trust implicitly any person for whom he has conceived a general respect. In nine cases out of ten he probably acts more wisely in trusting to such a person than in trusting to himself. But the same habit of mind, which is a virtue among uneducated men and in primitive states of society, becomes one of the most serious obstacles to progress and knowledge when men, either individually or collectively, have attained that stage at which they are able to enquire for themselves. We have to learn not only that men are to be trusted exclusively within the limits of their own experience, in their own profession or pursuit, but that even within those limits their authority is apt to become tyrannical and irrational unless it is constantly confronted with facts and subjected to the criticism of others.

But an undiscriminating submission to the authority of contemporaries, of which I have hitherto exclusively spoken, has been but a slight source of error when compared with undiscriminating submission to the authority of past generations 38. The latter involves a kind of com-

²⁵ Of this tendency we have many 'glaring instances,' as Bacon would call them. The error has been, so to say, canonised in the

pound fallacy. The authority of an Aristotle or a Galen has come, by the process already described, to be received without question and without limit by his own or by the succeeding generation; and then, by the constant repetition of a similar process, it is received from that generation by the leading minds of the next, from them by their contemporaries, and so on, respect for tradition being blended with respect for a great name, and both these resting for their support on the deference paid to established authority. Many of the propositions accepted without the slightest hesitation by previous generations on this kind of authority now appear to us patently absurd, nor is it without effort that we can realise the universality of their former reception ³⁶. Instances of such propositions have already

proverb 'Mallem cum Platone errare.' There is a characteristic anecdote of Scheiner, who contests with Galileo the honour of having been the first to observe the spots in the sun. 'Scheiner was a monk; and, on communicating to the superior of his order the account of the spots, he received in reply from that learned father a solemn admonition against such heretical notions:—"I have searched through Aristotle," he said, "and can find nothing of the kind mentioned: be assured, therefore, that it is a deception of your senses, or of your glasses." —Baden Powell's History of Natural Philosophy, p. 171.

The increasing unwillingness of men to accept a proposition on mere authority is thus forcibly put by Bentham, Book of Fallacies, Part I. ch. i., first published in French by M. Dumont, in 1815, and in English by 'A Friend,' in 1824.

As the world grows older, if at the same time it grows wiser (which it will do, unless the period shall have arrived at which experience, the mother of wisdom, shall have become barren), the

been given under the head of the Fallacies of Non-Observation, to the production of which class of fallacies the undue devotion to authority has, perhaps, contributed more than any other cause **7. But, in subjects lying remote from ordinary observation, propositions almost equally absurd have held their ground till quite recently; some continue still to maintain themselves, and others no doubt will be propounded, from time to time, to take advantage of the credulity of mankind.

'To give a general currency,' says Dr. Paris 38, 'to a hypo-

influence of authority will in each situation, and particularly in parliament, become less and less.'

'Take any part of the field of moral science, private morality, constitutional law, private law; go back a few centuries, and you will find argument consisting of reference to authority, not exclusively, but in as large a proportion as possible. As experience has increased, authority has been gradually set aside, and reasoning, drawn from facts, and guided by reference to the end in view, true or false, has taken its place.

'In mechanics, in astronomy, in mathematics, in the new-born science of chemistry—no one has at this time of day either effrontery or folly enough to avow, or so much as to insinuate, that the most desirable state of these branches of useful knowledge, the most rational and eligible course, is to substitute decision on the ground of authority to decision on the ground of direct and specific evidence.'

Authority should be classed amongst the Fallacies of Non-Observation; but, though a blind devotion to authority is one of the most powerful influences in leading men to neglect observation and experiment, the disposition to bow thus unduly to it is itself a fact which requires explanation, and one which it is here attempted to explain.

Dr. Paris' Pharmacologia, Introduction, p. 76, &c.

thetical opinion, or medicinal reputation to an inert substance, nothing more is required than the talismanic aid of a few great names; when once established upon such a basis, ingenuity, argument, and even experiment, may open their ineffectual batteries; the laconic sentiment of the Roman satirist is ever opposed to remonstrance :- "Marcus dixit? ita est." A physician cannot err in the opinion of the public, if he implicitly obeys the dogmas of authority. In the most barbarous ages of ancient Egypt, he was punished or rewarded according to the extent of his success; but to escape the former it was only necessary to show that an orthodox plan of cure had been followed, such as was prescribed in the acknowledged writings of Hermes. It is an instinct in our nature to follow the track pointed out by a few leaders; we are gregarious animals, in a moral as well as a physical sense, and we are addicted to routine because it is always easier to follow the opinions of others than to reason and judge for ourselves; and thus do one half of the world live as alms-folk on the opinions of the other half. What but such a temper could have upheld the preposterous system of Galen for more than thirteen centuries, and have enabled it to give universal laws in medicine to Europe, Africa, and part of Asia? What but the spell of authority could have inspired a general belief that the sooty washings of resin could act as a universal remedy? What but a blind devotion to authority, or an insuperable attachment to established custom and routine, could have so long preserved from oblivion the absurd medicines which abound in our earlier dispensatories? for example, the "Decoctum ad Ictericos" of the Edinburgh College, which never had any foundation but that of the doctrine of signatures in favour of the Curcuma and Chelidonium majus; and it is only within a few years that the Theriaca Andromacki, in its ancient form, has been dismissed from our Pharmacopæia. The CODEX MEDICA-MENTARIUS of Paris still cherishes the many-headed monster

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of pharmacy, under the appropriate title of " Electuarium Opiatum Polypharmacum."

'The same devotion to authority which induces us to retain an accustomed remedy with pertinacity, will frequently oppose the introduction of a novel practice with asperity, unless indeed it be supported by authority of still greater weight and consideration. The history of various articles of diet and medicine will prove in a striking manner how greatly their reputation and fate have depended upon authority. It was not until many years after Ipecacuse had been imported into Europe, that Helvetius, under the patronage of Louis XIV, succeeded in introducing it into practice: and to the eulogy of Katharine, queen of Charles II, we are indebted for the general introduction of tea into England.'

'The history of the warm bath presents us with another curious instance of the vicissitudes to which the reputation of our valuable resources is so universally exposed; that which for so many ages was esteemed the greatest luxury in health, and the most efficacious remedy in disease, fell into total disrepute in the reign of Augustus, for no other reason than because Antonius Musa had cured the emperor of a dangerous malady by the use of the *cold* bath. The most frigid water that could be procured was, in consequence, recommended on every occasion: thus Horace, in his epistle to Vala, exclaims—

"Caput ac stomachum supponere fontibus audent Clusinis, Gabiosque petunt, et frigida rura."—Epist. xv. lib. i.

'This practice, however, was doomed but to an ephemeral popularity, for, although it had restored the emperor to health, it shortly afterwards killed his nephew and son-in-law, Marcellus; an event which at once deprived the remedy of its credit and the physician of his popularity.

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'The history of the Peruvian bark would furnish a very curious illustration of the overbearing influence of authority in giving celebrity to a medicine, or in depriving it of that reputation to which its virtues entitle it. This heroic remedy was first brought to Spain in the year 1632, and we learn from Villerobel that it remained for seven years in that country before any trial was made of its powers, a certain ecclesiastic of Alcala being the first person in Spain to whom it was administered in the year 1639; but even at this period its use was limited, and it would have sunk into oblivion but for the supreme power of the Roman church, by whose auspices it was enabled to gain a temporary triumph over the passions and prejudices which opposed its introduction. Innocent the Tenth, at the intercession of Cardinal de Lugo. who was formerly a Spanish Jesuit, ordered that the nature and effects of it should be duly examined, and, upon being reported as both innocent and salutary, it immediately rose into public notice; its career, however, was suddenly stopped by its having unfortunately failed, in the autumn of 1652, to cure Leopold, Archduke of Austria, of a quartan intermittent; this disappointment kindled the resentment of the prince's principal physician, Chifletius, who published a violent philippic against the virtues of Peruvian bark, which so fomented the prejudices against its use, that it had nearly fallen into total neglect and disrepute."

In discussing the Argument from Authority, I have already touched on the Argument from Universal Consent. 'This is a proposition to which we cannot refuse our assent, for it is accepted by all mankind.' In dealing with this argument, we must always ask, first of all, whether the proposition assented to expresses an immediate perception or an inference. If it expresses the former, we cannot call it in question, for the immediate

perceptions of men are ultimate facts, true, at all events, to us, and admitting of no further test. But if the proposition expresses an inference, as, for instance, in the case of the belief in the motion of the sun round the earth, or the non-existence of antipodes, we must proceed to ask further what are the grounds of the inference, and, unless the grounds of the inference approve themselves to us, we are at liberty to doubt or reject it. At the same time, this argument, even though the proposition only express an inference, may possess considerable, if not overwhelming, force, provided that the conclusion has been arrived at by a number of competent persons after due examination, and as a result of independent investigation. Even here, however, the true authority is that of the competent investigators, not that of their credulous or incompetent followers 89. The latter, as was once said by the late Bishop Thirlwall, may be regarded as the ciphers after a decimal point 4.

V. The errors incident to the employment of the various Inductive Methods have already been pointed out

[&]quot;Verus enim consensus is est, qui ex libertate judicii (re prius explorata) in idem conveniente consistit. At numerus longe maximus eorum, qui in Aristotelis philosophiam consenserunt, ex præjudicio et auctoritate aliorum se illi mancipavit; ut sequacitas sit potius et coitio, quam consensus.'—Bacon, Nov. Org., Lib. I. Aph. lxxvii.

^{**} Cp. Glanvill's Scepsis Scientifica, ch. xvii.: 'Authorities alone with me make no number, unless Evidence of Reason stand before them: for all the Cyphers of Arithmetic are no better than a single nothing.'

in my detailed description of each of these Methods, but it may be useful in this place to take note of certain forms of fallacy which appear to be common to them all.

The Inductive Methods may all be regarded as devices for the elimination of extraneous circumstances and for the establishment of a causal connexion between some two phenomena, a and b, the connexion which it is sought to establish being generally that of cause and effect. Now, in our investigation, we may either have mistaken the precise relation between a and b, or we may have overlooked some other material circumstance or group of circumstances, c. In the former case, the most common sources of error are either the inversion of cause and effect or the neglect of their reciprocal action, the 'mutuality of cause and effect,' as it is called by Sir G. C. Lewis. In the latter case (supposing a to be the presumed cause, and δ the presumed effect), it seems open to us to have committed any of the following errors: (1) to have mistaken a for the cause, when the real cause is c; (2) to have mistaken a for the sole cause, when a and c are the joint causes, either (a) as both contributing to the total effect, or (B) as being both essential to the production of any effect whatever 41; (3) to have mistaken a for the cause of b, when they are really

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The distinction may be illustrated by a familiar example. If a cistern is filled by two pipes, the water passing through each contributes to the total amount of water in the cistern. But, if the cistern is filled by one pipe having two taps, one above the other, both taps must be turned in order that the cistern may receive any water whatever.

both of them effects of c; (4) to have mistaken a for the proximate cause of b, when it is really only the remote cause, c, which has escaped our attention, being the proximate cause.

To begin with the latter class of errors.

(1) The following extract from Mr. Lewes' Physiology of Common Life ** may serve as an illustration of the first subdivision:—

'One very general, indeed almost universal, misconception on this subject (asphyxia or suffocation) is that carbonic acid is poisonous in the blood; but the truth seems to be that the carbonic acid is noxious only when it prevents the access of oxygen. There is always carbonic acid in the blood, both venous and arterial. Its accumulation in the blood is only fatal when there is such an accumulation in the atmosphere as will prevent its exhalation; its mere presence in the blood seems to be quite harmless, even in large quantities, provided always that it be not retained there to the exclusion of oxygen. Carbonic acid, when absorbed into the blood, which is alkaline, cannot there exert its irritant action as an acid, because it will either be transformed into a carbonate or be dissolved. Bernard has injected large quantities into the veins and arteries, and under the skin, of rabbits, and found no noxious effect ensue. The more carbonic acid there is in the blood, the more will be exhaled, provided always that the air be not already so charged with it as to prevent this exhalation."

Here there are really two antecedents, the presence of carbonic acid and the exclusion of oxygen, and the noxious effects, which are erroneously ascribed to the

⁴⁹ Vol. i, p. 383.

former cause, ought properly to be referred to the latter.

The above extract exemplifies this error as vitiating an application of the Method of Agreement. In the following extracts from Dr. Paris' *Pharmacologia*, it will be seen also to vitiate applications of the Method of Difference:—

'Soranus, who was contemporary with Galen, and wrote the life of Hippocrates, tells us that honey proved an easy remedy for the aphthæ of children; but, instead of at once referring the fact to the medical qualities of the honey, he very gravely explains it, from its having been taken from bees that hived near the tomb of Hippocrates 43!

'In my life of Sir Humphry Davy, I have published an anecdote which was communicated to me by the late Mr. Coleridge, and which bears so strikingly upon the present subject that I must be excused for repeating it. As soon as the powers of nitrous oxide were discovered, Dr. Beddoes at once concluded that it must necessarily be a specific for paralysis: a patient was selected for the trial, and the management of it was entrusted to Davy. Previous to the administration of the gas, he inserted a small pocket thermometer under the tongue of the patient, as he was accustomed to do upon such occasions, to ascertain the degree of animal temperature, with a view to future comparison. The paralytic man, wholly ignorant of the nature of the process to which he was to submit, but deeply impressed, from the representations of Dr. Beddoes, with the certainty of its success, no sooner felt the thermometer under his tongue, than he concluded the talisman was in full operation, and in a burst of

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⁴⁸ Pharmacologia, p. 20.

enthusiasm declared that he already experienced the effect of its benign influence throughout his whole body: the opportunity was too tempting to be lost; Davy cast an intelligent glance at Mr. Coleridge, and desired his patient to renew his visit on the following day, when the same ceremony was performed, and repeated every succeeding day for a fortnight, the patient gradually improving during that period, when he was dismissed as cured, no other application having been used.

'Amongst the numerous instances which have been cited to show the power of faith over disease, or of the mind over the bodily organs, the cures performed by royal touch have been considered the most extraordinary: but it would appear, upon the authority of Wiseman, that the cures which were thus effected were in reality produced by a very different cause; for he states that part of the duty of the royal physicians and serjeant surgeons was to select such patients afflicted with scrofula as evinced a tendency towards recovery, and that they took especial care to choose those who approached the age of puberty. In short, those only were produced whom Nature had shown a disposition to cure; and as the touch of the king, like the sympathetic powder of Digby, secured the patient from the mischievous importunities of art, so were the efforts of Nature left free and uncontrolled, and the cure of the disease was not retarded or opposed by the administration of adverse remedies. The wonderful cures of Valentine Greatricks, performed in 1666, which were witnessed by contemporary prelates, members of parliament, and fellows of the Royal Society, amongst whom was the celebrated Mr. Boyle, would probably, upon investigation, admit of a similar explanation. It deserves, however, to be noticed that, in all records of extraordinary cures performed by mysterious agents, there has

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⁴ Pharmacologia, p. 28.

always been a desire to conceal the remedies and other curative means which might have been simultaneously administered. Thus Oribasius commends, in high terms, a necklace of peony-root for the cure of epilepsy; but we learn that he always took care to accompany its use with copious evacuations, although he assigns to them not the least share of credit in the cure. In later times, we have an excellent specimen of this species of deception, presented to us in a work on scrofula by Mr. Morley, written, as we were informed, for the sole purpose of restoring the much-injured character and use of the vervain; in which the author directs the root of that plant to be tied with a yard of white satin riband around the neck ;-but mark-during the period of its application, he calls to his aid the most active medicines in the materia medica. "It is unquestionable," says Voltaire, speaking of sorceries, "that certain words and ceremonies will effectually destroy a flock of sheep, if administered with a sufficient portion of arsenic 46."

'Our inability upon all occasions to appreciate the efforts of nature, in the cure of disease, must necessarily render our notions, with respect to the powers of art, liable to numerous errors and deceptions. Hence protracted or wire-drawn cures ought to be very cautiously received as evidences of the success of medical treatment. Many diseases require only time to enable nature to remove them. All the long train connected with hysteria are cured by time; the solution of which, as Mr. Travers has observed, is to be found in the fact that the hysteric period wanes, and the restlessness of the temperament undergoes a slow but salutary change. Nothing, certainly, is more natural, although it may be very erroneous, than to attribute the cure of a disease to the last medicine that had been administered; the advocates even of amulets and charms have been thus enabled to appeal to

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⁴⁵ Pharmacologia, p. 30.

the testimony of what they call experience, in justification of their superstition 44.7

Of a similar character was the old superstition, noticed by Sir Thomas Browne ⁴⁷ and many other authors, that the hardest stone could be broken by goat's blood:—

'And, first, we hear it in every mouth, and in many good authors read it, that a diamond, which is the hardest of stones, not yielding unto steel, emery, or any thing but its own powder, is yet made soft, or broke by the blood of a goat. But this, I perceive, is easier affirmed than proved. For lapidaries, and such as profess the art of cutting this stone, do generally deny it; and they that seem to countenance it have in their deliveries so qualified it, that little from thence of moment can be inferred for it. For first, the holy fathers, without a further enquiry, did take it for granted, and rested upon the authority of the first deliverers. . . . But the words of Pliny, from whom most likely the rest at first derived it, if strictly considered, do rather overthrow, than any way advantage this effect. His words are these: Hircino rumpitur sanguine, nec aliter quam recenti calidoque macerata, et sic quoque multis ictibus, tunc etiam præterquam eximias incudes malleosque ferreos frangens. That is, it is broken with goat's blood, but not except it be fresh and warm, and that not without many blows, and then also it will break the best anvils and hammers of iron."

The example of Sir Kenelm Digby's sympathetic powder (already quoted pp. 270-1) also illustrates this class of fallacies 48.

A Pharmacologia, p. 88.

⁴⁷ Enquiry unto Vulgar and Common Errors, Bk. II. ch. v. Collected Works, vol. ii. pp. 334, 335.

[&]quot;These instances, together with many others in this chapter,

It strould be noticed that, when we attribute a phenomenon to a wrong cause, it does not always follow that this cause, had it been in action, might not have produced the event. Thus, we may wrongly attribute death in some given case to poison, or infection to actual contact with a diseased person, or ignition to friction, because these causes were not then and there in action, though, had they been actually operating, they would have been perfectly competent to produce the effect. When we make a mistake of this kind, it frequently arises from our concentrating our attention exclusively on some one or a few of the possible causes which may produce a given effect, thus neglecting the consideration of the Plurality of Causes, to which attention has repeatedly been drawn in the previous pages ¹⁹.

(2) When an effect is the joint result of two or more

illustrate the ancient fallacies 'Non causa pro causa,' and 'Post hoc, ergo propter hoc.' It will probably have already occurred to the student that some of the examples just cited might have been equally well adduced as examples of the fallacy of non-observation. It, in fact, frequently happens that the same error may be assigned indifferently to two or more sources of deception. 'From the elliptical form,' says Archbishop Whately (Elements of Logic, Bk. iii. § 1), 'in which all reasoning is usually expressed, and the peculiarly involved and oblique form in which fallacy is for the most part conveyed, it must of course be often a matter of doubt, or rather of arbitrary choice, not only to which genus each kind of fallacy should be referred, but even to which kind to refer any one individual fallacy.' Thus, so intimately are our intellectual operations blended, that it is often extremely difficult to decide whether a mistake be mainly due to defective observation or erroneous reasoning.

^{*} See pp. 6, 23, 127-8, 131-4.

causes, the causes may either simply contribute towards the production of the total result, though one only would produce some portion of it, or they may all be essential to the production of any result whatever. It would be convenient if, in the former case, we could speak of the causes as joint causes, in the latter as joint conditions, but to do so would perhaps be too great an innovation on established language.

(a) An instance of supposing that a phenomenon is entirely due to one cause, when it seems in reality to be only partially due to it, is furnished by the prevalent notion that the heart is the sole cause of the circulation of the blood.

'What is it,' says Mr. Lewes⁵⁰, 'which causes the blood to circulate? "The heart," answers an unhesitating reader. That the heart pumps blood incessantly into the arteries, and that this pumping must drive the stream onwards with great force, there is no doubt; but, although the most powerful agent in the circulation, the heart is not the sole agent; and the more we study this difficult question, the more our doubts gather round the explanation.'

'Let a few of the difficulties be stated. There have been cases of men and animals born without a heart; these "acardiac monsters" did not live, indeed could not live; but they had grown and developed in the womb, and consequently their blood must have circulated. In most of these cases there has been a twin embryo, which was perfect; and the circulation in both was formerly attributed to the heart of the one; but it has been fully established that this is not the case. Further, Dr. Carpenter reminds us that "it has occa-

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³⁶ Physiology of Common Life, vol. i. p. 322.

sionally been noticed that a degeneration in the structure of the heart has taken place, during life, to such an extent that scarcely any muscular tissue could at last be detected in it, but without any such interruption to the circulation as must have been anticipated if this organ furnishes the sole impelling force." On the other hand, an influence acting on the capillaries will give a complete check to the action of the heart, although that organ is itself perfectly healthy and vigorous.'

Mr. Lewes then proceeds to discuss the subject at greater length, but the above quotation is sufficient for my purpose.

A familiar instance of this error occurs in the vulgar notion that the mean annual temperature of a place is exclusively determined by its latitude. The reader need hardly be told that in this case there are many other causes at work, namely, elevation, distance from the sea, proximity of mountain chains, and the like.

When a number of causes contribute towards the total effect, it is plain that, as in the last instance, they may operate in the way of modifying, counteracting, or even frustrating ⁶¹ each other's influence. This is a consideration which it is often of the utmost importance to bear in mind, as will be obvious from the following examples, extracted, the former from Dr. Paris' Pharmacologia ⁶², the latter from Sir G. C. Lewis' Methods of Observation and Reasoning in Politics ⁶³.

We sometimes speak of causes 'wholly or partially counteracting each other.' It would be an advantage if we could appropriate the word frustration to express complete counteraction.

st P. 498.

⁶⁸ Vol. i. p. 386.

'In ordering saline draughts as vehicles for active medicines, it is very important that they should be rendered perfectly neutral; the effect of a predominating acid or alkali may produce decompositions fatal to the efficacy of the remedy, as the practitioner will fully understand by a reference to the Acetate of Ammonia and other preparations in the Table of Incompatibles. In prescribing them to be taken in a state of effervescence, we must consider whether the disengaged carbonic acid may not invalidate the powers of the remedies simultaneously given with them. I should certainly recommend such a form to be avoided, in all cases where a salt of lead had been administered, for the carbonic acid retained in the stomach might probably convert it into a carbonate.'

But it is to be borne in mind that, in estimating negative instances, due allowance must be made for the occasional frustration of causes..... For example: it might be argued, from the occurrence of several cases in which the absence of high import duties and of commercial restrictions was accompanied with abundance and cheapness of commodities, that the former was the cause of the latter. Certain instances might then occur, in which the former existed without the latter; but each of these exceptional cases might be accounted for, by showing that there was a special circumstance, such as a deficient supply, or interruption of intercourse by war or blockade, which partially obstructed, and for a time suspended, the operation of the former cause. Again: it might be shown, by the evidence of facts, that the operation of a new law had been generally beneficial, with the exception of certain districts, where its enforcement had been prevented or retarded by certain peculiar and accidental circumstances. Exceptions of this kind, which admit of an adequate special explanation, serve rather to confirm the general inference than to weaken it; inasmuch as they raise the pre-

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sumption that, but for the partial obstruction to the cause, it would have operated in these as in the other instances where no obstructions existed ⁵⁴.'

'It is probably from observing this case of the problem of causation, that the popular error has arisen of supposing that a rule is sometimes proved by its exceptions. Every exception to a general proposition must, in so far as it is an exception, detract from the application of the proposition, and consequently disprove [or rather go towards disproving] it. Thus, if it were asserted that all cloven-footed animals ruminate, this assertion certainly would receive no confirmation from the fact, that certain cloven-footed animals-such as the hog-do not ruminate. If, however, the exception, as in the case which we have been examining, admitted of a peculiar explanation, and it could be shown that the nisus or tendency of the cause was the same in the exceptional as in the other instances, but that in the former it was counteracted and overcome, while in the latter it was not-then the exception may be said not to invalidate, but rather to confirm the rule.

The above passage is noteworthy, as furnishing a good comment on the maxim, Exceptio probat regulam, a maxim which is, of course, only applicable where the exceptions are apparent, and where they admit of explanation in conformity with the rule.

(β) That every event depends upon the concurrence of a number of causes, positive and negative, or, as they are often called, conditions, has already been pointed out (Chap. I. pp. 13-16). Thus, the burning of a fire

M Sir G. C. Lewis' Methods of Observation and Reasoning in Politics, vol. i. p. 386.

depends not only on the application of a lighted match and the supply of fuel, but also on the presence of atmospheric air, or rather of the oxygen which it contains, though, from the universal presence of air, we are less apt to think of the latter cause than of the former ones. The importance, however, of not overlooking this consideration is shown by the extent to which we can augment the temperature by constantly bringing fresh currents of air into contact with any heated mass, as well as by the similar and familiar phenomenon of the increased brightness with which a fire burns on a frosty day, owing to the better draught.

The importance of bearing in mind that an event depends upon a concurrence of causes may be further illustrated by the boiling-point of water. The point at which water (by which I mean pure water) boils depends slightly on the nature of the vessel, but mainly upon two causes or conditions, the temperature of the water and the pressure of the atmosphere. Now, as the latter varies at different heights and in different states of weather, water does not always boil at the same temperature, the boiling-point being, as a rule, diminished by 1° for every 590 feet that we ascend, so that, whereas at the sea level water boils at about 212° Fahrenheit, on the top of Mont Blanc it boils at about 185°. It is obvious that any one, not bearing in mind this fact, might be exposed to the greatest practical inconveniences.

The following quotations from Dr. Paris' *Pharmaco-logia* will furnish a sufficient illustration of the importance

of this consideration and of the errors which may result from neglecting it.

'In some cases of irritability of stomach, the addition of a small quantity of opium will impart efficacy to a remedy otherwise inert; an emetic will often thus be rendered more active, as I have frequently witnessed in my practice. some states of mania, and affections of the brain, emetics will wholly fail, unless the stomach be previously influenced and prepared by a narcotic. I have often also found that the system has been rendered more susceptible of the influence of mercury by its combination with antimony and opium. So, again, when the system is in that condition which is indicated by a hot and dry skin, squill will fail in exciting expectoration; but administer it in conjunction with ammonia, and in some cases with Antimonial Wine and a saline draught, and its operation will be promoted. As a diuretic, Squill is by no means active, when singly administered, but Calomel, or some mercurial, when in combination with it, appears to direct its influence to the kidneys, and in some unknown manner to render these organs more susceptible of its influence 58."

'It has been determined by the most ample experience that substances will produce effects upon the living system, when presented in a state of simple mechanical mixture, very different from those which the same medicinal ingredients will occasion when they are combined by the agency of chemical affinity. To illustrate this by a simple case,—a body suspended in a mixture in the form of a powder, will act very differently if held in solution by a fluid. The relative effects of alcohol in the form of what is termed "spirit," and in that of wine, may be explained upon the same principle; in the former case it is in a state of mixture, in the latter in

Pharmacologia, p. 388.

that of combination. It has been demonstrated, beyond all doubt, that a bottle of port, madeira, or sherry, actually contains as much alcohol as exists in a pint of brandy; and yet how different the effect!—a fact which affords a very striking illustration of the extraordinary powers of chemical combination in modifying the activity of substances upon the living system.

'It has been very generally supposed that substances, whose application does not produce any sensible action upon the healthy system, cannot possess medicinal energy; and, on the contrary, that those which occasion an obvious effect must necessarily prove active in the cure or palliation of disease. To this general proposition, under certain limitations and restrictions, we may perhaps venture to yield our assent; but it cannot be too early, nor too forcibly impressed upon the mind of the young practitioner, that medicines are, for the most part, but relative agents, producing their effects in reference only to the state of the living frame. We must, therefore, concur with Sir Gilbert Blane in stating that the virtues of medicines cannot be fairly essayed, nor beneficially ascertained, by trying their effects on sound subjects, because that particular morbid condition does not exist which they may be exclusively calculated to remove; thus, in a robust state of the body, the effects of steel, in commendation of which, in certain diseases, professional opinion is unanimous, may be wholly imperceptible. Bitter tonics, also, may either prove entirely inert, or they may give strength, relax the bowels, or induce constipation, according to the particular condition of the patient to whom they are administered; so again, in a healthy state of the stomach, a few grains of soda or magnesia will not occasion the least sensible effect, but, where that organ is infested with a morbid acid, immediate relief will follow the ingestion of the one, and purgation that

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^{*} Pharmacologia, pp. 426, 427.

of the other. By not reasoning upon such facts, physicians have, in my opinion, very unphilosophically advanced to conclusions respecting the inefficacy of certain agents. They have administered particular preparations in large doses, and, not having observed any visible effects, have at once denounced them as inert. I might allude, for instance, to the tris-nitrate of bismuth, a substance which, however powerless in health, I am well satisfied, from ample experience, is highly efficacious in controlling certain morbid states of the stomach. Dr. Robertson has well observed that disease calls forth the powers, and modifies the influence of medicines. That which agitates the calm of health may soothe the irritation of illness, and that, which without opposition is inert, may act powerfully where it meets with an opponent. Experiments should be made on the sick, in order to determine how the sick will be affected, and nothing should be pronounced feeble, merely because it has done nothing where there was nothing to be done 87.1

To adduce one more illustration: insanity, though sometimes due to a number of causes, each one of which simply contributes to and augments the affection, which would still exist, though in a weaker degree, even if some of them were absent, appears at other times to be the joint result of a number of causes, the presence of every one of which seems to be essential to the production of any effect so definite as to deserve the name of mental derangement. The train, in these cases, appears to be laid by a number of precedent circumstances, and the addition of some one other circumstance seems to be the spark which produces the conflagration.

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st Pharmacologia, pp. 133, 134.

'When we are told,' says Dr. Maudsley 58, 'that a man has become deranged from anxiety or grief, we have learned very little if we rest content with that. How does it happen that another man, subjected to an exactly similar cause of grief, does not go mad? It is certain that the entire causes cannot be the same where the effects are so different; and what we want to have laid bare is the conspiracy of conditions, internal and external, by which a mental shock, inoperative in one case, has had such serious consequences in another. A complete biographical account of the individual, not neglecting the consideration of his hereditary antecedents, would alone suffice to set forth distinctly the causation of his insanity. If all the circumstances, internal and external, were duly scanned and weighed, it would be found that there is no accident in madness; the disease, whatever form it might take, by whatsoever complex concurrence of conditions, or by how many successive links of causation, it might be generated, would be traceable as the inevitable consequence of certain antecedents, as plainly as the explosion of gunpowder may be traced to its causes, whether the train of events of which it is the issue be long or short. The germs of insanity are sometimes latent in the foundations of the character, and the final outbreak is perbaps the explosion of a long train of antecedent preparations.'

(3) The phenomena of insanity also furnish a good illustration of the next source of error, the mistaking of joint effects for cause and effect. In this, as in many other diseases, symptoms are often mistaken for causes. Thus, it is not uncommon to hear violent religious excitement or inordinate grief adduced as causes of insanity, whereas these are probably merely incipient

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⁵⁴ Physiology and Pathology of Mind, Part. II. ch. i. p. 225.

symptoms, due, in the vast majority of cases, to precisely the same combination of physical and mental causes, which, when they operate with greater intensity, ultimately issue in definite and unmistakable insanity.

We have an instructive instance of the same error in some of the speculations respecting the origin of fevers. In Abdominal Typhus (the so-called Typhoïd or Enteric Fever of the English Physicians) the febrile symptoms (Pyrexia, Erethism, &c.) have been ascribed to certain lesions of the glandular structures of the intestines; but a wider observation has shown that the other symptoms often precede by some time the formation of the lesions, and that the fever may even run a fatal course, though it may be impossible, in a post-mortem examination, to detect the specific lesions in question. Practically, the correction of this and similar errors is of great importance, as much mischief may be done, and much time may be lost, by a mode of treatment which, through mistaking symptoms for causes, or co-effects for cause and effect, addresses itself only to the consequences of the malady, and leaves the real source of evil unattacked.

The following anecdote, told by Dr. Paris, affords an amusing illustration of the extent to which the ignorant, in reasoning on cause and effect, may be deceived by an invariable, or even frequent, concurrence of events.

'It should,' says he⁵⁹, 'be kept in mind, that two events may arise from a common cause, and be co-existent, and yet have not the most remote analogy to, or dependence upon,

^{*} Pharmacologia, p. 89.

each other. It was a general belief at St. Kilda, that the arrival of a ship gave all the inhabitants colds. Dr. John Campbell took a great deal of pains to ascertain the fact, and to explain it as the effect of effluvia arising from human bodies; the simple truth, however, was that the situation of St. Kilda renders a north-east wind indispensably necessary before a stranger can land,—the wind, not the stranger, occasioned the epidemic.'

In speculations on the history of language, languages, which recent investigation has shown to be related collaterally, were by older philologists erroneously regarded as standing to each other in the relation of parent and child. I extract from Professor Max Müller's Lectures on the Science of Language the following illustration, which will already be familiar to many of my readers:—

'A glance at the modern history of language will make this clearer. There never could be any doubt that the so-called Romance languages, Italian, Wallachian, Provençal⁶¹, French, Spanish, and Portuguese, were closely related to each other. Everybody could see that they were all derived from Latin. But one of the most distinguished French scholars, Raynouard, who has done more for the history of the Romance languages and literature than any one else, maintained that Provençal only was the daughter of Latin; whereas French, Italian, Spanish, and Portuguese were

^{*} First Series. Lecture V.

The exact relationship of French to Provençal may be represented thus: the Peasant Latin became in the South of France the Langue d'Oc (or Provençal), and in the North the Langue d'Oil, of which the French (or the dialect of the Isle de France) was the principal dialect, and has in its modern form become the language of the nation. See Brachet's *Historical Grammar* (Dr. Kitchin's Translation), p. 18; 7th ed. pp. 22-3.

the daughters of Provençal. He maintained that Latin passed, from the seventh to the ninth century, through an intermediate stage, which he called Langue Romane, and which he endeavoured to prove was the same as the Provençal of Southern France, the language of the Troubadours. According to him, it was only after Latin had passed through this uniform metamorphosis, represented by the Langue Romane or Provençal, that it became broken up into the various Romance dialects of Italy, France, Spain, and Portugal. This theory, which was vigorously attacked by August Wilhelm von Schlegel, and afterwards minutely criticised by Sir Cornewall Lewis, can only be refuted by a comparison of the Provençal grammar with that of the other Romance dialects. And here, if you take the auxiliary verb to be, and compare its forms in Provençal and French, you will see at once that, on several points, French has preserved the original Latin forms in a more primitive state than Provençal, and that, therefore, it is impossible to classify French as the daughter of Provençal, and as the granddaughter of Latin. We have in Provençal:-

sem, corresponding to the French nous sommes, etz ,, vous êtes, son ,, ils sont,

and it would be a grammatical miracle if crippled forms, such as sem, etz, and son, had been changed back again into the more healthy, more primitive, more Latin, sommes, êtes, sont; sumus, estis, sunt.

Let us apply the same test to Sanskrit, Greek, and Latin; and we shall see how their mutual genealogical position is equally determined by a comparison of their grammatical forms. It is as impossible to derive Latin from Greek, or Greek from Sanskrit, as it is to treat French as a modification of Provençal. Keeping to the auxiliary verb to be, we find that I am is in

Sanskrit Greek Lithuanian asmi esmi,

The root is as, the termination mi.

Now, the termination of the second person is si, which together with as, or es, would make

as-si es-si es-si.

But here Sanskrit, as far back as its history can be traced, has reduced assi to asi; and it would be impossible to suppose that the perfect, or, as they are sometimes called, organic, forms in Greek and Lithuanian, es-si, could first have passed through the mutilated state of the Sanskrit asi.

The third person is the same in Sanskrit, Greek, and Lithuanian, as-ti or es-ti; and, with the loss of the final i, we recognise the Latin est, Gothic ist, and Russian est.

The same auxiliary verb can be made to furnish sufficient proof that Latin never could have passed through the Greek, or what used to be called the Pelasgic stage, but that both are independent modifications of the same original language. In the singular, Latin is less primitive than Greek; for sum stands for es-um, es for es-is, est for es-ti. In the first person plural, too, sumus stands for es-umus, the Greek es-mes, the Sanskrit 'smas. The second person es-tis is equal to Greek es-te, and more primitive than Sanskrit stha. But in the third person plural Latin is more primitive than Greek. The regular form would be as-anti; this, in Sanskrit, is changed into santi. In Greek, the initial s is dropped, and the Æolic enti is finally reduced to eisi. The Latin, on the contrary, has kept the radical s, and it would be perfectly impossible to derive the Latin sunt from the Greek eisi.'

(4) A not uncommon source of error is the confusion of the proximate with the primary or remote cause of a phenomenon. To be on our guard against this error is often of the utmost practical importance: for the remo-

val of the proximate cause may only temporarily remove the effect, and the primary cause may, after a time, reproduce it; or, again, the removal of the primary cause may still leave the proximate cause in full action. This error is well exemplified in Mr. Lewes' account of Thirst.

'The sensation of Thirst is not merely a sensation dependent on a deficiency of liquid in the system, but a local sensation dependent on a local disturbance: the more water these men (the prisoners confined in the Black Hole at Calcutta) drank, the more dreadful seemed their thirst; and the mere sight of water rendered the sensation, which before was endurable, quite intolerable. The increase of the sensation following a supply of water, would be wholly inexplicable to those who maintain that the proximate cause of Thirst is deficiency of liquid; but is not wholly inexplicable, if we regard the deficiency as the primary, not the proximate cause: for this primary cause having set up a feverish condition in the mouth and throat, that condition would continue after the original cause had ceased to exist. The stimulus of cold water is only a momentary relief in this case, and exaggerates the sensation by stimulating a greater flow of blood to the parts. If, instead of cold water, a little lukewarm tea, or milk-and-water, had been drunk, permanent relief would have been attained; or if, instead of cold water, a lump of ice had been taken into the mouth, and allowed to melt there, the effect would have been very different-a transitory application of cold increasing the flow of blood, a continuous application driving it away.

'We must not, however, forget that, although, where a deficiency of liquid has occasioned a feverish condition of the mouth and throat, no supply of cold liquid will at once remove that condition, the relief of the Systemic sensation not immediately producing relief of the local sensation, nevertheless, so long as the system is in need of liquid, the feeling of thirst must continue. Claude Bernard observed that a dog which had an opening in its stomach drank unceasingly because the water ran out as fast as it was swallowed; in vain the water moistened mouth and throat on its way to the stomach. Thirst was not appeared because the water was not absorbed. The dog drank till fatigue forced it to pause, and a few minutes afterwards recommenced the same hopeless toil; but no sooner was the opening closed, and the water retained in the stomach, from whence it was absorbed into the system, than thirst quickly vanished.

In studying the history of a language, it is often most important to bear in mind that words ultimately derived from one language are proximately derived through the medium of another. Thus, there will occur to the reader numberless English words which have been derived from the Latin through the French, as, for instance, judge, noble, emperor, governor, prince. And, to quote M. Brachet:—

'When Jerome translated the Old Testament into Latin, he incorporated into his version certain Hebrew words which had no Latin equivalents, as seraphim, Gehenna, pascha, &c.; from Latin they passed at a later time into French (séraphin, gêne, pâque). But they entered French from the Latin, not from the Hebrew. The same is the case with the Arabic; its relations with French have been purely accidental. To say nothing of those words which express oriental things, such as Alcoran, bey, cadi, caravane, derviche, firman, janissaire, &c., which were brought into the west by travellers, the French language received, in the middle ages, many Arabic words from another source: the Crusades, the

^{*} Lewes' Physiology of Common Life, vol. i. pp. 45-47.

scientific greatness of the Arabians, the study of oriental philosophies, much followed in France between the twelfth and fourteenth centuries, enriched the vocabulary of the language with many words belonging to the three sciences which the Arabians cultivated successfully: in astronomy it gave such words as asimuth, nadir, zénith; in alchemy, alcali, alcool, alambic, alchimie, élixir, sirop; in mathematics, algèbre, zéro, chiffre. But even so these words did not come directly from Arabic to French; they passed through the hands of the scientific Latin of the middle ages. In fact, the oriental languages have had little or no popular or direct influence on French 68."

The non-recognition of these intermediate channels, through which the words of one language have been introduced into another, has often led to the most erroneous theories as to the connexion of languages or the relations subsisting between the people speaking them. Thus, it was once a favourite theory that all languages are derived from Hebrew, and the occurrence in different languages of the same words has often, without any other ground, been regarded as a proof of the connexion of the most diverse races.

I add an example from the science of Political Economy. It has often been supposed that high prices produce high wages. A sudden rise in the price of any particular class of commodities may lead, by a desire on the part of the producers to increase the supply, and by a consequent increase in the demand for labour in that particular department, to a temporary rise in wages.

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^{**} Historical Grammar, Translation, p. 22, note 2; 7th ed. p. 27, note 2.

But a rise in prices produces no permanent rise in wages, unless it leads to an increased accumulation of capital, that is, an augmentation of the fund available for the further production of wealth and, consequently, for the payment of wages. Here the rise in prices is the remote or primary, and the increased accumulation of capital is the proximate, cause of the phenomenon; but, as counteracting causes, such as reckless speculation or the adoption of a more luxurious style of living on the part of the capitalists, may prevent the rise in prices from being followed by an increased accumulation of capital, it is often of great importance to distinguish the two.

I have, thus far, discussed those errors which originate in overlooking the presence of some third circumstance. But, even when all the circumstances except the cause and effect (or what we suppose to be such) have been eliminated, we may still commit an error, either from mistaking the cause for the effect, or from neglecting to take account of their mutual action and reaction and being thus led erroneously to assign to one of the two exclusively the whole share in the production of the ultimate effect.

(5) The importance of not overlooking this latter source of error is well illustrated by the following remarks of Sir G. C. Lewis **:—

^{*} See Mill's Political Economy, Bk. II. ch. xi. § 2.

⁴³ On Methods of Observation and Reasoning in Politics, vol. i. P. 375-

'An additional source of error in determining political causation is likewise to be found in the mutuality of cause and effect. It happens sometimes that, when a relation of causation is established between two facts, it is hard to decide which, in the given case, is the cause and which the effect, because they act and re-act upon each other, each phenomenon being in turn cause and effect. Thus, habits of industry may produce wealth; while the acquisition of wealth may promote industry: again, habits of study may sharpen the understanding, and the increased acuteness of the understanding may afterwards increase the appetite for study. So an excess of population may, by impoverishing the labouring classes, be the cause of their living in bad dwellings; and, again, bad dwellings, by deteriorating the moral habits of the poor, may stimulate population. The general intelligence and good sense of the people may promote its good government, and the goodness of the government may, in its turn, increase the intelligence of the people, and contribute to the formation of sound opinions among them. Drunkenness is in general the consequence of a low degree of intelligence, as may be observed both among savages and in civilized countries. But, in return, a habit of drunkenness prevents the cultivation of the intellect, and strengthens the cause out of which it grows. As Plato remarks, education improves nature, and nature facilitates education. National character, again, is both effect and cause: it re-acts on the circumstances from which it arises. The national peculiarities of a people, its race, physical structure, climate, territory, &c., form originally a certain character, which tends to create certain institutions, political and domestic, in harmony with that character. These institutions strengthen, perpetuate, and reproduce the character out of which they grew, and so on in succession, each new effect becoming, in its turn, a new cause. Thus a brave, energetic, restless nation, exposed to attack from neighbours,

organises military institutions: these institutions promote and maintain a warlike spirit: this warlike spirit, again, assists the development of the military organisation, and it is further promoted by territorial conquests and success in war, which may be its result—each successive effect thus adding to the cause out of which it sprung.'

The difference between the calculated and observed velocities of sound (already noticed.) furnishes another illustration of the importance of attending to the mutual action of cause and effect. The wave of sound, in its passage through the air, developes heat by compression, and this heat, by augmenting the elasticity of the air, increases, in turn, the velocity with which the sound is transmitted. Thus the effect re-acts upon, and promotes the operation of, the original cause. It was from overlooking this fact that Newton's calculation of the velocity of sound fell short of the observed velocity by about one-sixth of the actual rate.

Malthus' speculations on the increase of population illustrate another form of the same error. He found that, in many cases, population increased faster than food increased. He inferred that this increase of population once begun would continue under all circumstances; and that therefore a time was at hand, in many countries, when the bulk of the people would be reduced almost to a state of starvation. He did not observe that, in this case, the effect re-acts upon the cause; not, however, in the way of promoting but of retarding its

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[•] Pp. 181-2.

operation. The tendency of an increase of population is certainly to diminish the supply of food; but, in attempting to forecast the ultimate result of this tendency, Malthus did not take sufficient account of the fact that the diminution in the supply of food has, in its turn, a tendency to arrest the increase of population.

Instances of the tendency of an effect to re-act upon its cause, in the way of diminishing its intensity, are very frequent in human affairs. Thus, when a man discovers that he is labouring under a disease, the additional prudence which he is induced to exercise will often not only arrest or retard the progress of the disease, but lead to the prolongation of his life beyond the usual term. Again, when a deficiency of sanitary arrangements has led to an increased mortality or the outbreak of a pestilence, the attention thus directed to the noxious influences at work will often result in their removal, or, at least, in some considerable alleviation of them. It is plain that, in speculating on the future, these are considerations which ought not to be left out of account.

(6) We may invert cause and effect, mistaking one for the other. This error is not infrequent in historical speculations, as, for instance, when some great event, such as the religious reformation of the sixteenth century, or the French Revolution, is assigned as the cause of a general change of opinion or of certain mental and social habits, whereas, in reality, the gradual, and often unobserved, operation of this change has been the

cause, and not the effect, of the historical event. In a case of this kind, however, the event may, in turn, have intensified, and, perhaps, given the sanction of authority to, the causes which produced it.

Again, a particular form of government, monarchical, aristocratical, democratical, or the like, is often assigned as the cause of certain peculiarities of social feeling or national character, whereas it would probably be far more correct to regard the form of government as due, in the first instance, to these peculiarities, though it, in turn, may have intensified the causes to which it was originally due.

In meteorological speculations it has been questioned whether the electrical phenomenon of lightning is the cause or effect of the sudden precipitations of rain and hail which it generally accompanies. Sir John Herschel (in opposition to the ordinary opinion ⁶⁷) maintains that it is the effect, and argues thus:—

'Whatever may be the state of the ultimate molecules of vapour, it seems impossible but that when a great multitude of them lose their vaporous state by cold, and coalesce into a drop or snow spangle, however minute, that drop will have collected and retained on its surface (according to the laws of electric equilibrium) the whole electricity of its constituent molecules, which will therefore have some finite, though very feeble tension. Now, suppose any number (1000 for instance) of such globules to coalesce, or that by successive deposition one should gradually grow to 1000 times its original volume. The diameter will be only 10, and the surface 100 times

[&]quot; Herschel's Meteorology, §§ 135, 137.

increased. But the electric contents, being the sum of those of the elementary globules, will be increased one thousand-fold, and, being spread entirely over the surface, will have a tenfold density (i.e. tension).

'It will easily be seen that, when thousands of these electriferous globules again further coalesce into rain drops, a great and sudden increase of tension at their surface must take place. Their electricity, then, is enabled to spring from drop to drop, and, rushing in an instant of time from all parts of the cloud to the surface, a flash is produced. Accordingly, in thunder-storms, it is the commonest of all phenomena to find each great flash succeeded by a sudden rush of rain at such an interval of time as may be supposed to have been occupied in its descent. The sudden precipitation of large quantities of rain, and especially of hail, which is formed in a cold region, where the insulating power of the air is great, is almost sure to be accompanied with lightning, which the usual perversity of meteorologists, where electricity is in question, long persisted, and even yet persists, with few exceptions, in regarding as the cause, and not the consequence, of the precipitation.'

A question has also been raised whether the copious precipitation of rain which usually takes place in the centre of a cyclone is the cause or the effect of the cyclone. The more probable view is that the partial vacuum produced by the rain-fall, and the consequent inrush of the surrounding atmosphere, is the cause of the cyclone.

Mr. M'Lennan, in his *Primitive Marriage*, conceives that marriage by capture arose from the custom of exogamy, that is to say, from the custom which forbad

marriage within the tribe. Sir John Lubbock 57, on the other hand, opposes this opinion, and regards exogamy as arising from marriage by capture, not marriage by capture from exogamy. 'Mr. M'Lennan's theory,' says he, 'seems to me quite inconsistent with the existence of tribes which have marriage by capture and yet are endogamous. The Bedouins, for instance, have unmistakeably marriage by capture, and yet the man has a right to marry his cousin, if only he be willing to give the price demanded for her.'

Professor Rogers, in his Manual of Political Economy **, calls in question the received opinion on the relation between the increase of population and the cultivation of inferior soils. Though I cannot accept his position, the passage will serve as an instance of the difficulty frequently experienced in determining which of two phenomena or events is cause and which is effect.

'There is not a shadow of evidence in support of the statement that inferior lands have been occupied and cultivated as population increases. The increase of population has not preceded but followed this occupation and cultivation. It is not the pressure of population on the means of subsistence which has led men to cultivate inferior soils, but the fact that these soils being cultivated in another way, or taken into cultivation, an increased population became possible. How could an increased population have stimulated greater labour in agriculture, when agriculture must have supplied the means on which that increased population could have ex-

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Origin of Civilisation and Primitive Condition of Man, ch. 3.

[•] p. 153.

isted⁷⁰? To make increased population the cause of improved agriculture is to commit the absurd blunder of confounding cause and effect.'

While agreeing with the ordinary theory that the pressure of population leads, in the first instance, to the cultivation of inferior lands, I should admit that the greater area of land under cultivation, by rendering possible a larger population, reacts upon and intensifies the original cause, an increased population leading to the cultivation of fresh lands, that rendering possible a still larger population, this in turn leading to the cultivation of fresh lands, and so on, till the process is arrested by counteracting causes. If this view be correct, the ordinary theory is more justly open to the charge of neglecting to take into account the 'mutuality' of cause and effect, noticed a few pages back, than of inverting their relation.

VI. The Argument from Analogy, as has already been stated, consists in drawing the conclusion that, because two or more phenomena resemble each other in certain observed points, they also resemble each other in certain other points beyond the range of our observation. The conditions with which such an inference, in order to be legitimate, must conform, need not be here repeated. If the conditions be not fulfilled, we may commit the error

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This question appears to ignore the fact that a population may have an insufficient supply of food, though what it does possess may be just competent to sustain life.

either of over-estimating the force of the analogy; of mistaking the direction in which it points, so as to regard an analogy which makes against a certain position as making for it, or the reverse; or, lastly, of supposing grounds of analogy to subsist where there are really none. The two former errors have been sufficiently exemplified in the chapter on Imperfect Inductions.

When we exaggerate the value of analogical evidence, or mistake the conclusion to be drawn from it, we may be led to do so either by over-rating the number of ascertained points of resemblance as compared with ascertained points of difference, or the reverse, or by miscalculating the extent of our knowledge of the phenomena. The examples referred to illustrate both sources of error. Thus, for instance, the points in which electricity resembles a fluid are obvious, while the points of difference are far less obtrusive, and, moreover, the unknown properties of electricity are probably out of all proportion to those which we know. In this case, too, when we include the consideration of heat, light, and similar agencies, the argument from analogy may be used against, rather than in favour of, the identification of electricity with a fluid.

The student need, however, hardly be reminded that an analogy which in one state of knowledge appears to be a strong one may, as knowledge advances, become extremely faint, worthless, or even positively unfavourable to the position which it was originally adduced to support.

The term False Analogy is, strictly speaking, applied

not to those cases in which we over-estimate the value of the analogy, or mistake the direction in which the argument points, but to those cases of analogical inference in which there exists no ground for any analogy whatever. Two phenomena, A, B, resemble each other in the possession of the properties a, b, c. The phenomenon A is observed also to present the property d, and hence it is inferred as probable that the same property is to be found also in B. Now it has already been pointed out that if we have any special reason for supposing d to be causally connected with any of the properties a, b, c, the argument ceases to be analogical, and becomes inductive. But if, on the other hand, we have any special reason for supposing that d is causally connected with none of the properties a, b, c, there is no room for any inference whatever. The whole force of the Argument from Analogy consists in the chance of d being causally connected with a, b, or c: if we have reason to believe that this is the case, the argument becomes more than analogical; if we have reason to believe that it is not the case, we are debarred from employing the argument altogether. Thus, in a certain sense, the Argument from Analogy is based on our ignorance; it is the result of a calculation of chances, which an accession of knowledge may invalidate, by either augmenting, diminishing, or annihilating it. Of False Analogy, in its strict sense, that is to say, the error of supposing that similarity or dissimilarity in certain points is an evidence of similarity or dissimilarity in other points, when more careful re-

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flexion or observation would lead to the belief that there is probably no connexion whatever between the observed points from which the Analogy proceeds and the unobserved points to which it argues, instances are extremely numerous in almost every branch of knowledge. As this form of Fallacy is so common, I shall subjoin several examples of it.

The following excellent illustration is quoted by Mr. Mill from Archbishop Whately's Rhetoric 11:

'It would be admitted that a great and permanent diminution in the quantity of some useful commodity, such as corn, or coal, or iron, throughout the world, would be a serious and lasting loss; and again that, if the fields and coal mines yielded regularly double quantities with the same labour, we should be so much the richer: hence it might be inferred that, if the quantity of gold and silver in the world were diminished one half, or were doubled, like results would follow; the utility of these metals, for the purposes of coin, being very great. Now there are many points of resemblance and many of difference between the precious metals on the one hand, and corn, coal, &c. on the other: but the important circumstance to the supposed argument is that the utility of gold and silver (as coin, which is far the chief) depends on their value, which is regulated by their scarcity, or rather, to speak strictly, by the difficulty of obtaining them; whereas, if corn and coal were ten times as abundant (i. e. more easily obtained), a bushel of either would still be as useful as now. But if it were twice as easy to procure gold as it is, a sovereign would be twice as large; if only

⁷¹ Mill's Logic, Bk. V. ch. v. § 6; Whately's Rhetoric, Part I. ch. ii. § 7. The passage does not occur in the earlier editions of Whately's Rhetoric.

half as easy, it would be of the size of a half-sovereign, and this (besides the trifling circumstance of the cheapness or dearness of gold ornaments) would be all the difference. The analogy, therefore, fails in the point essential to the argument.'

Respect for antiquity is often urged by an argument so sweeping as to assume the form of a False Analogy. 'Who are we,' it is said, 'that we should presume to think that we know better than previous generations?' Now, on many matters of fact, there can be no question that the belief of previous generations, when properly examined and sifted, must be accepted as final, inasmuch as they were contemporary, or nearly contemporary, with the original sources of information. To infer from this just and limited deference the necessity of an undiscriminating submission to the opinions of our ancestors, would be an instance of the fallacy of Inductio per Enumerationem Simplicem. But this, at least in many cases, seems not to be the nature of the argument, which appears rather to proceed on some such grounds as these: we reverence the opinions of the aged, because they have had more experience than we have had, and therefore, surely, on the same principle, we ought to accept the opinions of our ancestors, who lived in bygone generations. The point of resemblance is the fact of having been born at a period prior to ourselves, and hence it is inferred that the greater experience and the greater wisdom which are found to be concomitants of this fact in the case of many of our senior contemporaries

long since been dead. It, of course, escapes the notice of those who have recourse to this argument, that the average age of the persons living at any one time is about the same as that of those living at any other, and that superior wisdom is the consequence not of priority of birth but of greater experience. Thus far, the fallacy may be regarded as one of False Analogy, strictly so called. But there is another consideration which turns the edge of the argument. Experience grows with time, each generation not only inheriting the accumulated experience of previous generations, but adding to the stock its own acquisitions. 'Recte enim,' says Bacon 's,

72 Novum Organum, Lib. I. Aph. lxxxiv. In the first edition of this work I suggested that the reference might possibly be to Æschylus, Promethens Vinctus, 1. 981 : ἀλλ' ἐκδιδάσκει πάνθ' ὁ γηράσκων χρόνοι. Through the courtesy of the Rev. E. Marshall, I am now enabled to supply the true reference, which is to Aulus Gellius, Noctes Attica, Lib. XII. cap. 11: 'Alius quidam veterum poetarum, cujus nomen mihi nunc memorise non est, veritatem temporis filiam esse dixit.' It has also been pointed out to me that 'Veritas temporis filia' is the legend on the groats of Queen Mary, which were doubtless in use in Bacon's time. The following sentences occur in the same Aphorism of the Novum Organum: 'De antiquitate autem opinio, quam homines de ipsa fovent, negligens omnino est, et vix verbo ipsi congrua. Mundi enim senium et grandævitas pro antiquitate vere habenda sunt; que temporibus nostris tribui debent, non juniori setati mundi, qualis apud antiquos fuit. Illa enim ætas, respectu nostri, antiqua et major; respectu mundi ipsius, nova et minor fuit. Atque revera quemadmodum majorem rerum humanarum notitiam, et maturius judicium, ab homine sene expectamus, quam a juvene, propter experientiam, et rerum, quas vidit, et audivit, et cogitavit, varietatem et copiam; eodem modo et a nostra

'veritas temporis filia dicitur, non auctoritatis.' 'Antiquitas sæculi juventus mundi 78.'

Bishop Wilkins' Discovery of a New World contains

atate (si vires suas nosset, et experiri et intendere vellet) majora multo quam a priscis temporibus expectari par est; utpote atate mundi grandiore, et infinitis experimentis et observationibus aucta et cumulata.' Bentham in his Book of Fallacies, Part I. ch. il., and Sydney Smith in his review of that work (Edinburgh Review, No. laxxiv, reprinted in his Collected Works), have some very apposite and amusing remarks on this subject.

73 De Augmentis Scientiarum, Lib. I. Dr. Whewell in his Philosophy of Discovery (chap. xiii. § 4) appears to think that this celebrated Aphorism may be traced to Giordano Brano. 'It is worthy of remark that a thought which is often quoted from Francis Bacon, occurs in Bruno's Cena di Cenere, published in 1584; I mean, the notion that the later times are more aged than the earlier. In the course of the dialogue, the Pedant, who is one of the interlocutors, says, "In antiquity is wisdom;" to which the Philosophical Character replies, "If you knew what you were talking about, you would see that your principle leads to the opposite result of that which you wish to infer ;-I mean, that we are older, and have lived longer, than our predecessors." He then proceeds to apply this thought, by tracing the course of astronomy through the earlier astronomers up to Copernicus.' See Wagner's edition of Giordano Bruno's Works, vol. i. p. 132. In the original the passage runs thus :- ' Prudenzio. Sii come la si vuole, io non voglio discostarmi dal parer de gli antichi ; per che dice il saggio : Ne l'antiquità è la sapienza. Teofilo. E soggiunge: In molti anni la prudenza. Se vol intendeste bene quel che dite, vedreste, che dal vostro fondamento s' inferisce il contrario di quel che pensate: voglio dire, che noi siamo più vecchi et abbiamo più lunga età, che i nostri predecessori.' Mr. Spedding, however, in his edition of Bacon, questions whether Bacon intended the aphorism as a quotation, and thinks it probable that he did not derive it from any earlier writer.—See Ellis and Spedding's edition of Bacon, vol. i. p. 458, n. 4.

the following curious extract, translated from the work of Cardinal Nicolò de Cusa De doctà Ignorantià 74:

'We may conjecture the inhabitants of the sun are like to the nature of that planet, more clear and bright, more intellectual than those in the moon where they are nearer to the nature of that duller planet, and those of the earth being more gross and material than either, so that these intellectual natures in the sun are more form than matter, those in the earth more matter than form, and those in the moon betwixt both. This we may guess from the fiery influence of the sun, the watery and aerous influence of the moon, so also the material heaviness of the earth. In some such manner likewise is it with the regions of the other stars; for we conjecture that none of them are without inhabitants, but that there are so many particular worlds and parts of this one universe as there are stars, which are innumerable, unless it be to Him who created all things in number.'

The analogy in this case is founded not, as in the previous instances, on points of resemblance but on points of dissimilarity. The sun, the moon, and the earth are formed of different materials, and, therefore, it is argued, their inhabitants differ in their intellectual capacities, the exaltation of intelligence rising in proportion to the 'clearness and brightness' of the globe which they inhabit. Waiving the assumptions as to the materials of which the three bodies are composed and the habitation of them all by intelligent beings, it is plain that there is no presumption in favour of the theory that the intelligence of the inhabitants stands in

²⁴ Wilkins' Discovery of a New World in the Moon, p. 128; Cusanus, De docta Ignorantia, Lib. II. ch. xii.

any relation to the material of the globe on which they live; by parity of reasoning, birds ought to be far more intelligent than men.

The following passage from Bacon's Novum Organum⁷⁶ furnishes a remarkable example of a combination of Confusion of Language with False Analogy: 'Sed temporibus insequentibus, ex inundatione Barbarorum in imperium Romanum, postquam doctrina humana velut naufragium perpessa esset; tum demum philosophiæ Aristotelis et Platonis, tanquam tabulæ ex materia leviore et minus solida, per fluctus temporum servatæ sunt.' The student may exercise his sagacity in assigning its due share to each source of deception.

The arguments for or against the independence of colonies will often be found to rest on a False Analogy. Sometimes it is said that, under no circumstances, ought a colony to rebel against the authority of the mother-country; at other times, that, the colony having come to maturity, the time for its emancipation has arrived. In each of these cases the argument is suggested by the term 'mother-country.' Now the relations of the child to the parent are mainly determined by natural affection, by early associations, by gratitude for favours received, and frequently by the fact that, while the child is gradually approaching to the prime of life, the parent is gradually receding from it. Similar circumstances, though to a far weaker degree, may undoubtedly determine the relations of a colony to its 'mother-country,'

⁷⁸ Lib. I. Aph. lxxvii.

as, for instance, sympathy of race, the associations of many of the colonists with their early home, gratitude for assistance received at the foundation of the colony or during the earlier years of its existence, the growing prosperity of the colony or the waning power of the 'mother-country.' But, in addition to the fact that there are many cases in which these circumstances or some of them do not exist, or in which they exist only to the slightest extent, it must be plain, on reflexion, that the justice or injustice, the expediency or inexpediency, of separation from the mother-country or of repudiation by it must often be settled by considerations totally distinct from these, and such as receive no elucidation whatever from the relations between parent and child.

The illusion, originating in a false analogy, that every community must, like every individual man, pass through the three stages of growth, vigour, and decay, is thus exposed by Sir G. C. Lewis 74:

Methods of Observation and Reasoning in Politics, vol. ii. p. 438. The Rev. E. H. Hansell has pointed out to me a striking passage in Burke's 'Letters on a Regicide Peace,' in which Sir G. C. Lewis' notice of this fallacy is anticipated: 'I am not quite of the mind of those speculators who seem assured that necessarily, and by the constitution of things, all states have the same periods of infancy, manhood, and decrepitude, that are found in the individuals who compose them. Parallels of this sort rather furnish similitudes to illustrate or to adorn, than supply analogies from whence to reason. The objects which are attempted to be forced into an analogy are not found in the same classes of existence. Individuals are physical beings, subject to laws universal and invariable. The immediate cause acting in these laws may be obscure: the general results are subjects of certain calculation. But commonwealths are not physical

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'From what has been already said, it follows that the comparison which is sometimes instituted between the progress of a community and the life of a man fails in essentials, and is therefore misleading. Both a man and a community, indeed, advance from small beginnings to a state of maturity: but a man has an allotted term of life, and a culminating point from which he descends; whereas a community has no limited course to run; it has no necessary period of decline and decay, similar to the old age of a man; its national existence does not necessarily cease within a certain time. Nations, as compared with other nations, have periods of prosperity and power; but even these periods often ebb and flow, and when a civilised nation loses its pre-eminence -as Italy in the nineteenth, as compared with Italy in the fourteenth and sixteenth centuries—it does not necessarily lose its civilisation. A political community is renewed by the perpetual succession of its members; new births, immigrations, and new adoptions of citizens, keep the political body in a state of continuous youth. No such process as this takes place in an individual man. If he loses a limb, it is not replaced by a fresh growth. The effects of disease are but partially repaired; all the bodily and mental functions are gradually enfeebled, as life is prolonged, till at last decay inevitably ends in death: whereas a community might, consistently with the laws of human nature, have a duration co-extensive with that of mankind.

'The supposed analogy between the existence of a political community and the life of a man seems to have contributed to the formation of the belief in a liability to corruption, inherent in every society. It was a favourite doctrine among but moral essences. They are artificial combinations, and, in their proximate efficient cause, the arbitrary productions of the human mind. We are not yet acquainted with the laws which necessarily influence the stability of that kind of work made by that kind of agent.'—Works, vol viii. pp. 78, 79.

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some writers of the last century that every civilised community is fated to reach a period of corruption, when its bealthy and natural action ceases, and it undergoes some great deterioration. The notion of an inevitable stage of corruption in a nation was, indeed, partly suggested by the commonplaces condemnatory of luxury, derived both from the classical and ecclesiastical writers; and by the more modern eulogies of savage life. So far, however, as it was founded on the inevitable periods of decay in animal and vegetable life, the comparison was delusive; for the two relations which are brought together do not correspond. The death of individuals may, indeed, be considered a necessary condition for the progress of the society, into which they enter as temporary elements. It is by the substitution of new intelligences, and of natures not hardened to old customs, for minds whose thoughts and habits have learnt to move uniformly in the same groove, that progressive changes in human affairs are effected. The decay and death of the individual, therefore, tends not only to prevent the deterioration of the society, but to promote its improvement.'

Ancient medicine was full of false analogies. I select the following examples from Dr. Paris 77 :

'An example of reasoning by false analogy is presented to us by Paracelsus, in his work de vita longa, wherein, speaking of antimony, he exclaims, "Sicut antimonium finit aurum, sic, eadem ratione et forma, corpus humanum purum reddit."'

The alchemists, or some of them, appear to have imagined that the same preparation by which they hoped to convert the baser metals into gold (called metaphori-

^Π Pharmacologia, p. 64.

cally 'the healthy man') would also be effective in removing the sources of all bodily diseases. Why should not the impurities of the human body be removable by the same means as the impurities of the metals?

'They [that is, the Arabian physicians] conceived that gold was the metallic element in a state of perfect purity, and that all the other metals differed from it in proportion only to the extent of their individual contamination; and hence the origin of the epithet base, as applied to such metals. This hypothesis explains the origin of alchemy; but in every history we are informed that the earlier alchemists expected, by the same means that they hoped to convert the baser metals into gold, to produce an universal remedy, calculated to prolong indefinitely the span of human existence.

'It is difficult to imagine what connexion could exist in their ideas between the "Philosopher's Stone," which was to transmute metals, and a remedy which could arrest the progress of bodily infirmity: upon searching, however, into the writings of these times, it appears probable that this conceit may have originated with the alchemists from the application of false analogies, and that the error was subsequently diffused and exaggerated by a misconstruction of alchemical metaphors.'

The old maxim that 'Nature abhors a vacuum,' the curious belief, still prevalent even amongst persons of intelligence, that the weather changes with the 'changes' of the moon, the once fashionable doctrine of the 'Social Contract' or 'Original Compact,' the explanation of moral and physical facts by applying to them the conceptions of 'perfect numbers' and 'regular solids',' the

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⁷⁰ On this subject the reader will find some very curious informa-

Pythagorean theory of the Harmony of the Spheres, the Aristotelian doctrine of the Mean, and innumerable other instances with which the student will meet in his reading, will abundantly illustrate the nature of False Analogy and its frequency in the reasoning of early speculators.

The Argument from Final Causes 79, at least that tion in Mill's Logic, Bk. V. ch. v. § 6, and Whewell's History of the Inductive Sciences, Bk. IV. ch. iii. § 2.

" Tum vero, ad ulteriora tendens [intellectus humanus], ad proximiora recidit, videlicet ad causas finales, que sunt plane ex natura hominis, potius quam universi: atque ex hoc fonte philosophiam miris modis corruperant.'-Bacon, Nov. Org Lib. I. Aph. zlviii. To prevent misconception, I may state that I am far from denying that the Argument from Final Causes, if it take sufficient account of the evolution of organisms and their power of adapting themselves to external circumstances, and if it be based on the contemplation of Nature as a whole, instead of on that of individual objects, may admit of being stated in such a form as to occupy once more an important position in any scheme of Natural Theology. Bearing in mind these qualifications, it may be perfectly legitimate to speak, with reference to the universe at large, of design and a designer, whatever may have been the agency, and however mysterious and prolonged the process, by which an intelligent Creator may have worked. Theories of evolution may be so stated as not to impair, but indefinitely to exalt, our ideas of the power, wisdom, and benevolence of the Being in whom Nature had its source.

The student will find a very temperate statement of the prevalent theory, together with much useful information on the literature of the subject, in Sir H. Acland's *Harveian Oration* for 1865. On the other side he may, with most advantage, consult the works of Mr. Herbert Spencer and Mr. Darwin. I have discussed the subject, with special reference to the views of Bacon, in the Introduction to my edition of the *Novum Organum*, § 10.

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extreme form of it which assumes that every natural organism was specially designed to subserve some special object, and fashioned, once for all, in immediate reference to that object, appears ultimately to repose on a False Analogy. God or Nature (for both terms are used) is assimilated to a human artificer, and the argument appears to rest on the assumption that the motives, conceptions, and contrivances of the one may be regarded as similar to those of the other. 'Nature does nothing in vain.' 'Nature always acts for the best.' 'Everything is designed for some good purpose.' These and similar maxims express the general principle on which the argument rests. Of its application to special cases we may take the following examples.

The instances given by Bacon, in the Advancement of Learning and the De Augmentis *0, when protesting

^{*} Advancement of Learning, Bk. II. (Ellis and Spedding's edition, vol. iii. p. 358). Cp. De Augmentis, iii. 4. It should be noticed, however, that Bacon allows the use of Final Causes in what he calls 'Metaphysic.' Of the foregoing instances, 'and the like,' he says that they are 'well enquired and collected in Metaphysic; but in Physic they are impertinent.' And again: 'Not because these final causes are not true, and worthy to be enquired, being kept within their own province; but because their excursions into the limits of physical causes hath bred a vastness and solitude in that track.' What Bacon appears to mean (and the distinction is important) is that, in extra-physical speculations, as are those of Natural Theology (for the study of 'Metaphysics,' in the ordinary sense of the term, he repudiated), we may argue from an ascertained case of adaptation to the wisdom or goodness of the Creator, but that we are not justified in assuming adaptation or design as a datum in physical investigation. Those who defend this use of the argument, would

against the employment of Final Causes in physical enquiries, are the following: 'The hairs of the eye-lids are for a quickset and fence about the sight; the firmness of the skins and hides of living creatures is to defend them from the extremities of heat or cold; the bones are for the columns or beams, whereupon the frames of the bodies of living creatures are built; the leaves of trees are for protecting of the fruit; the clouds are for watering of the earth; the solidness of the earth is for the station and mansion of living creatures.'

The absurd extent to which the argument may be carried by speculators who attempt to find a Final Cause for every phenomenon which falls under their cognisance, will be plain from the examples which follow. It would, however, be unjust to charge these absurdities to the account of those writers of the past generation who took a more sober, though, perhaps, an erroneous view of the argument.

In the Timeus of Plato 11, the construction of the

reply that many discoveries (such as, notably, Harvey's discovery of the circulation of the blood, which set out from observing the action of the valves in the veins of many parts of the body, and enquiring into their purpose) have been suggested by the idea of adaptation (which, it may be noticed, does not necessarily include the idea of design). See Acland's Harveian Oration, and Dugald Stewart's Philosophy of the Human Mind, Part II. ch. xi. (Sir W. Hamilton's edition of Stewart's Works, vol. lii. p. 335, &c.) This fact may be, and, indeed, must be, admitted with respect to physiological enquiries (however the adaptation may be accounted for), and hence Bacon's prohibition is certainly too absolute.

at Of Plato, Bacon says truly, that he 'ever anchoreth on that shore.'

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whole universe, and specially of man, is explained on the principle of Final Causes. The following extract from Mr. Grote's *Plato* ** will serve as a specimen of the method there employed:

'The Demiurgus, having constructed the entire Kosmos, together with the generated Gods, as well as Necessity would permit-imposed upon these Gods the task of constructing Man: the second-best of the four varieties of animals whom he considered it necessary to include in the Kosmos. He furnished to them as a basis an immortal rational soul (diluted remnant from the soul of the Kosmos); with which they were directed to combine two mortal souls and a body. They executed their task as well as the conditions of the problem admitted. They were obliged to include in the mortal souls pleasure and pain, audacity and fear, anger, hope, appetite, sensation, &c., with all the concomitant mischiefs. By such uncongenial adjuncts the immortal rational soul was unavoidably defiled. The constructing Gods, however, took care to defile it as little as possible. They reserved the head as a separate abode for the immortal soul: planting the mortal soul apart from it in the trunk, and establishing the neck as an isthmus of separation between the two. Again the mortal soul was itself not single but double: including two divisions, a better and a worse. The Gods kept the two parts separate; placing the better portion in the thoracic cavity nearer to the head, and the worse portion lower down, in the abdominal cavity: the two being divided from each other by the diaphragm, built across the body as a wall of partition: just as, in a dwelling-house, the apartments of the women are separated from those of the men. Above the diaphragm, and near to the neck, was planted the energetic, courageous, contentious soul; so placed as to receive orders

Vol. iii. pp. 272-275.

easily from the head, and to aid the rational soul in keeping under constraint the mutinous soul of appetite which was planted below the diaphragm. The immortal soul was fastened or anchored in the brain, the two mortal souls in the line of the spinal marrow continuous with the brain: which line thus formed the thread of connexion between the three. The heart was established as an outer fortress for the exercise of influence by the immortal soul over the other two. It was at the same time made the initial point of the veins, -the fountain from whence the current of blood proceeded to pass forcibly through the veins round to all parts of the body. The purpose of this arrangement is that, when the rational soul denounces some proceeding as wrong (either on the part of others without, or in the appetitive soul within), it may stimulate an ebullition of anger in the heart, and may transmit from thence its exhortations and threats through the many small blood channels to all the sensitive parts of the body; which may thus be rendered obedient everywhere to the orders of our better nature.

'In such ebullitions of anger, as well as in moments of imminent danger, the heart leaps violently, becoming overheated and distended by excess of fire. The Gods foresaw this, and provided a safeguard against it by placing the lungs close at hand with the windpipe and trachea. The lungs were constructed soft and full of internal pores and cavities like a sponge; without any blood,—but receiving, instead of blood, both the air inspired through the trachea, and the water swallowed to quench thirst. Being thus always cool, and soft like a cushion, the lungs received and deadened the violent beating and leaping of the heart; at the same time that they cooled down its excessive heat, and rendered it a more equable minister for the orders of reason.

'The third or lowest soul, of appetite and nutrition, was placed between the diaphragm and the navel. This region of the body was set apart like a manger for containing necessary food; and the appetitive soul was tied up to it like a wild beast; indispensable indeed for the continuance of the race, yet a troublesome adjunct, and therefore placed afar off, in order that its bellowings might disturb as little as possible the deliberations of the rational soul in the cranium for the good of the whole. The Gods knew that this appetitive soul would never listen to reason, and that it must be kept under subjection altogether by the influence of phantoms and imagery. They provided an agency for this purpose in the liver, which they placed close upon the abode of the appetitive soul. They made the liver compact, smooth, and brilliant, like a mirror reflecting images:-moreover, both sweet and bitter on occasions. The thoughts of the rational soul were thus brought within view of the appetitive soul, in the form of phantoms or images exhibited on the mirror of the liver. When the rational soul is displeased, not only images corresponding to this feeling are impressed, but the bitter properties of the liver are all called forth. It becomes crumbled, discoloured, dark, and rough; the gall bladder is compressed; the veins carrying the blood are blocked up, and pain as well as sickness arise. On the contrary, when the rational soul is satisfied, so as to send forth mild and complacent inspirations,—all this bitterness of the liver is tranquillised, and all its native sweetness called forth. The whole structure becomes straight and smooth; and the images impressed upon it are rendered propitious. thus through the liver, and by means of these images, that the rational soul maintains its ascendancy over the appetitive soul; either to terrify and subdue, or to comfort and encourage it.

'Moreover, the liver was made to serve another purpose. It was selected as the seat of the prophetic agency; which the Gods considered to be indispensable, as a refuge and aid for the irrational department of man. Though this portion of the soul had no concern with sense or reason, they would

not shut it out altogether from some glimpse of truth. The revelations of prophecy were accordingly signified on the liver, for the instruction and within the easy view of the appetitive soul; and chiefly at periods when the functions of the rational soul are suspended-either during sleep, or disease, or fits of temporary extasy. For no man in his perfect senses comes under the influence of a genuine prophetic inspiration. Sense and intelligence are often required to interpret prophecies, and to determine what is meant by dreams or signs or prognostics of other kinds, but such revelations are received by men destitute of sense. To receive them, is the business of one class of men: to interpret them, that of another. It is a grave mistake, though often committed, to confound the two. It was in order to furnish prophecy to man, therefore, that the Gods devised both the structure and the place of the liver. During life, the prophetic indications are clearly marked upon it: but after death they become obscure and hard to decypher.

'The spleen was placed near the liver, corresponding to it on the left side, in order to take off from it any impure or excessive accretions or accumulations, and thus to preserve it clean and pure.'

Aristotle constantly employs this method of reasoning. Thus, in a familiar passage of the *Ethics* **, he says that 'if it is better for men to attain happiness through their own exertions than through chance, it is reasonable to suppose that this will be the case, since everything that depends on Nature ** is in the best possible condition.'

⁶⁸ Eth. Nic. i. 9 (5). El & έστὶν οὕτω βέλτιον ἡ διὰ τύχην εὐδαιμονείν, εὕλογον ἔχειν οὕτως, εἴπερ τὰ κατὰ φύσιν, ὡς οἴόν τε κάλλιστα ἔχειν, οὕτω πέφυκεν.

^{**} The student will notice the transition from the Demiurgus and Inferior gods of Plato to the 'Nature' of Aristotle. 'And in this,'

From his physiological works (in which the argument is most commonly employed) it will be sufficient to adduce one or two examples, which will serve also to show how a preconceived opinion may lead an author to invent false facts for the purpose of supporting his theory.

Having fixed the seat of sensation in the heart, inasmuch as it is in the centre of the body, rather than in the brain, as some philosophers had done, it was necessary to discover a special function for the brain. The necessity of discovering some function for it led to the fiction of its 'coldness,' which was supposed to counteract the heat of the heart, and so to preserve the body 'in a mean state 65.' On this account, he supposed, all animals which have blood are furnished with a brain, while bloodless animals, having little heat, require nothing to cool them, and are, therefore, without one. Moreover, in order to temper the coldness of the brain, blood is conveyed to the membrane which says Bacon, 'Aristotle is more to be blamed than Plato, seeing that he left out the fountain of final causes, namely God, and substituted Nature for God; and took in final causes themselves rather as the lover of logic than of theology.'-The Dignity and Advancement of Learning (Translation of the De Augmentis), Bk. III. ch. iv. (Ellis and Spedding's edition, vol. iv. p. 364.)

**Compare the extraordinary fancy (De Partibus Animalium, iii.

4) that the reason why the heart, in man, inclines slightly towards the left side is that it may temper the greater coldness of that side (πρὸς τὸ ἀνισοῦν τὴν κατάψυξιν τῶν ἀριστερῶν μάλιστα γὰρ τῶν ἄλλων ζοῦνν ἀνθρωπος ἔχει κατεψυγμένα τὰ ἀριστερά). It is needless to observe that the left side of man is not colder than the right; the fact is simply assumed in order to account for the position of the heart in a manner conformable with Aristotle's theories.

envelopes it by means of veins or channels. But, again, lest the heat so conveyed should injure the brain, the veins, instead of being large and few, are small and many, and the blood conveyed, instead of being copious and thick, is thin and pure **.

'The viscera are formed out of the blood, and therefore are only found in sanguineous animals, which necessarily have a heart: for it is clear that, having blood, which is a fluid, they must have a vessel to contain it, and hence also Nature has created veins; and for these veins the origin must necessarily be one, since one, whenever possible, is better than many. The heart is the origin of the veins: this is seen in the fact that they spring from it, and do not go through it; also they resemble it in structure. The heart has the chief position, namely, that of the centre, but more upwards than downwards, and rather in front than behind: for Nature is accustomed to seat the noblest in the noblest place, unless any stronger reason prevails: oð μή τι κωλύει μεῖζον⁶⁷.

The work of Bishop Wilkins, already quoted, furnishes some curious examples of the arguments which, even within the last two hundred years, have found favour with men distinguished for their scientific attainments.

'Though there are some who think mountains to be a deformity to the earth, as if they were either beat up by the flood, or else cast up like so many heaps of rubbish left at the

^{*} De Partibus Animalium, ii. 7. Cp. Lewes' Aristotle, § 164 p. 180.

⁴⁷ De Partibus Animalium, iii. 4. I here quote Mr. Lewes' summary, given in § 395, p. 310, of his Aristotle.

Bishop Wilkins was one of the founders of the Royal Society, and enjoyed one of the highest scientific reputations of his time.

Creation; yet, if well considered, they will be found as much to conduce to the beauty and conveniency of the universe, as any of the other parts. Nature (saith Pliny) purposely framed them for many excellent uses: partly to tame the violence of greater rivers, to strengthen certain joints within the veins and bowels of the earth, to break the force of the sea's inundation, and for the safety of the earth's inhabitants, whether beasts or men ⁵⁹.'

'I have now sufficiently proved that there are hills in the moon, and hence it may seem likely that there is also a world; for, since Providence hath some special end in all its works, certainly then these mountains were not produced in vain; and what more probable meaning can we conceive there should be, than to make that place convenient for habitation²⁰?'

'It hath been before confirmed that there was a sphere of thick vaporous air encompassing the moon, as the first and second regions do this earth. I have now showed that thence such exhalations may proceed as do produce the comets. Now from hence it may probably follow that there may be wind also and rain, with such other meteors as are common amongst us. This consequence is so dependent that Fromondus dares not deny it, though he would (as he confesses himself); for, if the sun be able to exhale from them such fumes as may cause comets, why not such as may cause winds, why not then such also as may cause rain, since I have above showed that there is sea and land, as with us? Now rain seems to be more especially requisite for them, since it may allay the heat and scorchings of the sun, when he is over their heads. And Nature hath thus provided for those in Peru, with the other inhabitants under the line"."

One of the most whimsical applications of the Argu-

A Discovery of a New World in the Moon, p. 77.

^{ps} Id. p. 91. ^{pt} Id. p. 121. ^{pt}

ment from Final Causes is to be found in the 'Doctrine of Signatures,' of which Dr. Paris thus speaks **.

'But the most absurd and preposterous hypothesis that has disgraced the annals of medicine, and bestowed medicinal reputation upon substances of no intrinsic worth, is that of the "DOCTRINE OF SIGNATURES," as it has been called, which is no less than a belief that every natural substance, which possesses any medicinal virtues, indicates, by an obvious and well-marked external character, the disease for which it is a remedy, or the object for which it should be employed. This extraordinary monster of the fancy has been principally adopted and cherished by Paracelsus, Baptista Porta, and Crollius, although traces of its existence may certainly be discovered in very ancient authors.

'The conceit, however, did not assume the importance of a theory until the end of the fourteenth century, at which period we find several authors engaged in the support of its truth, and it will not be unamusing to offer a specimen of their sophistry: they affirm that, since man is the lord of the creation, all other creatures are designed for his use, and therefore that their beneficial qualities and excellences must be expressed by such characters as can be seen and understood by every one; and as man discovers his reason by speech, and brutes their sensations by various sounds, motions, and gestures, so the vast variety and diversity of figures, colours, and consistencies, observable in inanimate creatures, is certainly designed for some wise purpose. must be, in order to manifest those peculiar properties and excellences, which could not be so effectually done in any other way, not even by speech, since no language is universal. Thus, the lungs of a fox must be a specific for

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^{**} Pharmacologia, pp. 47-50.

asthma, because that animal is remarkable for its strong powers of respiration. Turmerick has a brilliant yellow colour, which indicates that it has the power of curing jaundice; by the same rule, Poppies must relieve diseases of the head;... and the Euphrasia (eye-bright) acquired fame as an application in complaints of the eye, because it exhibits a black spot in its corolla resembling the pupil. In the curious work of Chrysostom Magnenus (Exercit. de Tabaco), we meet with a whimsical account of the signature of tobacco. "In the first place," says he, "the manner in which the flowers adhere to the head of the plant indicates the infundibulum cerebri, and pituitary gland; in the next place, the three membranes, of which its leaves are composed, announce their value to the stomach, which has three membranes."

'The blood-stone, the *heliotropium* of the ancients, from the occasional small specks or points of a blood-red colour exhibited on its green surface, is even at this day employed in many parts of England and Scotland to stop a bleeding from the nose; the nettle-tea continues a popular remedy for *urticaria*.

'It is also asserted that some substances bear the SIGNA-TURES of the humours, as the petals of the red rose that of the blood, and the roots of rhubarb, and the flowers of saffron, that of the bile.

'I apprehend that John of Gaddesden, in the fourteenth century, celebrated by Chaucer, must have been directed by some remote analogy of this kind, when he ordered the son of Edward I, who was dangerously ill with the small-pox, to be wrapped in scarlet cloth, as well as all those who attended upon him, or came into his presence; and even the bed and room in which he was laid were covered with the same drapery; and so completely did it answer, say the credulous

historians of that day, that the prince was cured without having so much as a single mark left upon him.'

In these and similar instances, which might be multiplied to almost any extent 15, it is plain that much is gained by the employment of the vague word Nature. Presuming that the majority of at least the more modern writers who have employed the Argument from Final Causes, if pressed to attach a definite meaning to the word Nature, would reply that they regard it, in this connexion, as only another name for God, the argument, as employed in the above and similar examples (I am not here discussing the more refined employment of it), seems to rest on the three following assumptions:—

- (1) That God [or Nature] acts, not by laws, governing the evolution of natural objects, but after the manner of a human artificer, having in view some special end in the production of each object and of each separate part of it.
- (2) That all objects are designed for the good of man, or, at least, of sentient or intelligent beings.
- (3) That we are so well acquainted with what is, on the whole, good for ourselves, or others, or the world at large, as well as with the general plan of the universe, that we are able, in each case, to pronounce positively

The following example (taken from Plutarch, De Stoicorum Repugnantiis, p. 1042, by Mr. Lecky, in his History of European Morals, from Augustus to Charlemagne, vol. ii. p. 174, note 2) is perhaps unsurpassed in absurdity: 'Chrysippus maintained that cock-fighting was the final cause of cocks, these birds being made by Providence in order to inspire us by the example of their courage.'

()) [

on the ends which God [or Nature] proposed to himself in his constructions *4.

Of these three assumptions, the first and second are, as I conceive, based on false analogies, the first transferring to God [or Nature] the habit, observed in the human artificer, of producing each object with reference to some special end, and the second the motives which usually guide the artificer in the selection of those ends.

The 'principle' laid down by Descartes (De Principiis Philosophia, i. 28) supplies an appropriate commentary on this assumption: 'Ita denique nullas unquam rationes circa res naturales a fine, quem Deus aut natura in its faciendis sibi proposuit, desumemus; quia non tantum nobis debemus arrogare, ut ejus consiliorum participes nos esse putemus.'

It is interesting to compare the following extracts from Galileo's Systema Cosmicum, Dial. III. (Sir Thomas Salusbury's translation, Pp. 333, 334): -

'SALV. Methinks we arrogate too much to our selves, Simplicius, whilst we will have it that the onely care of us is the adæquate work and bound, beyond which the Divine Wisdome and Power doth or disposeth of nothing. If one should tell me that an immense space interposed between the Orbs of the Planets and the Starry Sphere, deprived of stars and idle, would be vain and useless, as likewise that so great an immensity for receipt of the fixed stars as exceeds our utmost comprehension would be superfluous, I would reply that it is rashnesse to go about to make our shallow reason judg of the Works of God, and to call vain and superfluous whatsoever thing in the Universe is not subservient to us.'

'SAGR. Say rather, and I believe you would say better, that we know not what is subservient to us; and I hold it one of the greatest vanities, yea follies, that can be in the World, to say, because I know not of what use *Jupiter* or *Saturn* are to me, that therefore these Planets are superfluous, yea more, that there are no such things in rerum natura.'

356 FALLACIES INCIDENT TO INDUCTION.

The third assumption, it need hardly be added, involves a generalisation from a very narrow range of experience to operations co-extensive with all space and all time.

Even though these various errors have been avoided, and the inductive process has been correctly performed, it is still possible, either through confusion of language, through mistaking the question at issue, or through drawing erroneous inferences in our subsequent deductions, to arrive at false conclusions. But these are considerations which properly appertain to the other branch of Logic, which is concerned with deductive reasoning.

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